

# Parallel Processing of Graphs

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This talk is about graph processing  
from a pragmatic point of view ...

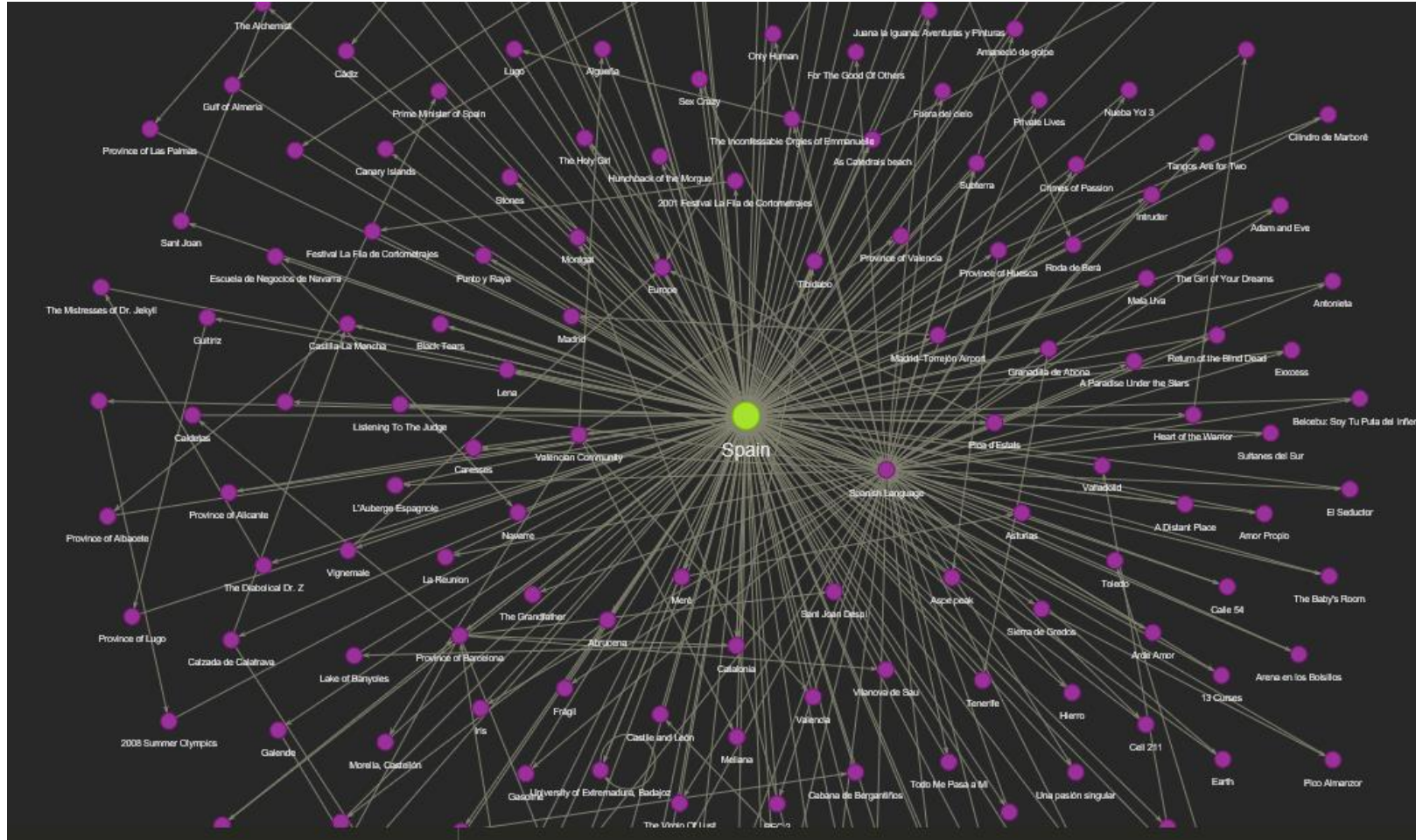
Appetizer

# Entities related to Spain

```
KnowledgeGraph
  .StartFrom(519480106787667)
  .VisitNode(_ => _.continue_if(_.dice(0.1)))
  .VisitNode(_ => _.continue_if(_.dice(0.1)))
  .VisitNode(_ => _.return_if(_.has_cell_id(519480106787667)))
```

**A graph query example**

# Entities related to Spain

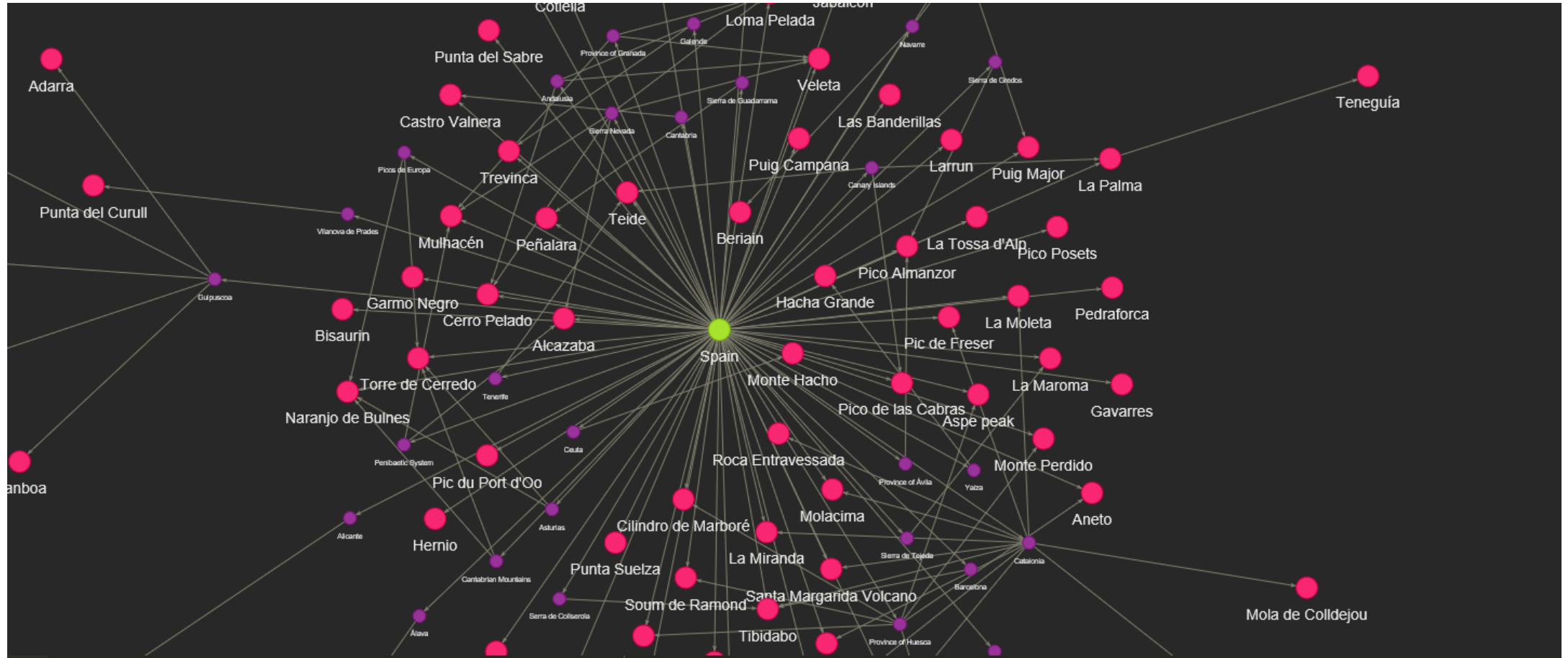


# Mountains in Spain

```
KnowledgeGraph
  .StartFrom("Spain")
  .FollowEdge("location_location_contains")|
  .VisitNode(_ => Action.Continue & _.return_if(_.type("geography_mountain")))
  .FollowEdge("location_location_contains")
  .VisitNode(_ => _.return_if(_.type("geography_mountain")))
```

**A graph query example**

# Mountains in Spain



# Outline

- Graph processing scenarios
- Challenges of large graph processing
- General design principles
- Offline analytics
- Online query processing
- Graph generation
- Case study
- Advance topics



# Outline

- Graph processing scenarios
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# Graph processing scenarios

Online query processing + Offline analytics

# A real-life **relation search** scenario

## A News Headline

**Tom Cruise** Admits **Katie Holmes** Divorced Him To Protect **Suri** From Scientology

- 1 **Tom Cruise** – people.person.marriage – (**marriage**) – time.event.person – **Katie Holmes**
- 2 **Tom Cruise** – people.person.children – (**Suri Cruise**) – people.person.parent – **Katie Holmes**
- 3 **Tom Cruise** – film.actor.film – (**Bambi Verleihung 2007**) – film.filmactor – **Katie Holmes**
- 4 ...

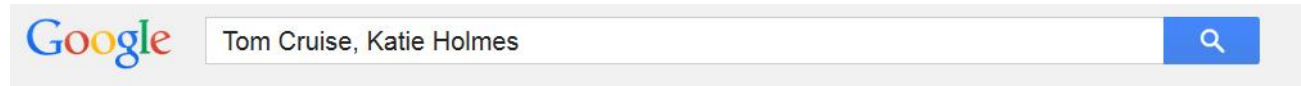
# Relation search in knowledge graph

Entity A . . .  $\rightsquigarrow$  Entity B

## Multi-hop Relation Search

- Discover the **hidden relations** between entities
- Enable more than what entity indexes can support

# Search results of Google



[Web](#) [News](#) [Images](#) [Videos](#) [Shopping](#) [More ▾](#) [Search tools](#)

About 19,600,000 results (0.40 seconds)

## Tom Cruise Admits Katie Holmes Divorced Him To Protect ...



[www.huffingtonpost.com/.../tom-cruise-katie-holmes-protect-su...](http://www.huffingtonpost.com/.../tom-cruise-katie-holmes-protect-su...) ▾

by Stephanie Marcus

Nov 8, 2013 - **Tom Cruise** has admitted that **Katie Holmes** filed for divorce in part because of his involvement in the controversial Church of Scientology.

## Images for Tom Cruise, Katie Holmes

[Report images](#)



## More images for Tom Cruise, Katie Holmes

## Tom Cruise Comes Clean on Role of Scientology in Divorce ...

[abcnews.go.com](http://abcnews.go.com) ▸ [Entertainment](#) ▾ [ABC News](#) ▾

Nov 9, 2013 - Amidst his court battle against tabloid headlines, **Tom Cruise** admitted that ex-wife **Katie Holmes** filed for divorce "to protect Suri from ...

## Tom Cruise admits Katie Holmes left to protect Suri from ...



[www.nydailynews.com/.../tom-cruise-ad...](http://www.nydailynews.com/.../tom-cruise-ad...) ▾ [New York Daily News](#) ▾

by Bill Hutchinson - in 29 Google+ circles

Nov 7, 2013 - **Tom Cruise** has admitted in an explosive court deposition that actress **Katie Holmes** fled their marriage to protect their daughter from ...

# Search results of Bing

MS Beta 4,340,000 RESULTS Any time ▾

## News about Tom Cruise, Katie Holmes

[bing.com/news](http://bing.com/news)



**KATIE HOLMES DATING JAMIE FOXX RUMORS CONTINUE AS THE ACTRESS' EX-HUSBAND, TOM CRUISE WAS REPORTED TO HAVE FINALLY MOVED ON**

*Travelers Today* · 3 days ago  
Katie Holmes dating rumors again sparked as her ex-husband Tom Cruise was reportedly dating other woman and that...

**Is Tom Cruise Dating Laura Prepon - Katie Holmes Ex Lands Scientologist Girlfriend?**  
*The National Ledger* · 10 days ago

**Katie Holmes Celebrates Suri Cruise's 8th Birthday**  
*WebProNews* · 3 days ago

## Images of Tom Cruise, Katie Holmes

[bing.com/images](http://bing.com/images)



## Katie Holmes Celebrates Suri Cruise's 8th Birthday ...



[www.webpronews.com/katie-holmes-celebrates-suri-cruises-8th...](http://www.webpronews.com/katie-holmes-celebrates-suri-cruises-8th...)  
Katie Holmes helped daughter Suri Cruise celebrate her 8th birthday in style. She treated her daughter, along with a few guests, to dinner at Nobu Next ...

## Tom Cruise: Katie Holmes Divorce Was A Surprise (UPDATE)

[www.huffingtonpost.com/2013/04/09/tom-cruise-katie-holmes-divorce...](http://www.huffingtonpost.com/2013/04/09/tom-cruise-katie-holmes-divorce...)  
Apr 09, 2013 · Tom Cruise says Katie Holmes divorce was a surprise. Here, the former couple is pictured at the "Mission Impossible: Ghost Protocol" premiere in Dec. 2011.

## See results for



**Katie Holmes**  
American Actress  
Kate Noelle "Katie" Holmes is an American actress and model who first achieved fame for her role as Joey Pot...



**Tom Cruise**  
Film Actor  
Tom Cruise, is an American film actor and producer. He has been nominated for three Academy Awards and h...

## Related searches

- Tom Cruise Katie Holmes **Married**
- Tom Cruise Katie Holmes **Gossip**
- Tom Cruise Katie Holmes **Photos**
- Tom Cruise Katie Holmes **Baby**
- Tom Cruise Katie Holmes **Unusual Marriage**
- Katie Holmes Tom Cruise **Split**
- Tom Cruise Katie Holmes **Suri Custody Settlement**
- Leah Remini Problems Started** Tom Cruise **Wedding**

# Relation search in knowledge graph

Satori

**Tom Cruise, Mimi Rogers, Nicole Kidman, Katie Holmes**

[Results](#) [View](#)

94 Results (103 ms)

Results
o--film.actor.film-->(Eyes Wide Shut)--film.film.actor-->(Nicole Kidman)
o--film.actor.film-->(National Movie Awards)--film.film.actor-->(Katie Holmes)
o--film.actor.film-->(InStyle: Celebrity Weddings)--film.film.actor-->(Katie Holmes)
o--people.person.marriage-->(marriage)--time.event.person-->(Katie Holmes)
o--people.person.marriage-->(marriage)--time.event.person-->(Nicole Kidman)
o--film.actor.film-->(War of the Worlds: UK Premiere Special)--film.film.actor-->(Katie Holmes)
o--film.producer.film-->(The Others)--award.nominated_work.nomination-->(nomination)--award.nomination.nominee--(Nicole Kidman)
o--people.person.children-->(Connor Cruise)--people.person.siblings-->(Isabella Jane Cruise)--people.person.parent--(Nicole Kidman)
o--film.producer.film-->(The Others)--award.nominated_work.nomination-->(nomination)--award.nomination.nominee--(Nicole Kidman)
o--film.actor.performance-->(performance)--film.performance.film-->(Eyes Wide Shut)--film.film.actor--(Nicole Kidman)

[Prev Page](#) [Next Page](#)

# Relation search in knowledge graph

Satori

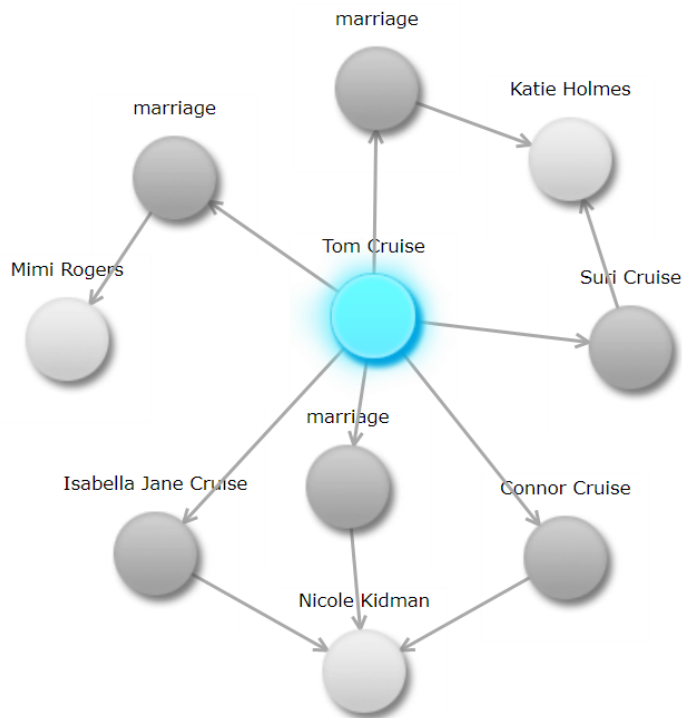
Add

Search

**Tom Cruise, Mimi Rogers, Nicole Kidman, Katie Holmes**

Results

[View](#)



## Tom Cruise



Tom Cruise (born Thomas Cruise Mapother IV; July 3, 1962), is an American film actor and producer. He has been nominated for three Academy Awards and has won three Golden Globe Awards. He started his career at age 19 in the 1981 film *Endless Love*. After portraying supporting roles in *Taps* (1981) and *The Outsiders* (1983), his first leading role was in *Risky Business*, released in August 1983. Cruise became a full-fledged movie...

### Types

award.nominee, award.winner, film.actor, film.director, film.producer, film.story\_contributor ...

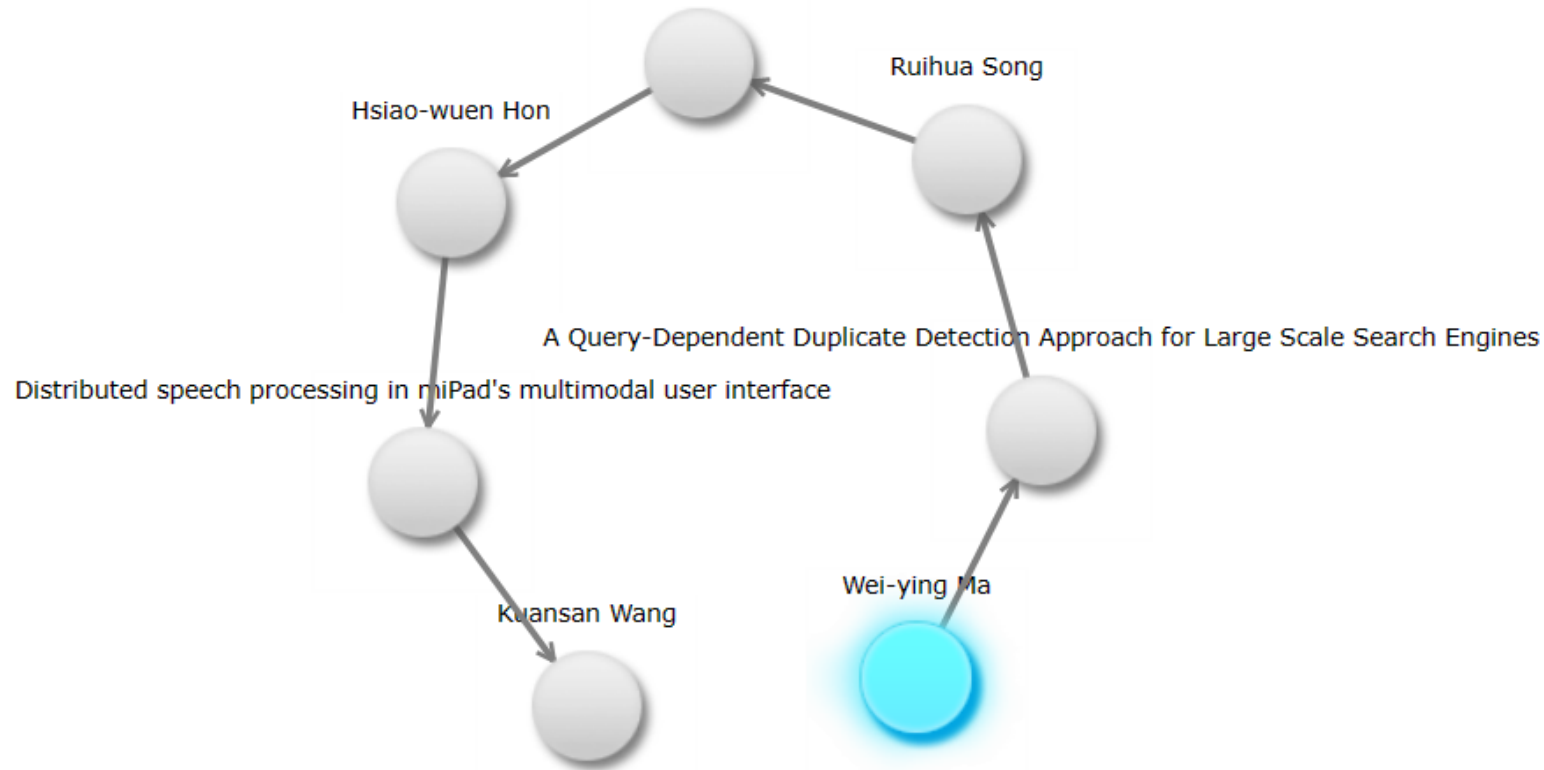


# Academic graph

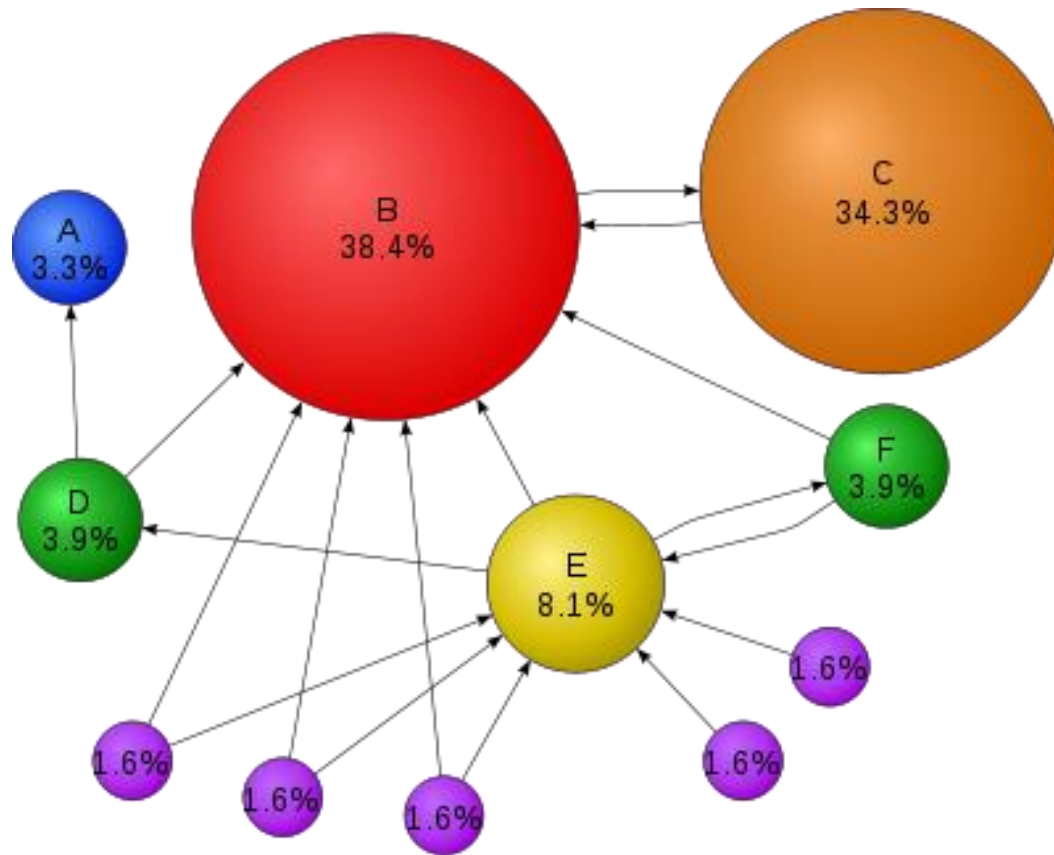
CoAuthor Search  ⇄

**Wei-Ying Ma (Microsoft) --> Kuansan Wang (Microsoft)**

Identifying ambiguous queries in web search



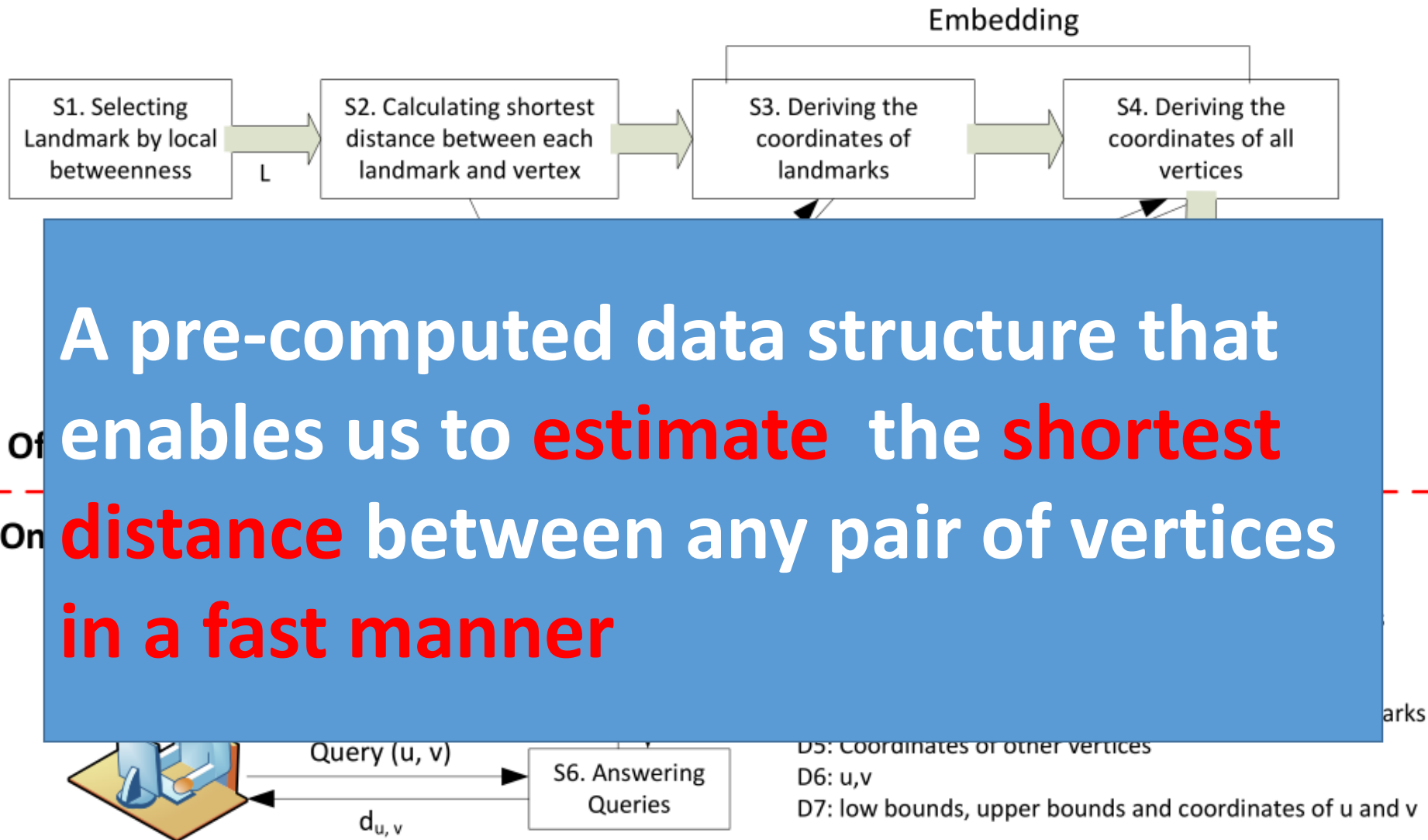
# Offline analytics example: PageRank



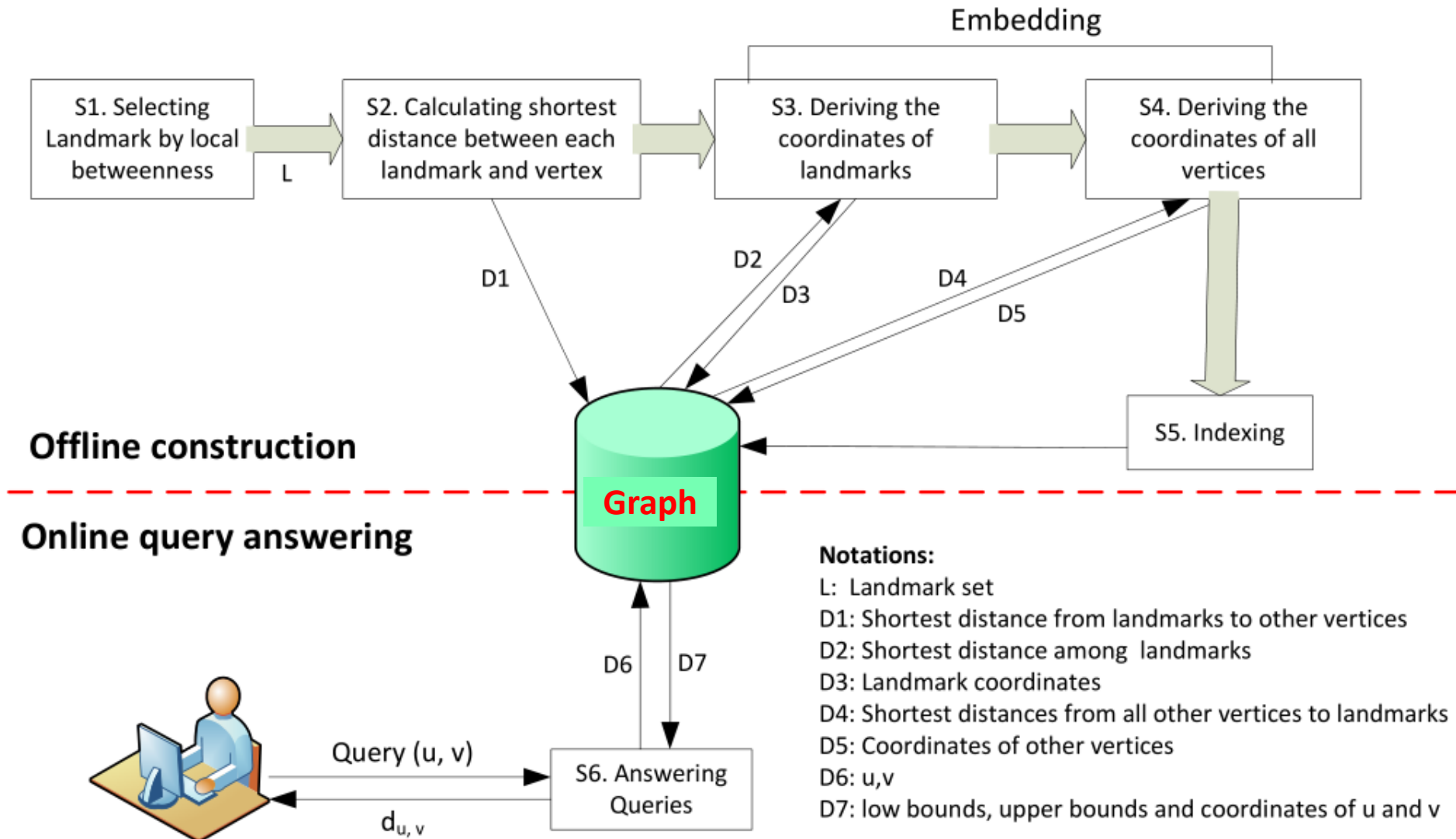
An important algorithm behind Google, Bing, ...

Query processing + offline analytics

# Architecture of distance oracle [Qi et al. vldb 2014]



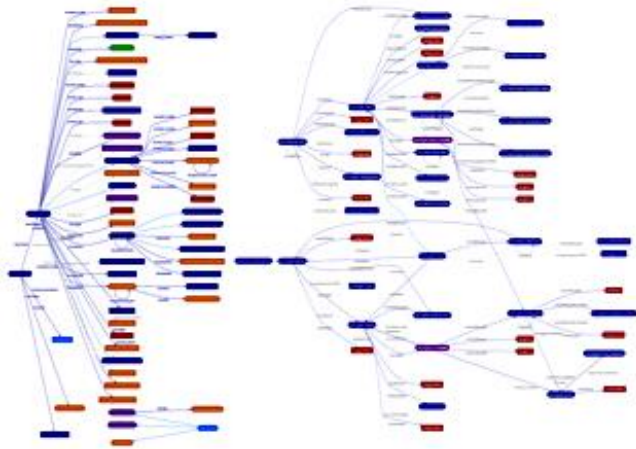
# Architecture of distance oracle [Qi et al. vldb 2014]



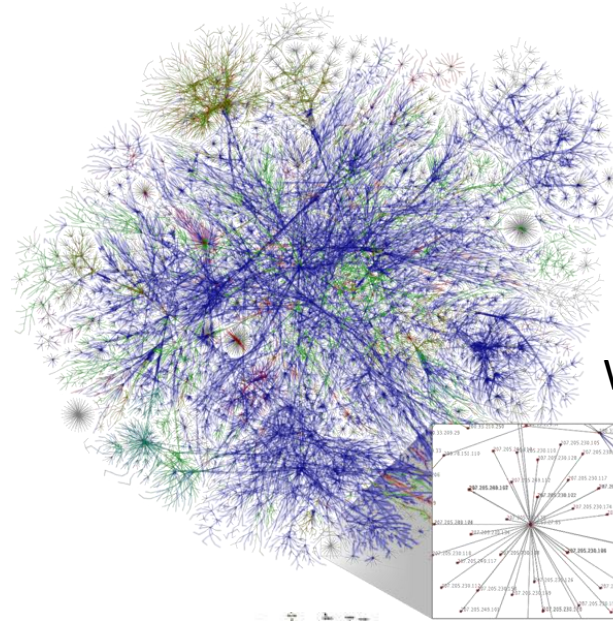
# Outline

- Graph processing scenarios
- **Challenges of large graph processing**
- General design principles
- *Offline analytics*
- Online query processing
- Graph generation
- Case study
- Advance topics

# Challenge I: diversity of graphs



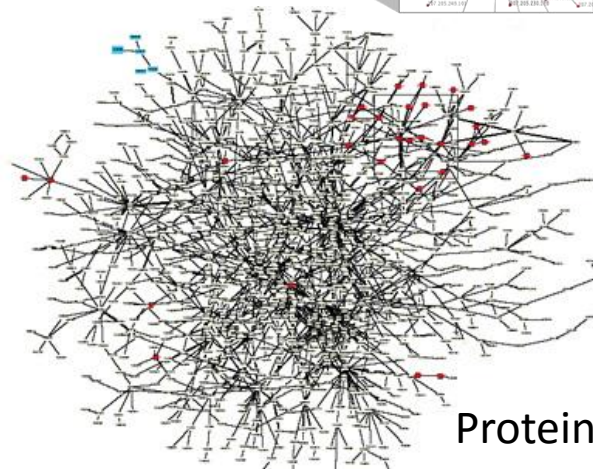
Schema Graph



Web Graph



Social Network



Protein Interaction Network

Do we need to design algorithms for each type of graphs?

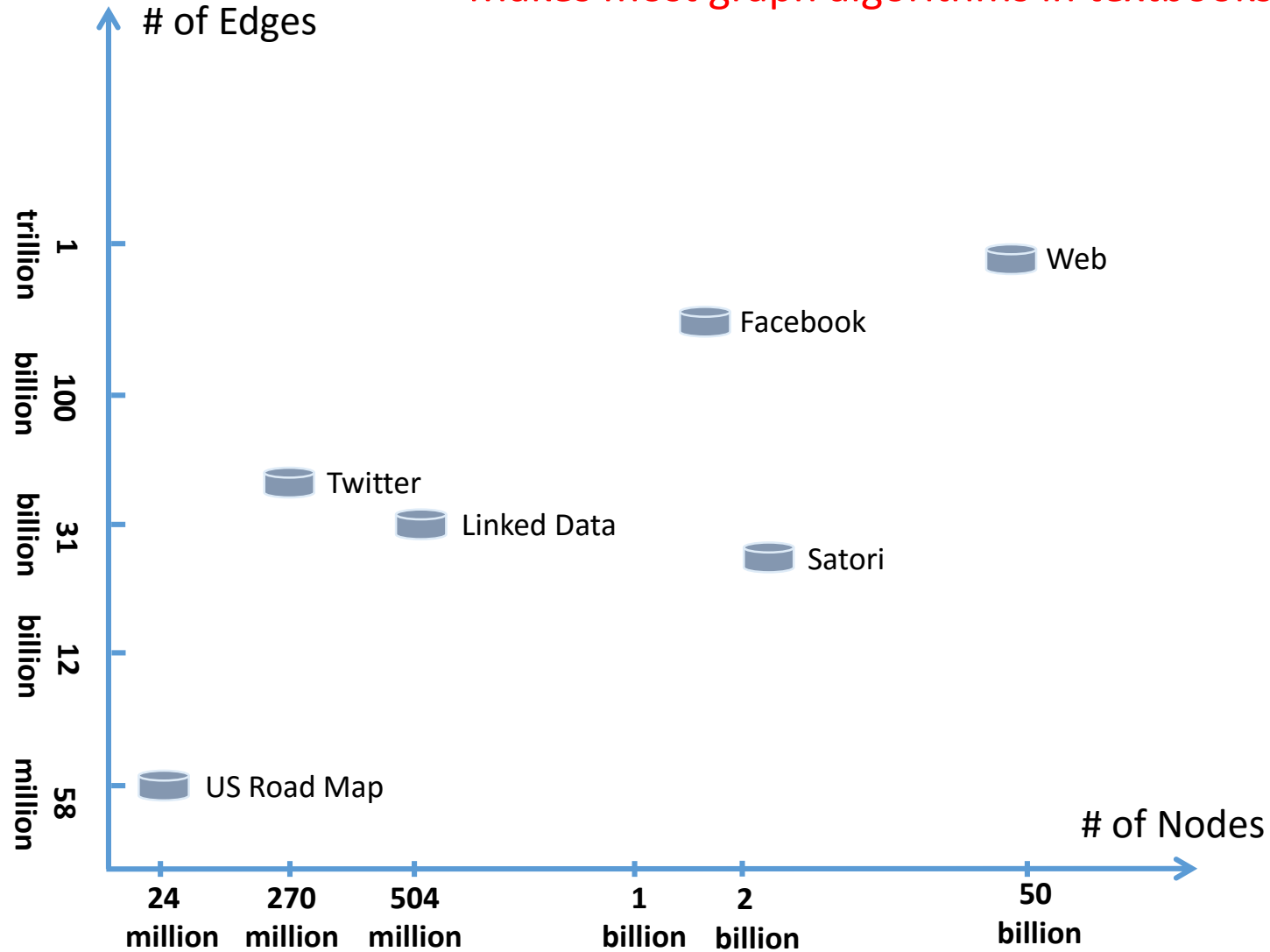
# Challenge II: diversity of computations

- Online query processing
    - Shortest path query
    - Subgraph matching query
    - SPARQL query
    - ...
  - Offline graph analytics
    - PageRank
    - Community detection
    - ...
  - Other graph operations
    - Graph generation, visualization, interactive exploration, etc.
- Do we need to implement systems for each graph operation?



# Challenge III: the scale of graphs

Makes most graph algorithms in textbooks ineffective!



# Existing systems

- Mature data processing systems
  - RDBMS
  - Map Reduce Systems
- Systems specialized for certain graph operations:
  - PageRank, FlockDB
- General-purpose graph processing systems
  - Neo4j, Trinity, Horton, HyperGraphDB, TinkerGraph, InfiniteGraph, Cayley, Titan, PEGASUS, Pregel, Giraph, GraphLab, GraphChi, GraphX ...

# Representative graph processing systems

	Property graphs	Online query	Data sharding	In-memory storage	Atomicity & Transaction
★	Neo4j	Yes	Yes	No	Yes
★	Trinity	Yes	Yes	Yes	Atomicity
★	Horton	Yes	Yes	Yes	No
★	HyperGraphDB	No	Yes	No	Yes
★	FlockDB	No	Yes	Yes	Yes
★	TinkerGraph	Yes	Yes	No	Yes
★	InfiniteGraph	Yes	Yes	Yes	No
★	Cayley	Yes	Yes	SB	SB
★	Titan	Yes	Yes	SB	SB
★	MapReduce	No	No	Yes	No
★	PEGASUS	No	No	Yes	No
★	Pregel	No	No	Yes	No
★	Giraph	No	No	Yes	No
★	GraphLab	No	No	Yes	No
★	GraphChi	No	No	No	No
★	GraphX	No	No	Yes	No

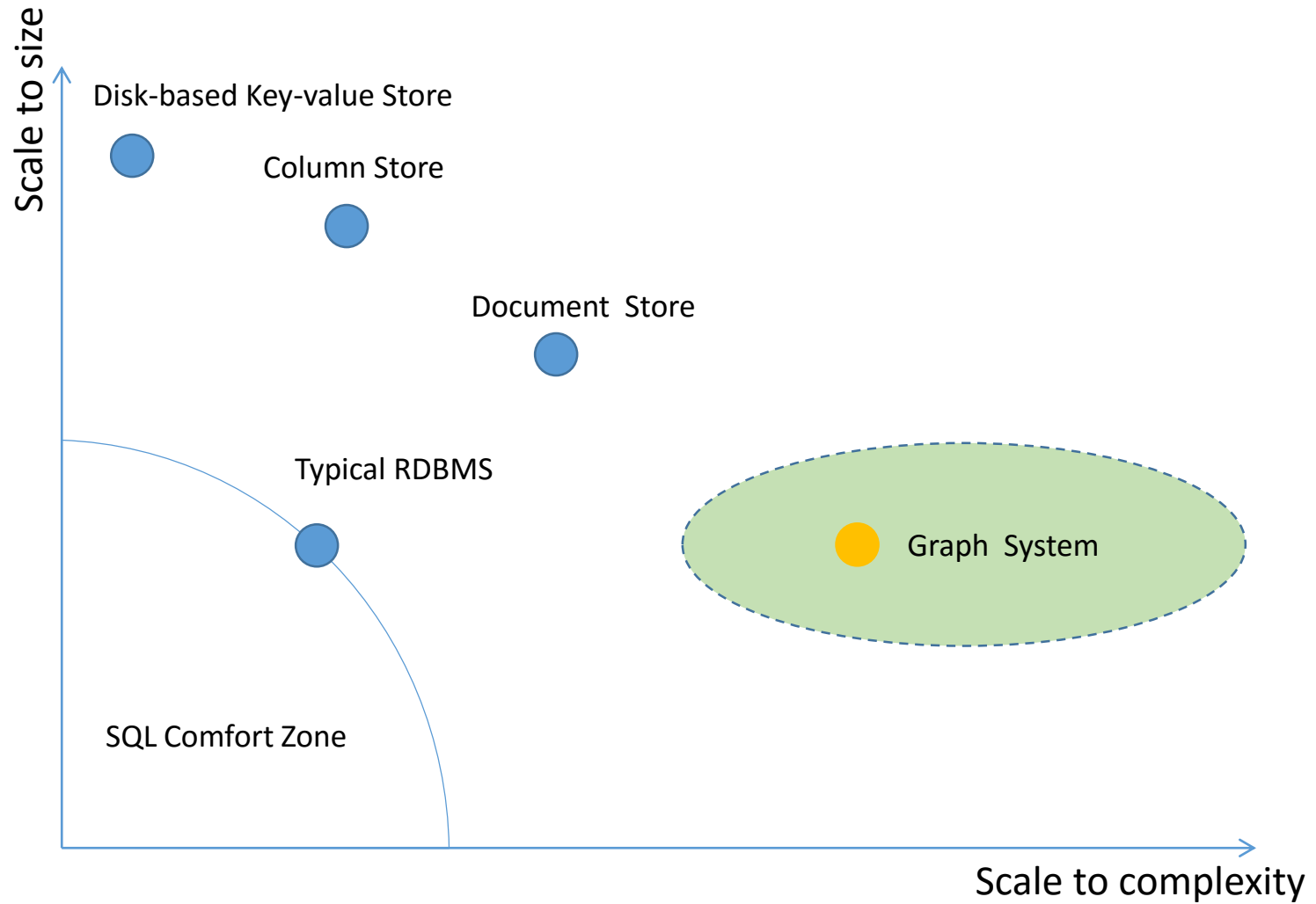
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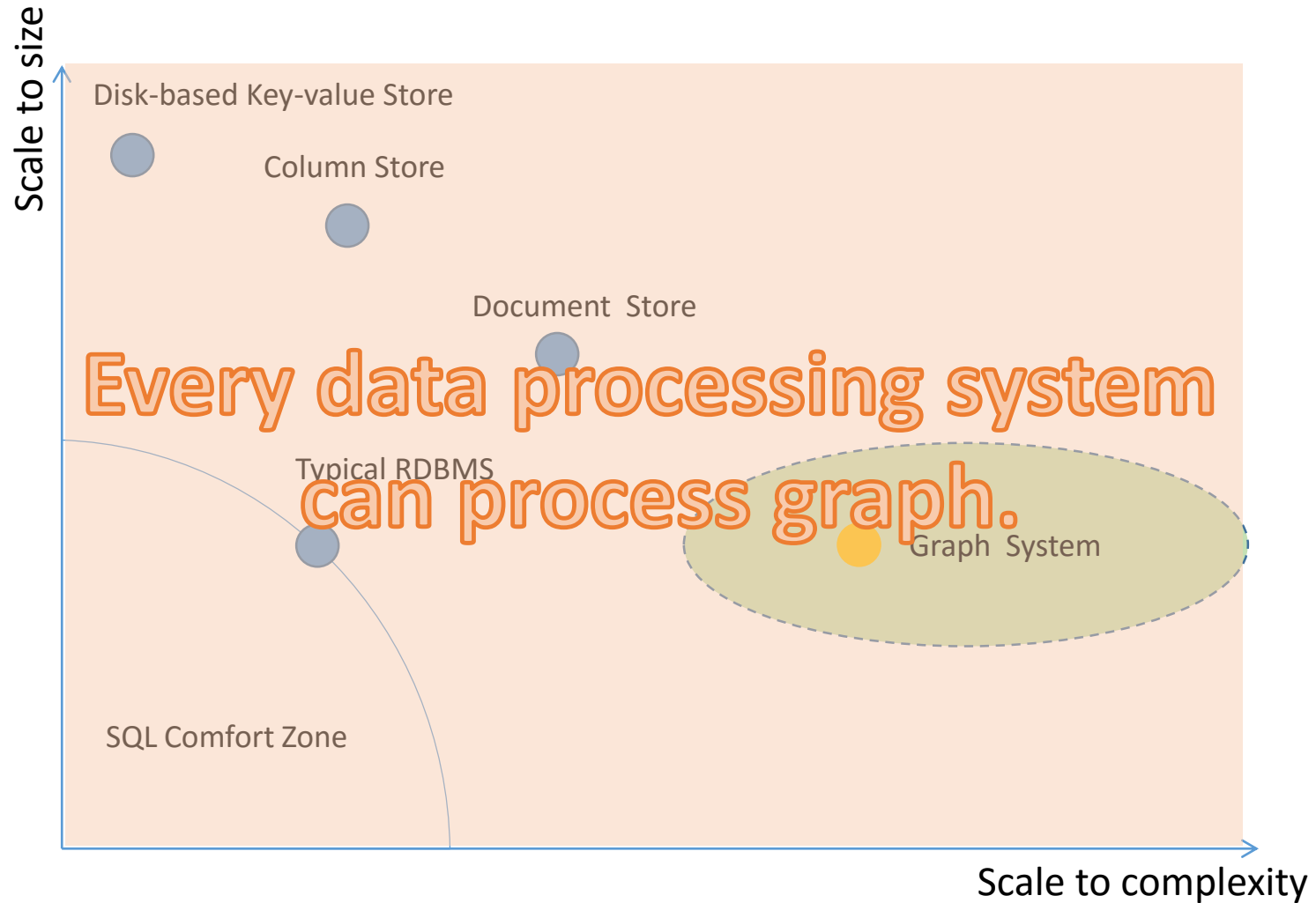
# The needs ultimately determine the design

- The first important rule: there is no one-size-fits-all system

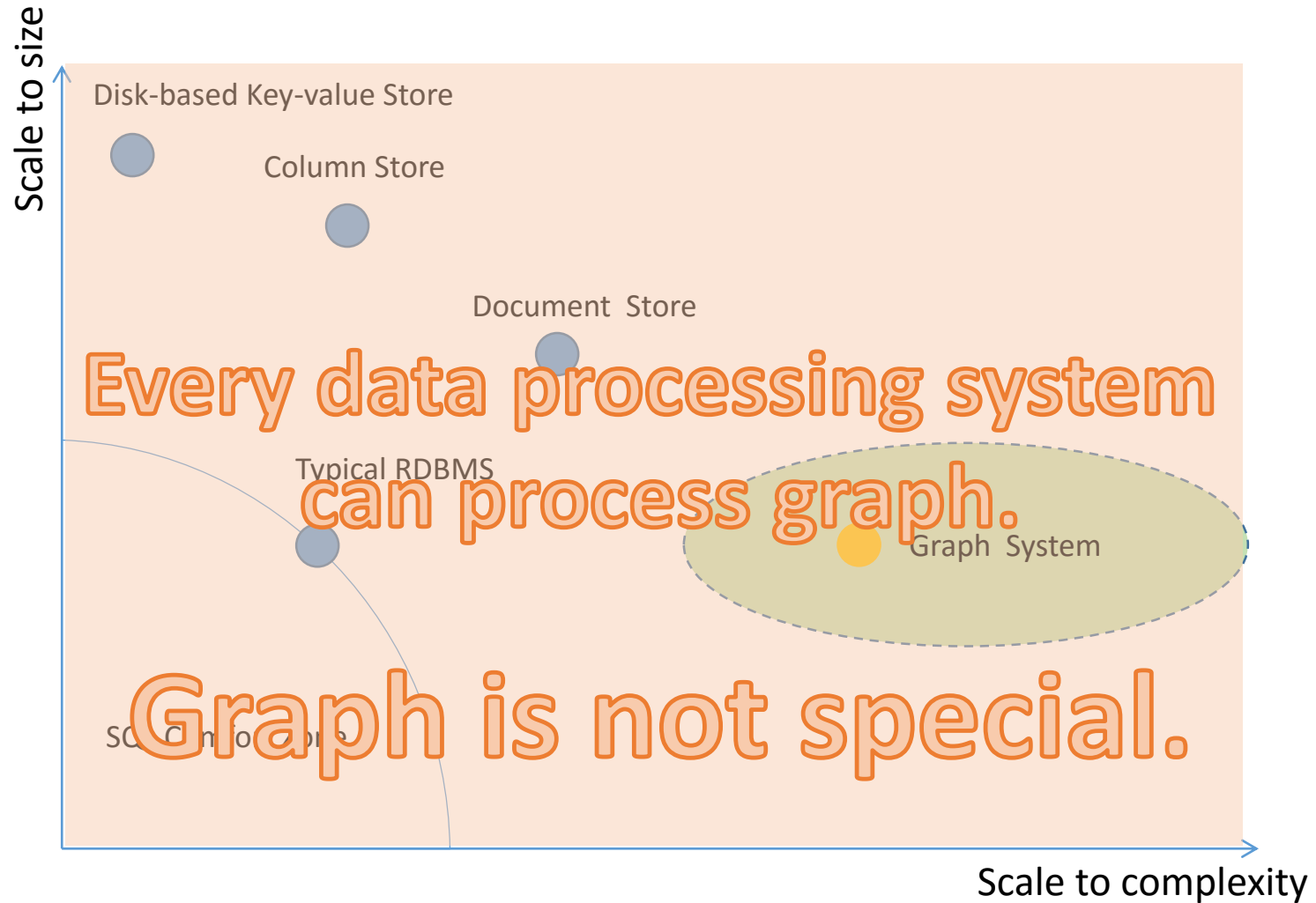
# First rule: no one-size-fits-all system



# First rule: no one-size-fits-all system



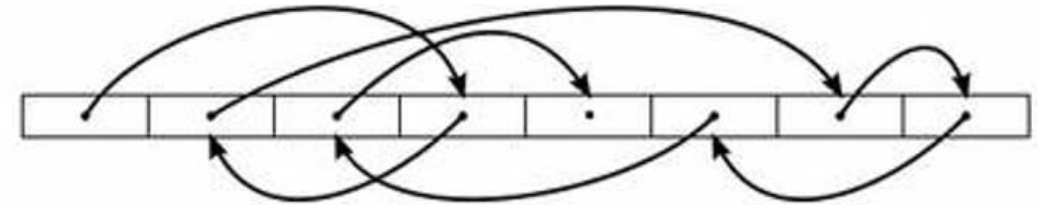
# First rule: no one-size-fits-all system





# Characteristics of parallel graph processing

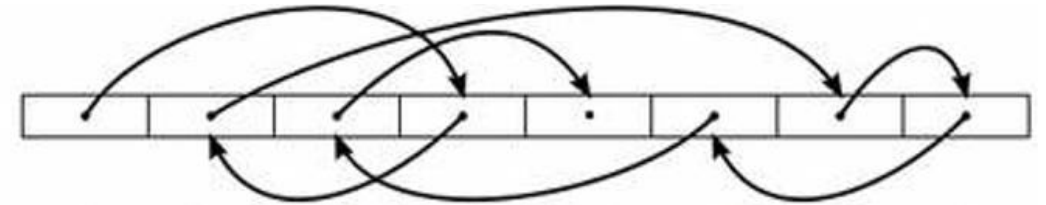
- Random access (Poor Locality)
  - For a node, its adjacent nodes cannot be accessed without “jumping” no matter how you represent a graph
  - Not cache-friendly, data reuse is hard



- Data is hard to partition
  - Difficult to extract parallelism by partitioning data
  - Hard to get an efficient “Divide and Conquer” solution
- Data driven
  - the structure of computations is not known a priori
- High data access to computation ratio

# Characteristics of parallel graph processing

- Random access (Poor Locality)
  - For a node, its adjacent nodes cannot be accessed without “jumping” no matter how you represent a graph
  - Not cache-friendly, data reuse is hard



- Data is hard to partition

• In this sense, graph is “special”.

- Data driven
  - the structure of computations is not known a priori
- High data access to computation ratio

# Design choices

- **First important rule: there is no one-size-fits-all system**
- Does this system support online queries, offline analytics, or both?
- Is the system optimized for response time, throughput, or both?
- Does the system scale, “out” or “up”?
- Does the system need transaction support?

# Online queries vs. offline analytics

- Online query processing is usually optimized for response time
- Offline analytics is usually optimized for throughput
- Compared with offline analytics, online queries are usually harder to optimize
  - Online queries are sensitive to latency
  - The data access patterns of a graph query are difficult to predict

# Online queries vs. offline analytics

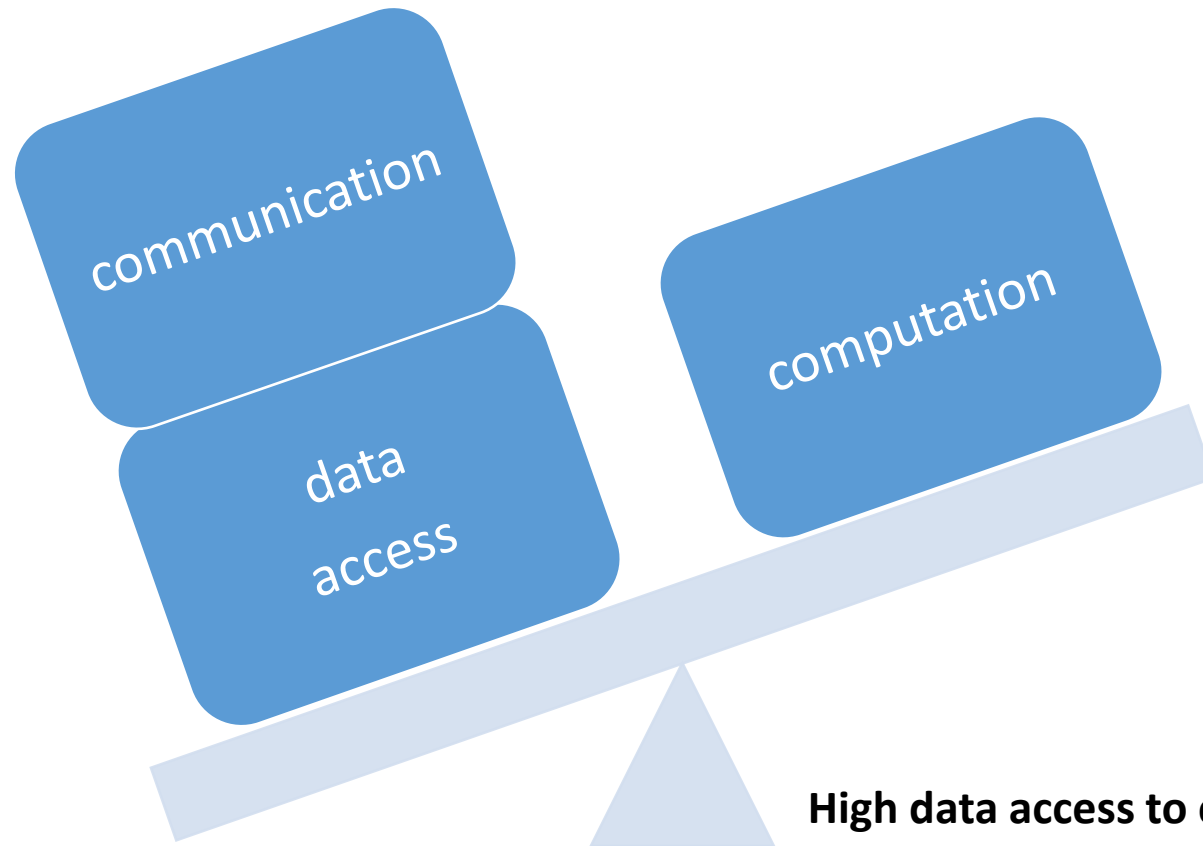
## Online Query Processing

- ★ • Random access
- ★ • Data is hard to partition
- ★ • Data driven
- ★ • High data access to computation ratio

## Offline Analytics

- ★ • Data is hard to partition
- ★ • High data access to computation ratio

Query response time:  
data access + communication + computation



**High data access to computation ratio**

# System design choice

- Main storage (storage backend)
- Index
- Communication paradigm: two-sided vs. one-sided
- Scale out or scale up
- ACID Transactions or not

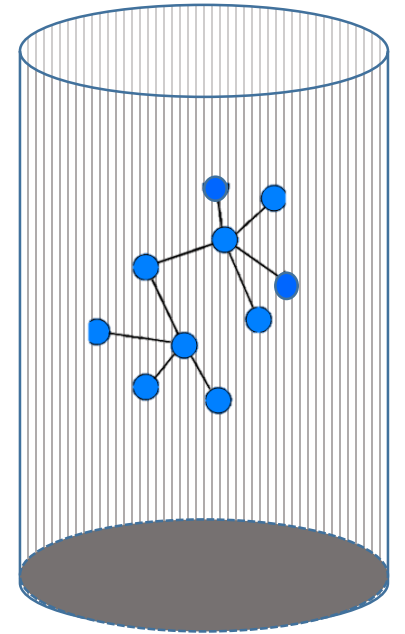
# System design choice

- **Main storage (storage backend)**
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# Graph may be in the jail of storage

- We can use many existing data management systems to process graph
- Many existing systems are mature, but not for graph
  - RDBMS, MapReduce
  - The commonest graph operation “traversal” incurs excessive amount of joins



Graph in the Jail of the storage

# Traverse graph using joins in RDBMS

ID	name	...	src	dst
1	N1	...	1	3
2	N2	...	2	4
3	N3	...	2	1
4	N4	...	4	3
5	N5	...	1	5
6	N6	...	1	6
...	...	...	...	...

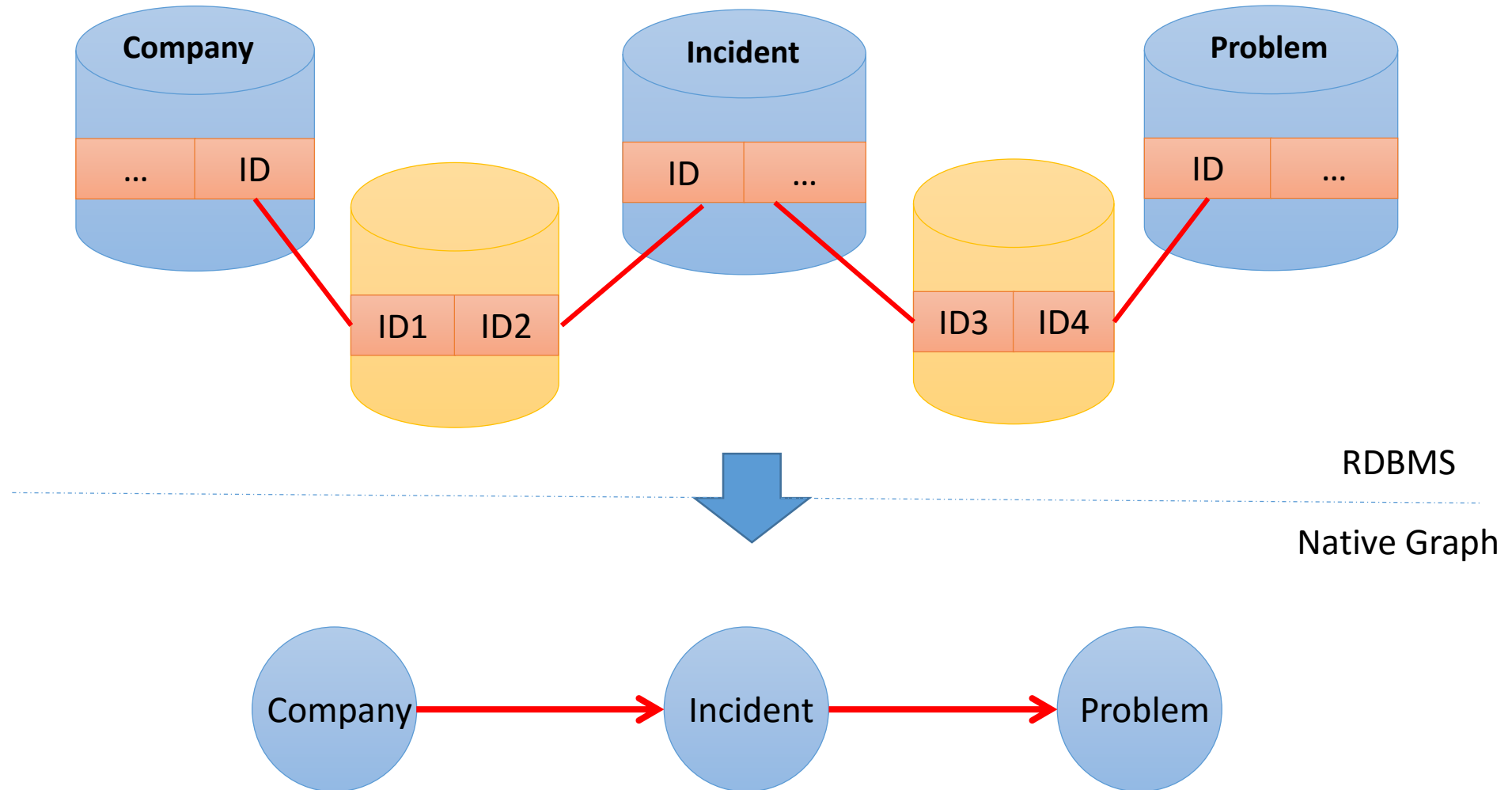
Node Table: N

Edge Table: E

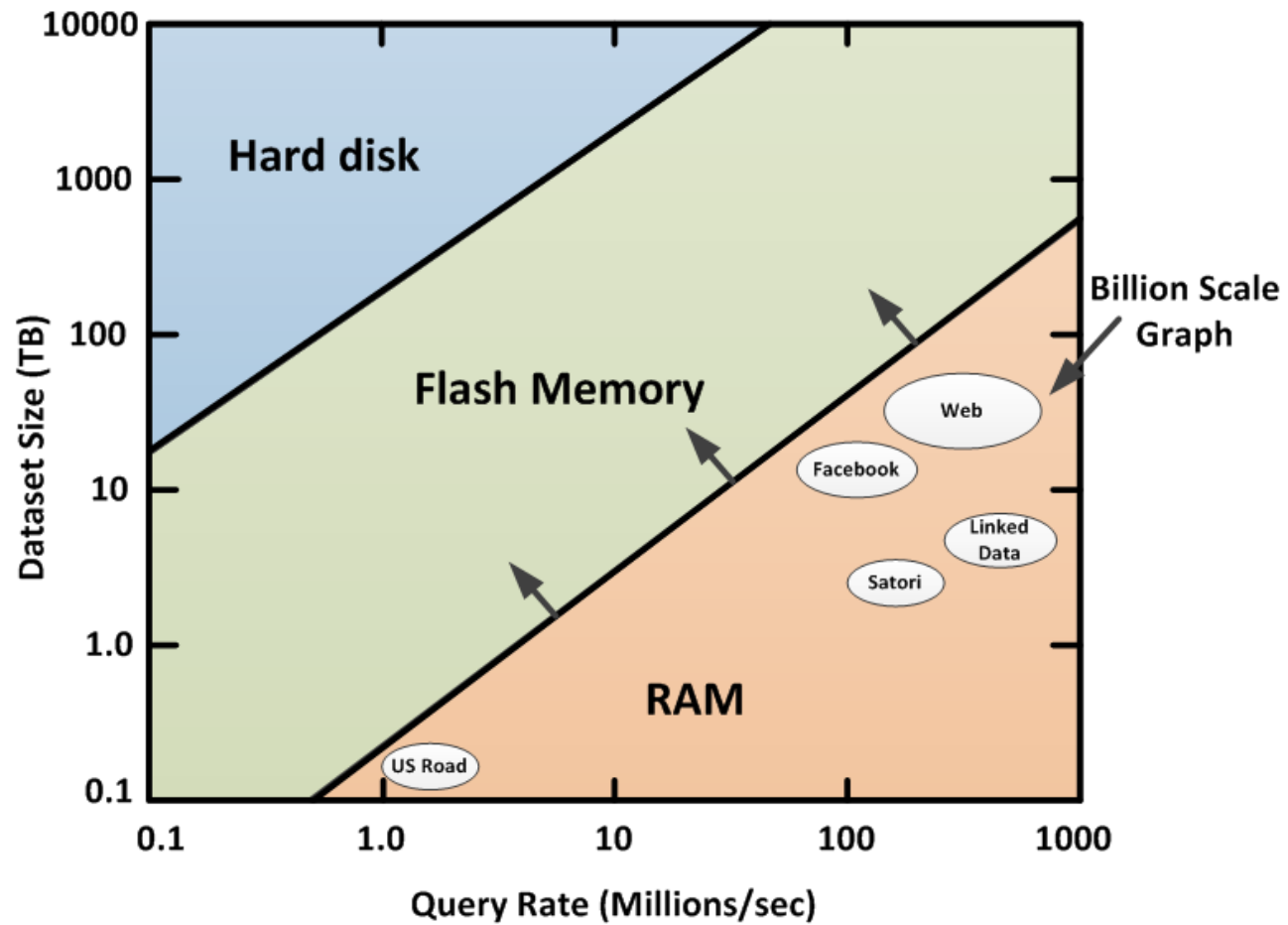
Get neighbors of N1

```
SELECT*  
FROM N  
LEFT JOIN E ON N.ID = E.dst  
WHERE E.src = 1;
```

# Multi-way Join vs. graph traversal



# Total cost of ownership



Reproduced from Anderson's SOSP 2009 paper

# Trend in cost of RAM

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	Today	In 5-10 years
<b># servers</b>	<b>1000</b>	<b>1000</b>
<b>GB/server</b>	<b>64GB</b>	<b>1024GB</b>
<b>Total capacity</b>	<b>64TB</b>	<b>1PB</b>
<b>Total server cost</b>	<b>\$4M</b>	<b>\$4M</b>
<b>\$/GB</b>	<b>\$60</b>	<b>\$4</b>

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# System design choice

- Main storage (storage backend)
- **Index**
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# Index

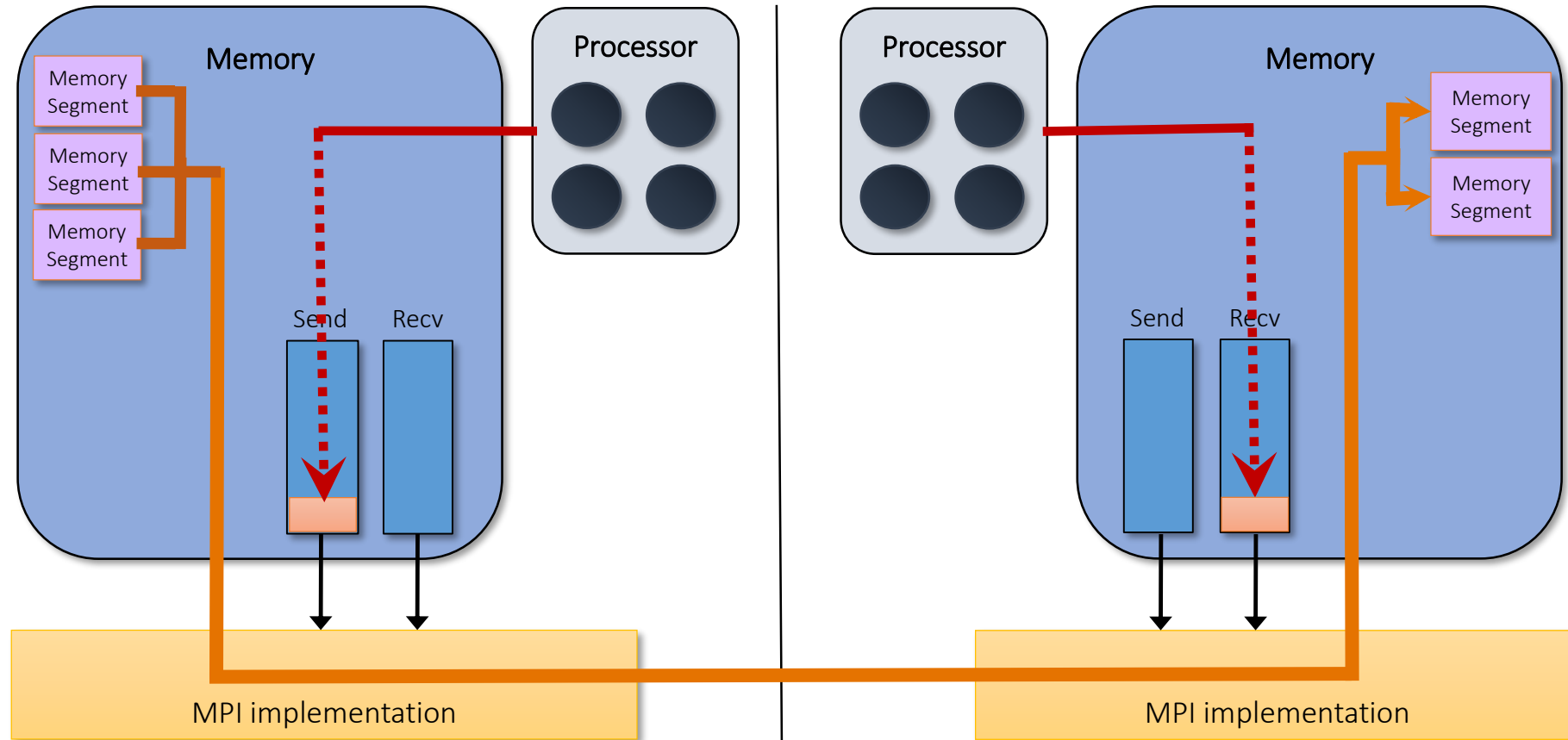
- It is costly to index graph structures, use it wisely.
- We will get back to this later ...

# System design choice

- Main storage (storage backend)
- Index
- **Communication paradigm: two-sided vs. one-sided**
- Scale out or scale up
- ACID Transactions or not



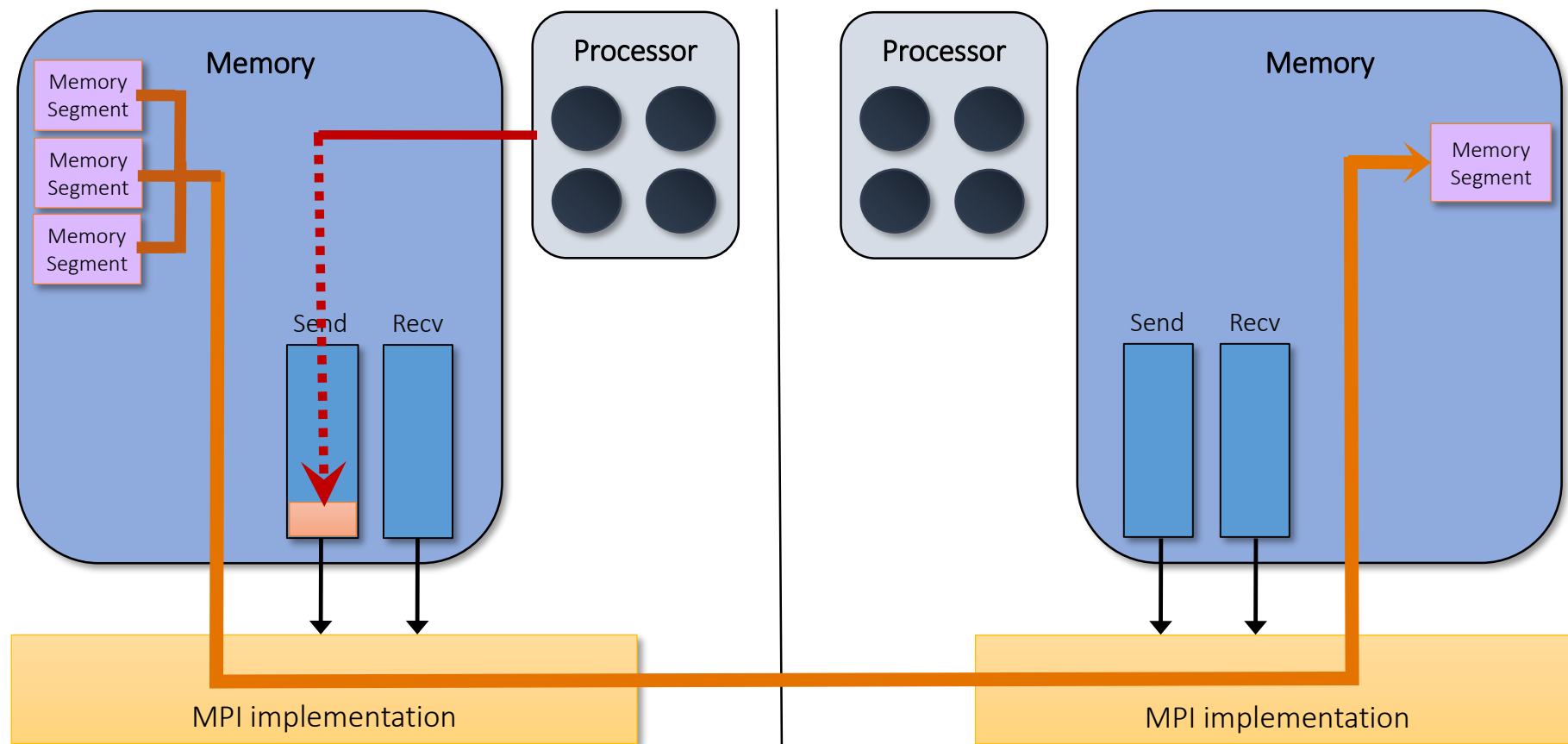
# Communication paradigm: two-sided vs. one-sided



Two-sided communication

Adapted from: Advanced parallel programming with MPI (Balaji et al)

# Communication paradigm: two-sided vs. one-sided



One-sided communication

# System design choice

- Main storage (storage backend)
- Index
- Communication paradigm: two-sided vs. one-sided
- **Scale out or scale up**
- ACID Transactions or not

# Design choice: scale-up vs. scale-out

- Supercomputer model
  - Programming model simple and efficient
    - shared memory address space
  - Expensive and not common
  - Hardware is your ultimate limit
- Distributed cluster model
  - Programming model is complex
    - Message passing and synchronization is more complex
  - Relatively cheaper and can make use of commodity pc
  - More flexible to meet various needs

Scale “OUT”, not “UP”

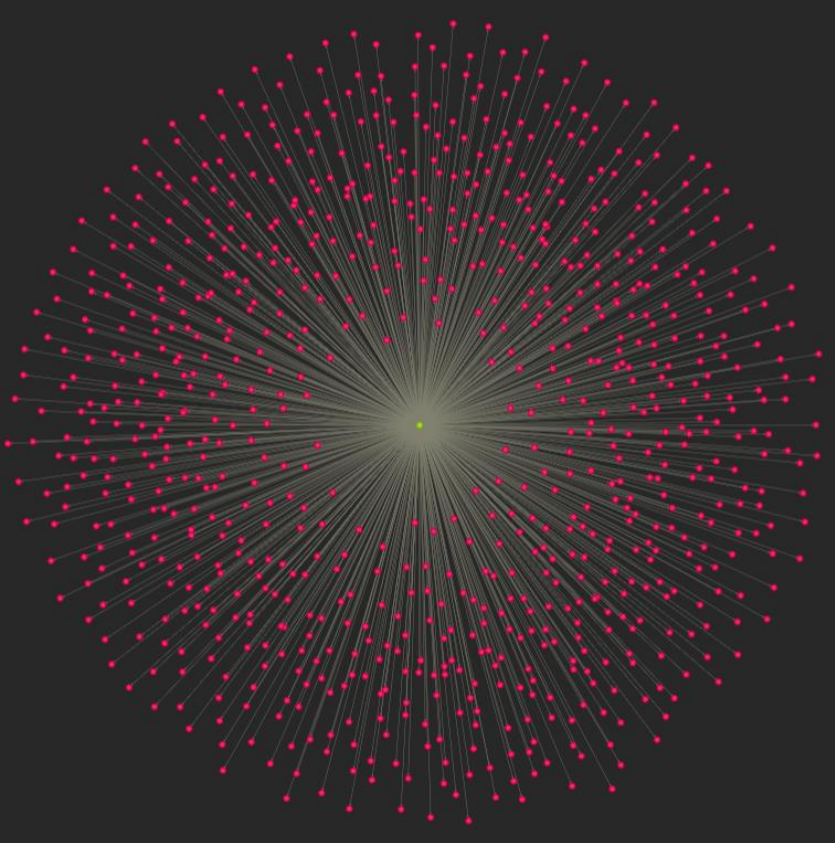
# System design choice

- Main storage (storage backend)
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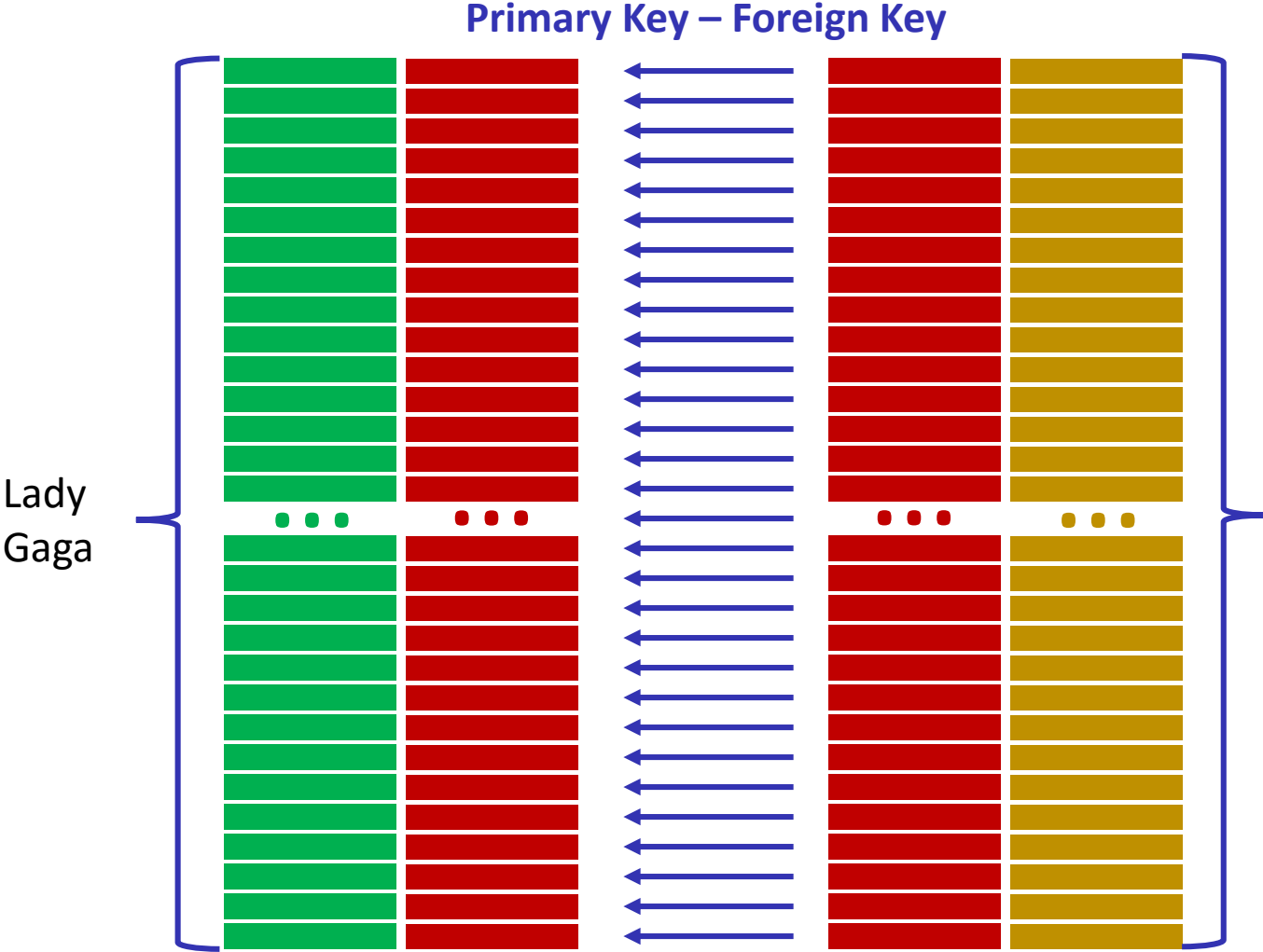
# Think twice before diving into transactions

- Pros
  - Strong data consistency guarantee
- Cons
  - The hell of referential integrity
  - The disaster of cascading rollback
  - Multi-round network communications per commit for distributed transactions

# The hell of referential integrity

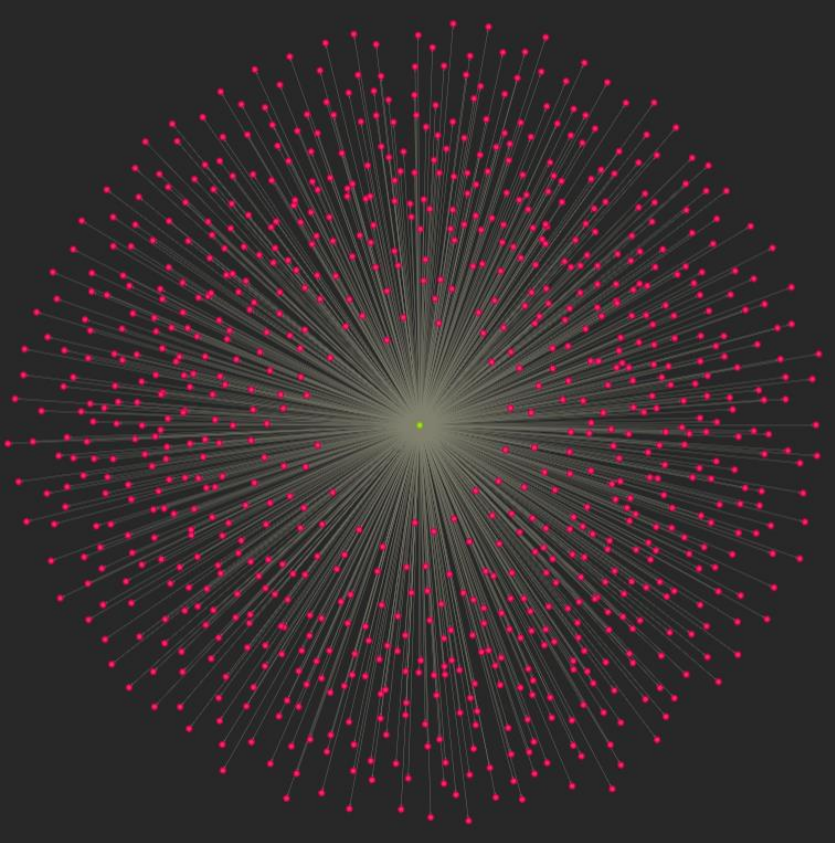


Lady Gaga in Freebase

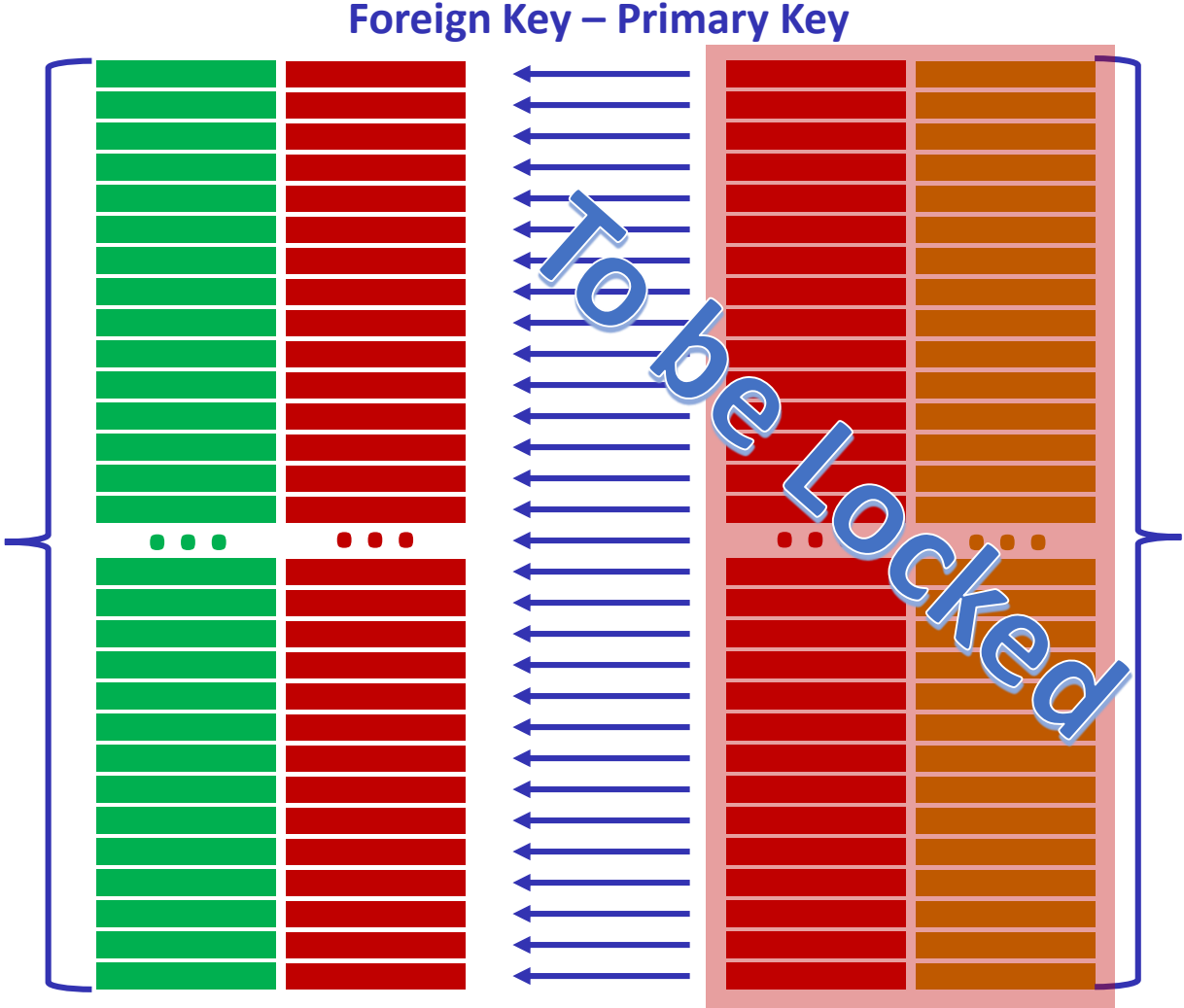




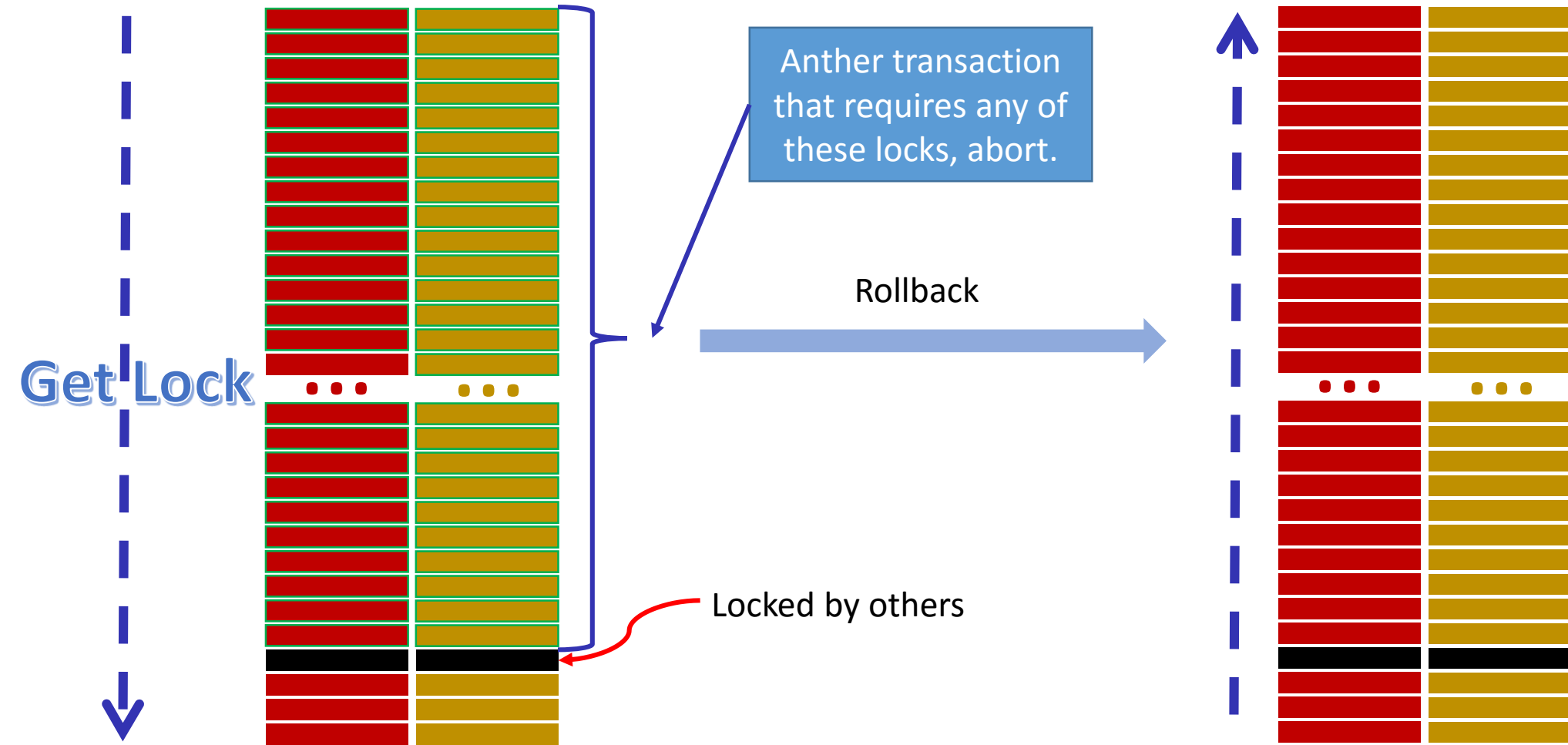
# The hell of referential integrity



Lady Gaga



# The disaster of cascading rollback



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- Online query processing
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MapReduce

# MapReduce

- High latency, yet high throughput general purpose data processing platform
- Optimized for offline analytics on large data partitioned on hundreds of machines

# Processing graph using MapReduce

- No online query support
- The data model of map reduce cannot describe graph natively
  - Graph algorithms cannot be expressed intuitively
- Inefficiency for graph processing
  - Intermediate results of each iteration need to be materialized
  - Entire graph structure need to be sent over network iteration after iteration, this incurs huge unnecessary data movement

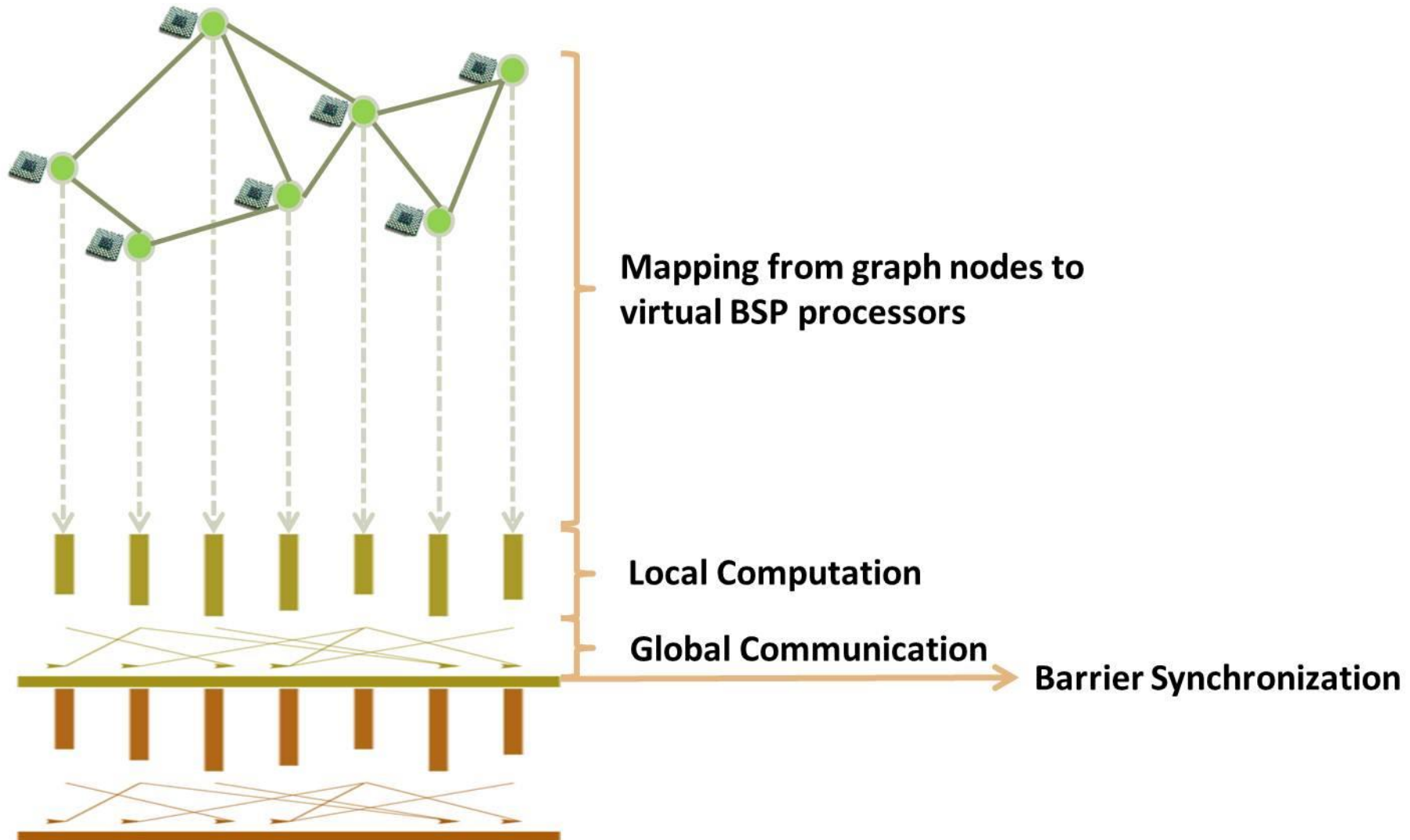
# MapReduce

- De facto of distributed large data processing
- Great scalability: supports extremely large data, but unfortunately not for graph

# Vertex-centric graph computation



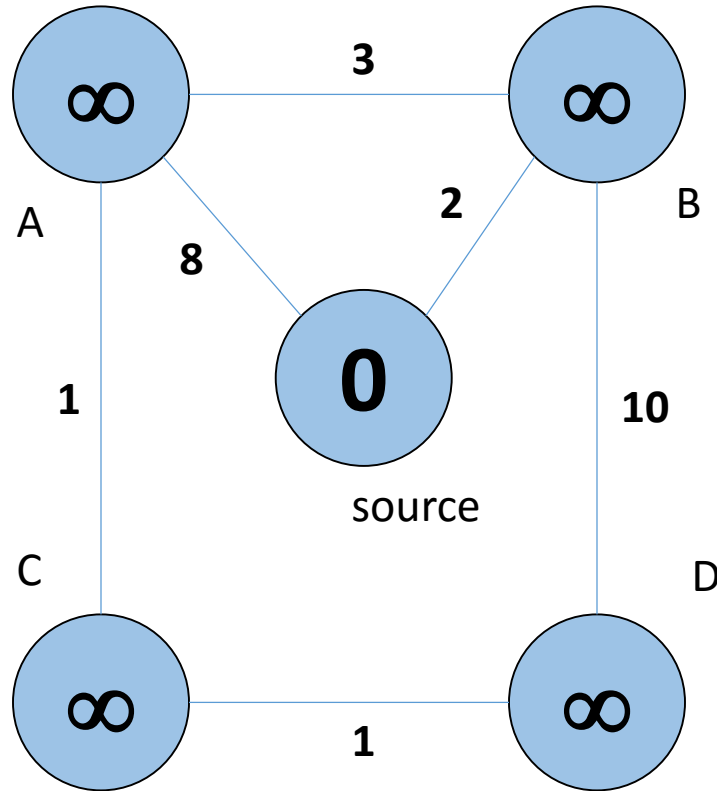
# Basic idea: think like a vertex!



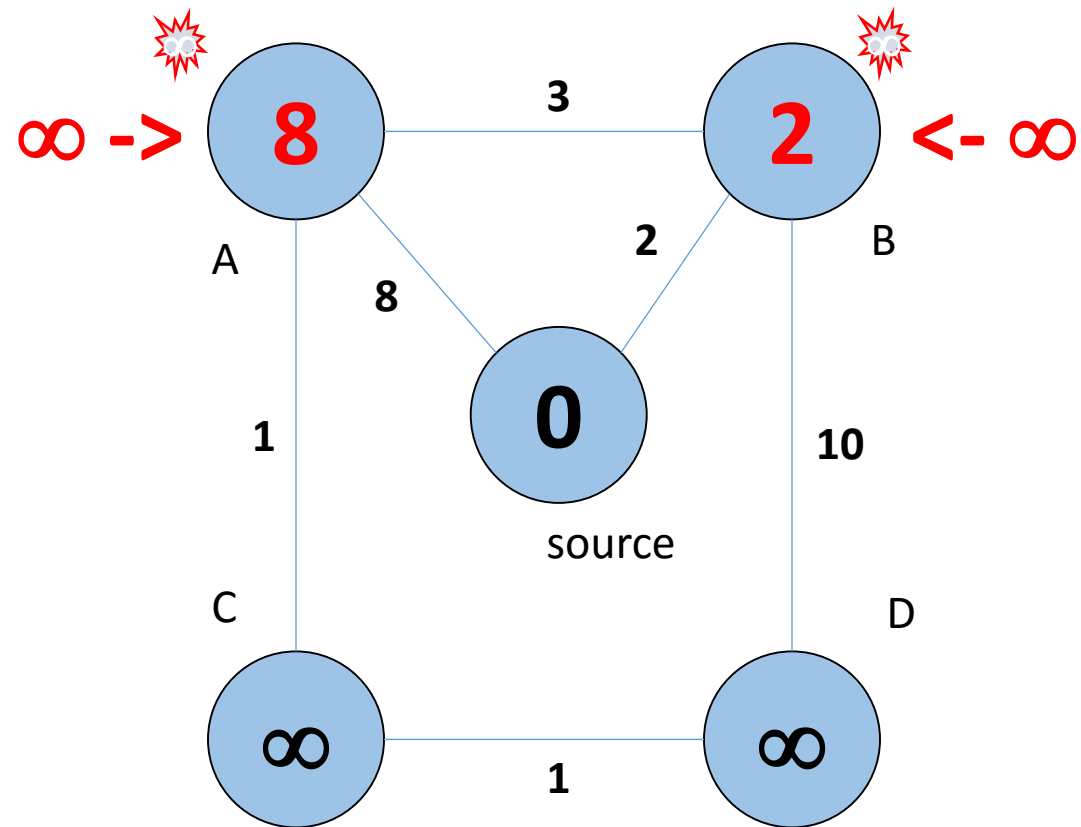
# Computation model

- Graph computation is modeled as many supersteps
- Each vertex reads messages sent in previous superstep
- Each vertex performs computation in parallel
- Each vertex can send messages to other vertices in the end of an iteration

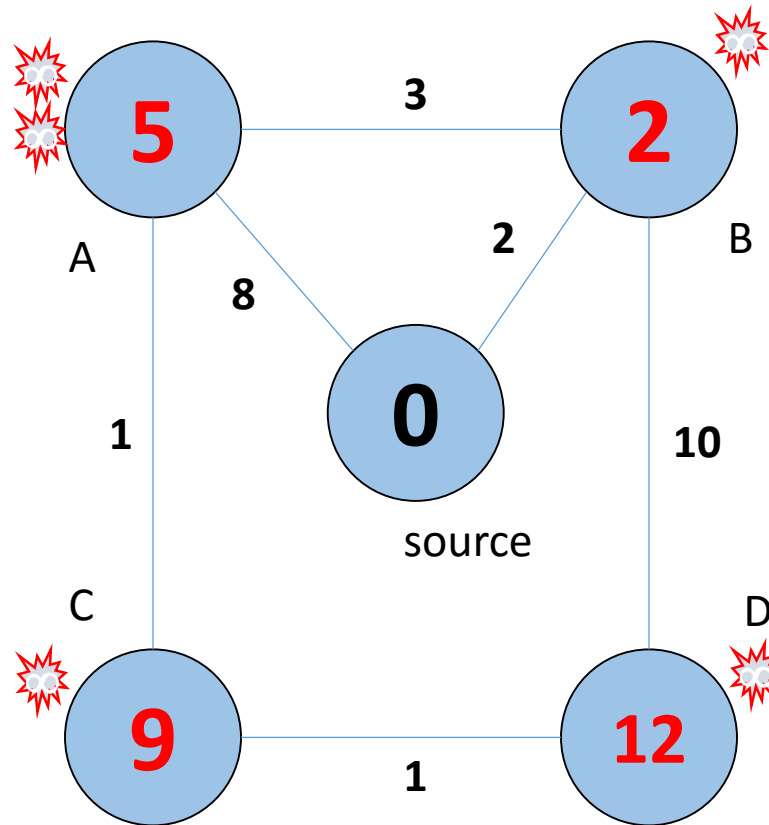
# Example: SSSP in Pregel



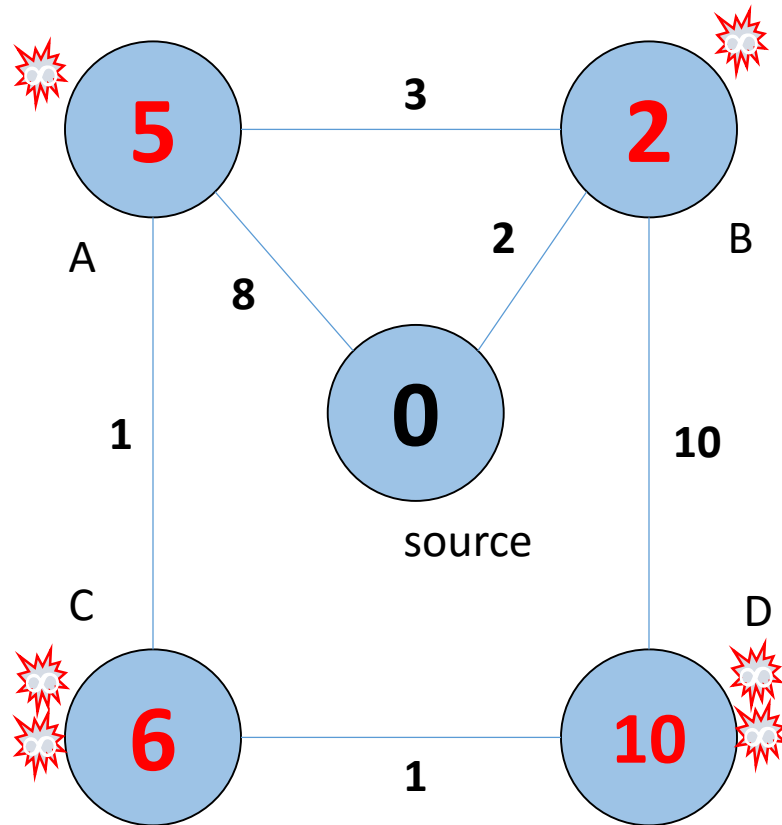
# Example: SSSP in Pregel



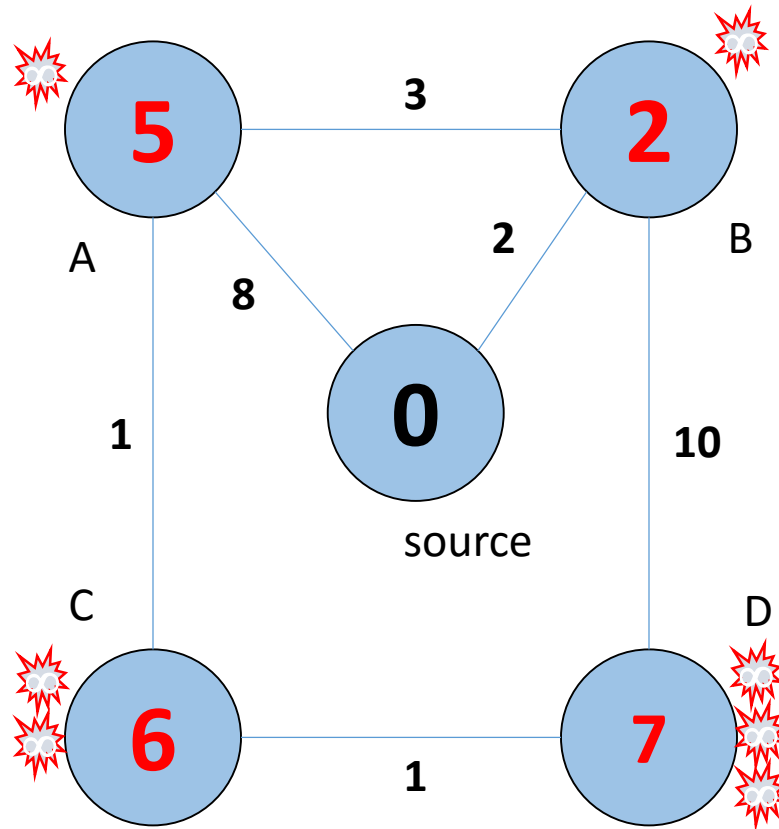
# Example: SSSP in Pregel



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# Example: SSSP in Pregel



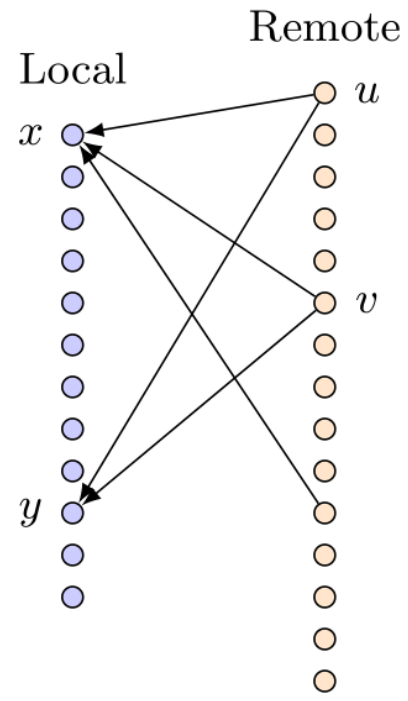
# Pregel vs. MapReduce

- Exploits fine-grained parallelism at node level
- Pregel doesn't move graph partitions over network, only messages among nodes are passed at the end of each iteration
- Many graph algorithms cannot be expressed using vertex-centric computation model intuitively and elegantly

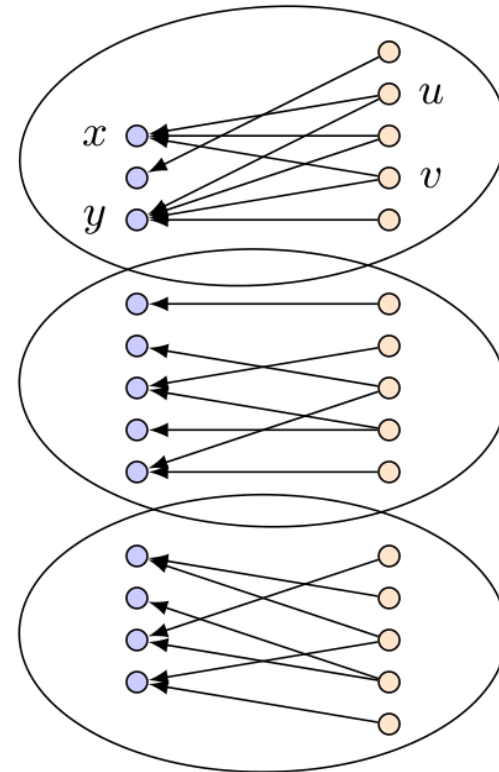


# Communication optimization

# Bipartite view of a graph on a local machine

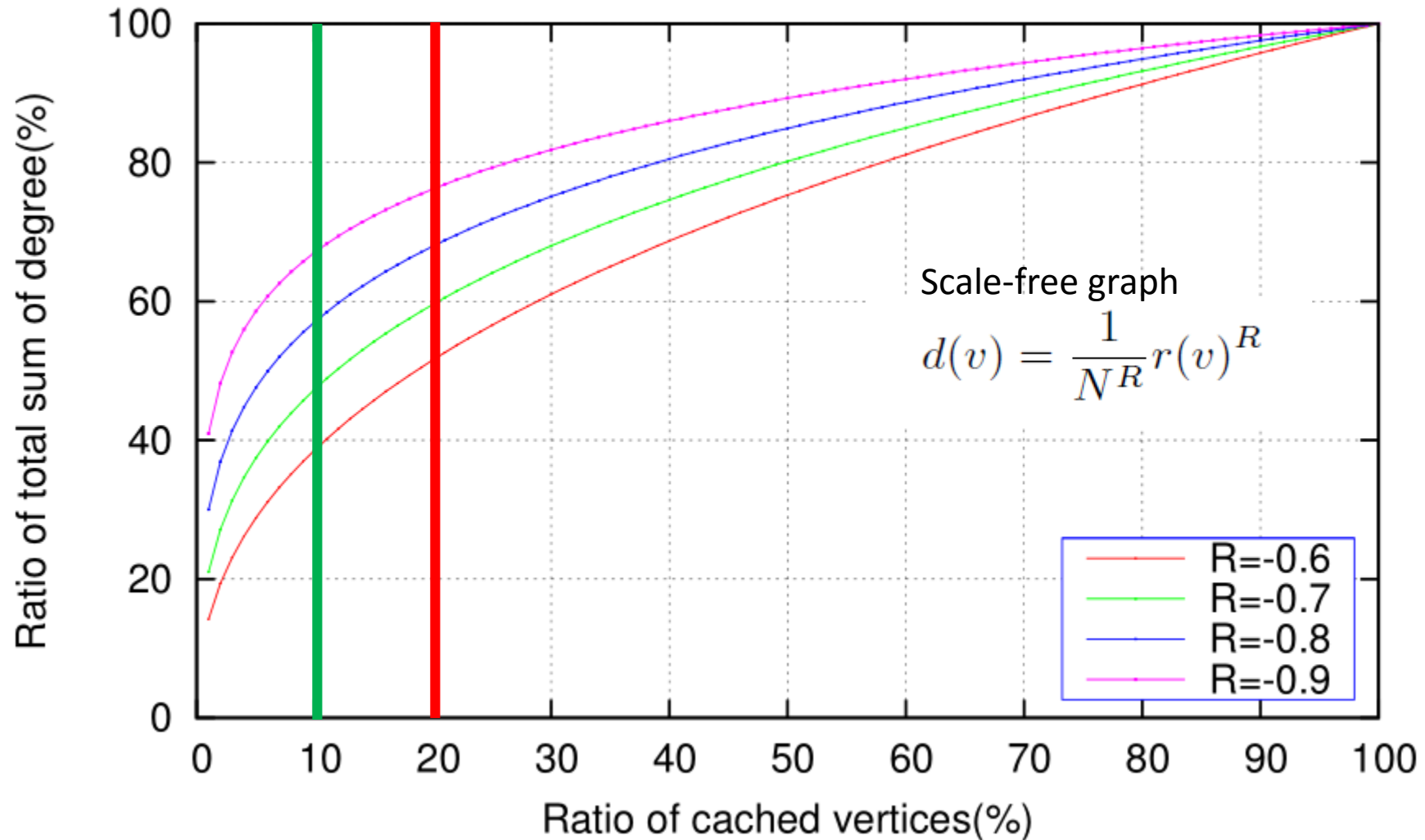


a)



b)

# Message cache (“80/20” rule in real graphs)



# Outline

- Graph processing scenarios
- Challenges of large graph processing
- General design principles
- Offline analytics
- **Online query processing**
- Case study
- Graph generation
- Other graph representations and their applications

# Online query processing

- Where latencies come from and asynchronous fan-out search
- Index-free query processing

# Online query processing

- Where latencies come from and asynchronous fan-out search
- Index-free query processing

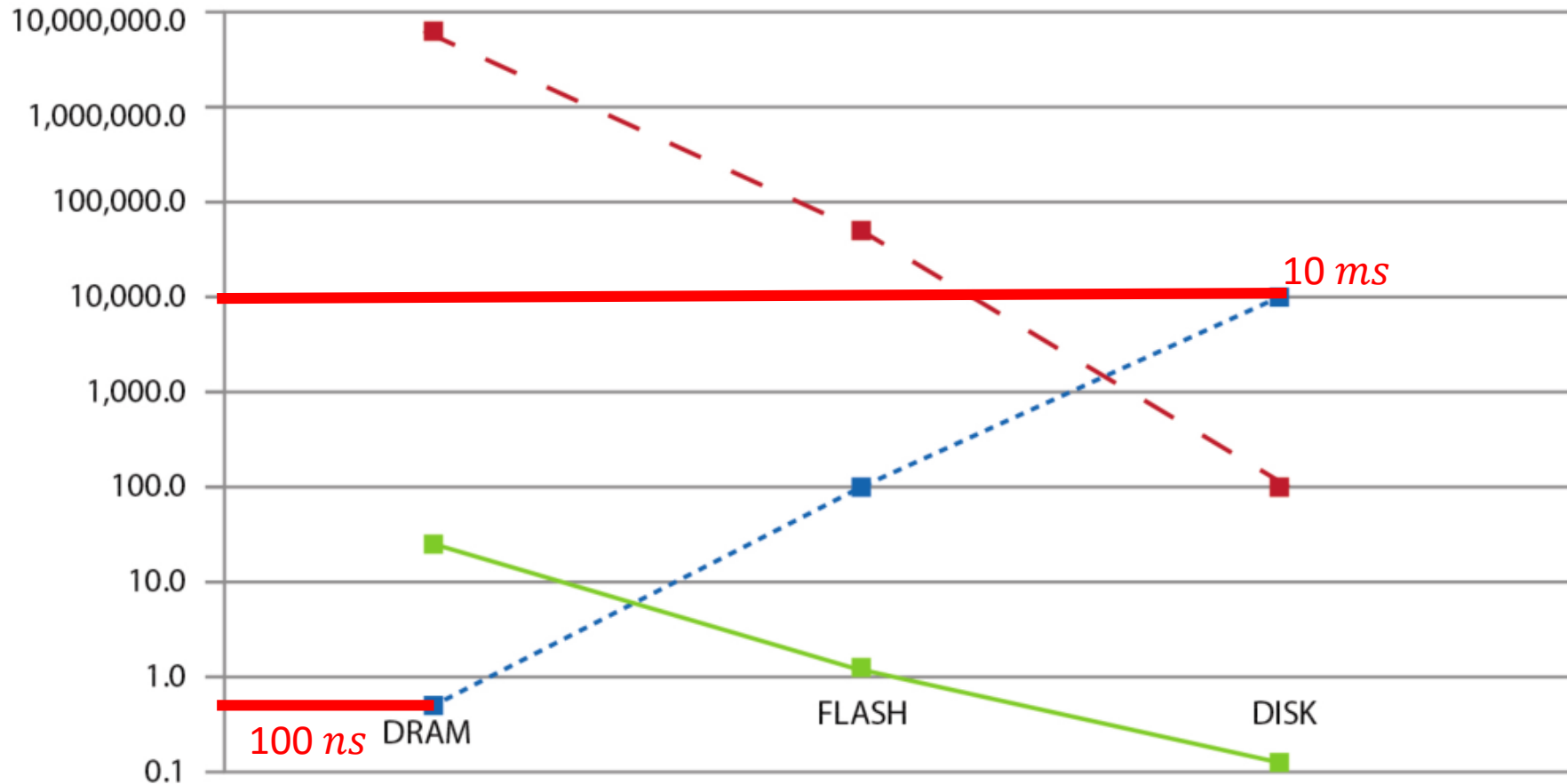
# People search challenge in Facebook graph

- Among adult Facebook users, the average number of friends is 338.

$$\begin{aligned} & 338 \\ & +338 \times 338 \\ & +338 \times 338 \times 338 \\ & =\mathbf{38,729,054} \end{aligned}$$

Can we search a person in one's 3-hop neighborhood within 500 ms?

# Latency, Bandwidth, and Capacity



Latency (us)    - - - - -  
Ops/sec        - - - - -  
\$/GB           - - - - -



# Disk-based approach

$$\begin{aligned} & 338 \\ & + 338 \times 338 \\ & + 338 \times 338 \times 338 \\ & = 38,729,054 \end{aligned} \quad \longrightarrow \quad \begin{aligned} & 387,290,540 \text{ ms} \\ & = 4.5 \text{ days} \end{aligned}$$

each disk seek + read: > 10 ms

# RAM-based approach

- DRAM latency: 100 ns

10 million reads/writes per second

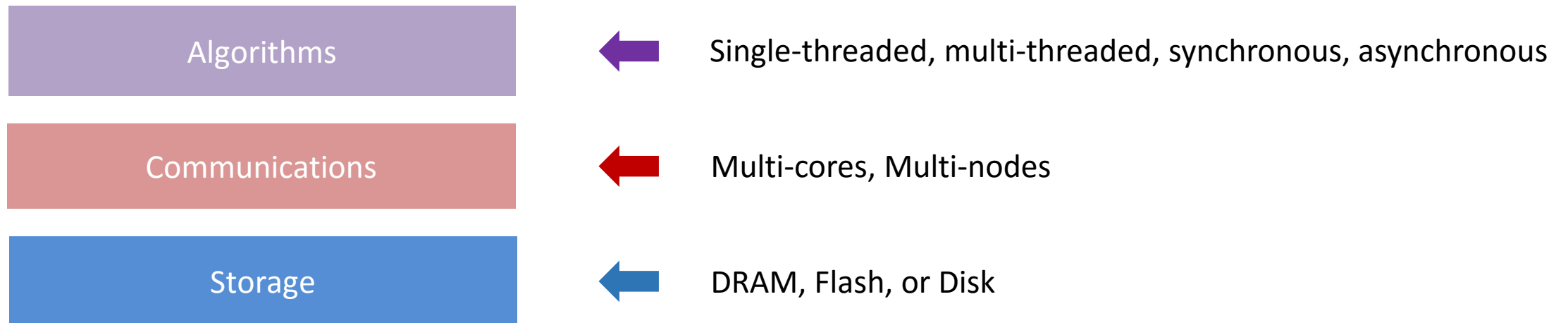
1 million node-level read/write per second

**38,729,054 nodes to access, it takes at least 38 seconds.**

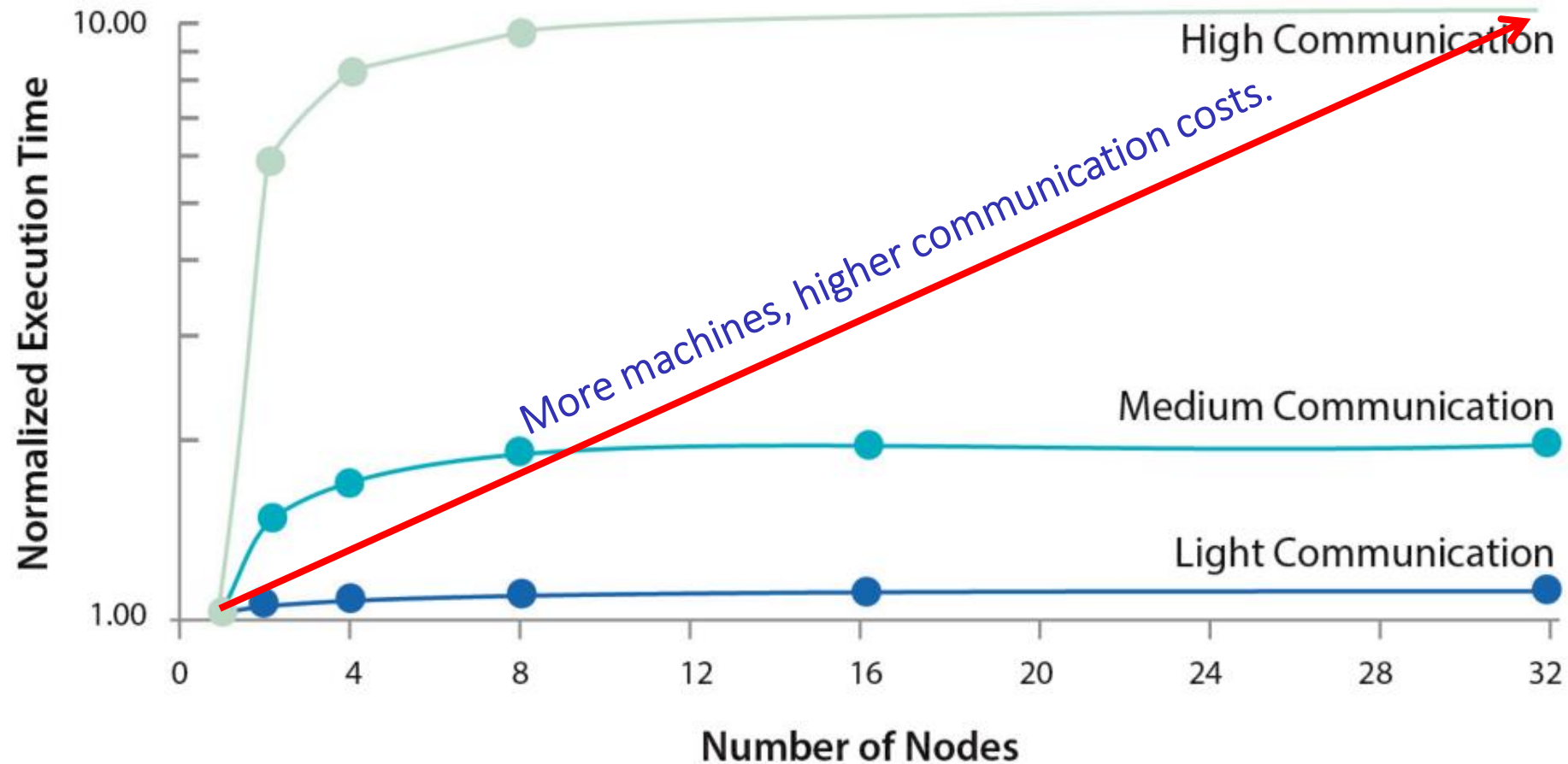
Hmm, no parallel data accesses yet!

How much time can we reduce with parallel data accesses?

# Where do latencies come from?



# Move computation, instead of data!



If you care about latency, do not use the shared-memory model in a distributed setting.

# Lessons learned so far (how to reduce latencies)

- RAM (Hardware sometimes does matter a lot)
  - The stupid buy faster computers, smart ones write better programs?
- Avoid moving data
- .....

# Lessons learned so far (how to reduce latencies)

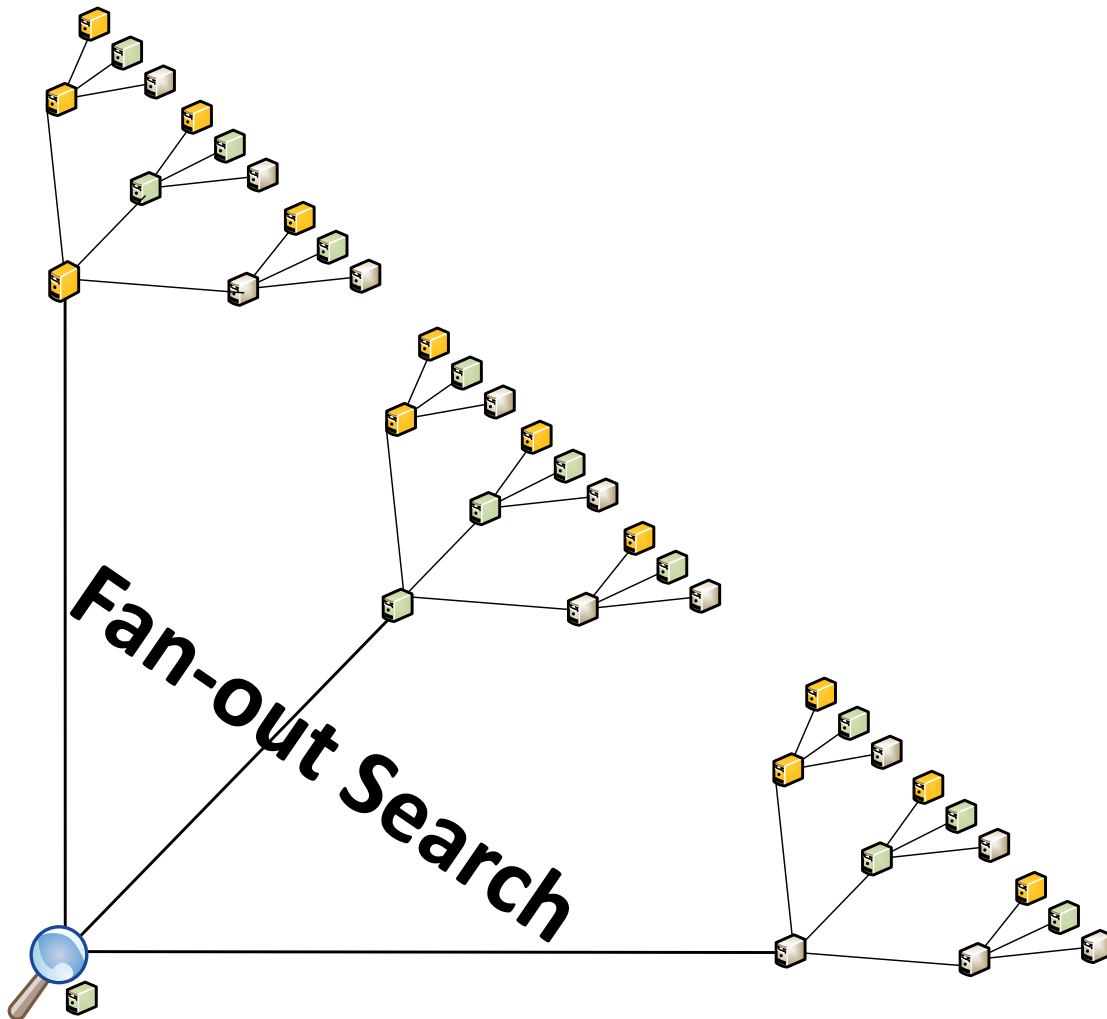
- RAM (Hardware sometimes does matter a lot)
  - The stupid buy faster computers, smart ones write better programs?
- Avoid moving data
- Avoid unnecessary synchronizations



**Makes programming harder**



# Asynchronous fan-out search



Hop	Msg #	Node # per machine
1	$n$	$\frac{d}{n}$
2	$n^2$	$\frac{d^2}{n}$
3	$n^3$	$\frac{d^3}{n}$

$n$  is the server count  
 $d$  is the average degree



MORGAN & CLAYPOOL PUBLISHERS

# The Datacenter as a Computer

*An Introduction to the Design  
of Warehouse-Scale Machines  
Second Edition*

**Luiz André Barroso**  
**Jimmy Clidaras**  
**Urs Hölzle**

***SYNTHESIS LECTURES ON  
COMPUTER ARCHITECTURE***

Mark D. Hill, *Series Editor*

# Online query processing

- Where latencies come from and fan-out search
- Index-free query processing

# Online query example: subgraph matching

Procedure:

1. Break a graph into basic units (edges, paths, frequent subgraphs, ...)
2. Build index for every possible basic unit
3. Decompose a query into multiple basic unit queries, and join the results.

# Query Index Examples

Algorithms	Index Size	Index Time	Update Cost
Ullmann [Ullmann76], VF2 [CordellaFSV04]	-	-	-
RDF-3X [NeumannW10]	$O(m)$	$O(m)$	$O(d)$
BitMat [AtreCZH10]	$O(m)$	$O(m)$	$O(m)$
Subdue [HolderCD94]	-	<b>Exponential</b>	$O(m)$
SpiderMine [ZhuQLYHY11]	-	<b>Exponential</b>	$O(m)$
R-Join [ChengYDYW08]	$O(nm^{1/2})$	$O(n^4)$	$O(n)$
Distance-Join [ZouCO09]	$O(nm^{1/2})$	$O(n^4)$	$O(n)$
GraphQL [HeS08]	$O(m + nd^r)$	$O(m + nd^r)$	$O(d^r)$
Zhao [ZhaoH10]	$O(nd^r)$	$O(nd^r)$	$O(d^L)$
GADDI [ZhangLY09]	$O(nd^L)$	$O(nd^L)$	$O(d^L)$

Index-based subgraph matching [Sun VLDB 2012]

# Query Index Examples

Algorithms	Index Size for Facebook	Index Time for Facebook	Query Time on Facebook (s)
Ullmann [Ullmann76], VF2 [CordellaFSV04]	-	-	>1000
RDF-3X [NeumannW10]	1T	>20 days	>48
BitMat [AtreCZH10]	2.4T	>20 days	>269
Subdue [HolderCD94]	-	> 67 years	-
SpiderMine [ZhuQLYHY11]	-	> 3 years	-
R-Join [ChengYDYW08]	>175T	> $10^{15}$ years	>200
Distance-Join [ZouCO09]	>175T	> $10^{15}$ years	>4000
GraphQL [HeS08]	>13T( $r=2$ )	> 600 years	>2000
Zhao [ZhaoH10]	>12T( $r=2$ )	> 600 years	>600
GADDI [ZhangLY09]	> $2 \times 10^5$ T ( $L=4$ )	> $4 \times 10^5$ years	>400

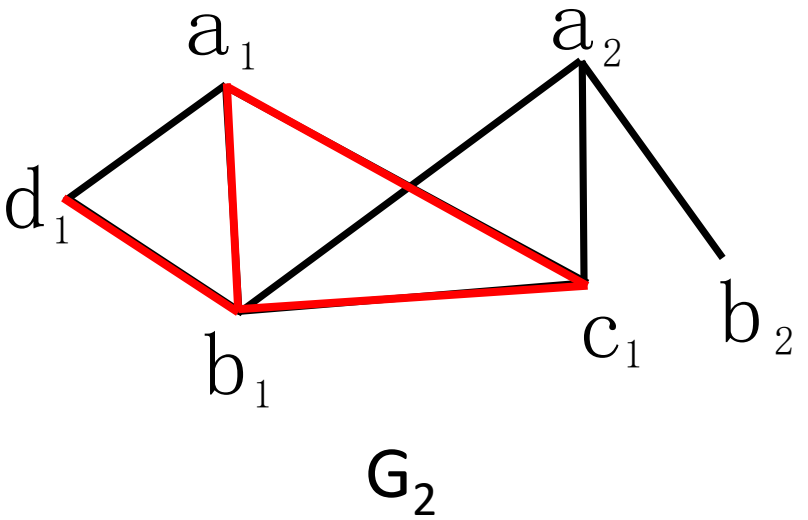
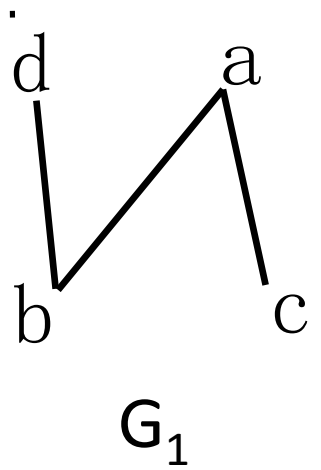
Index-based subgraph matching [Sun VLDB 2012]

# Case study: distributed subgraph matching

Procedure:

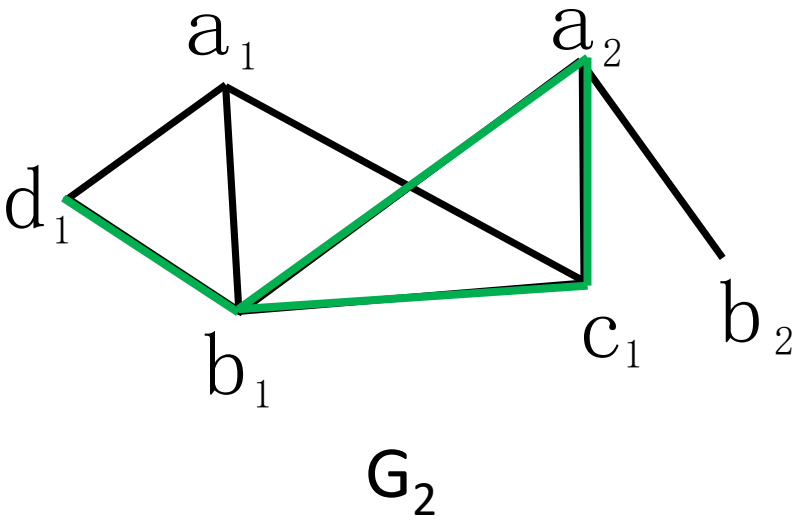
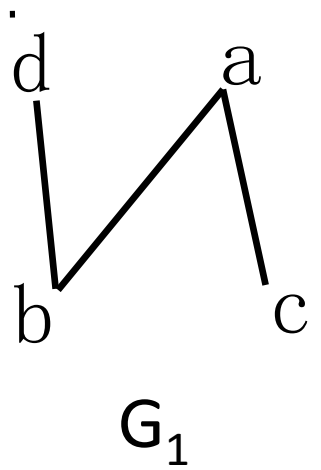
1. Break a query into basic units
- 2. Match the basic units in parallel on the fly**
3. Join the results

# Subgraph matching

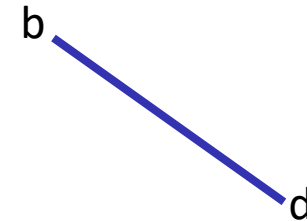
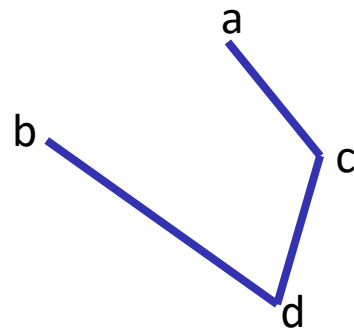
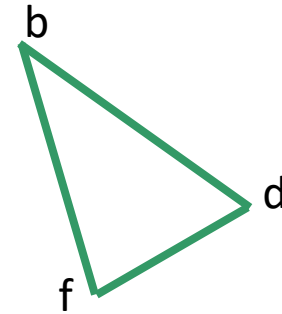
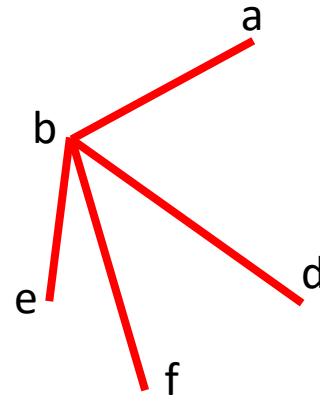
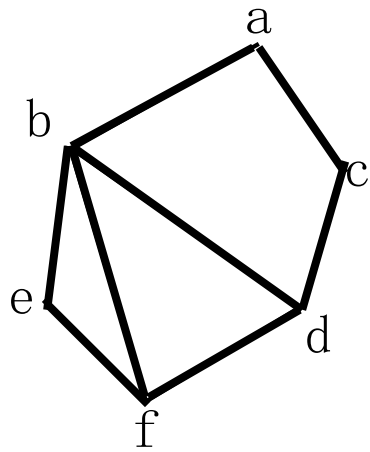




# Subgraph matching

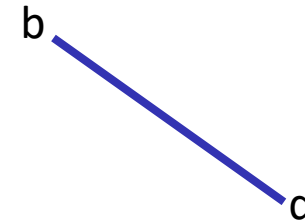
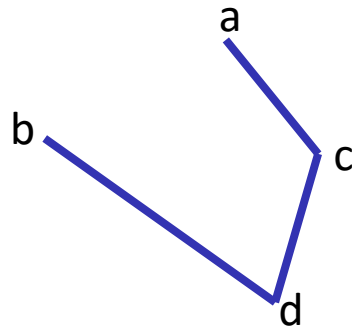
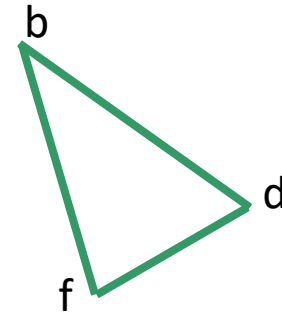
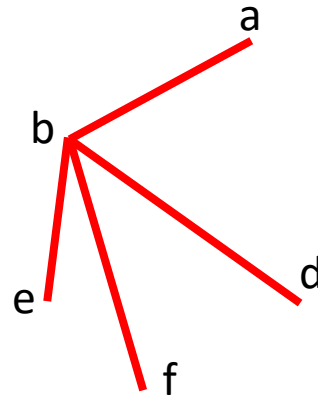
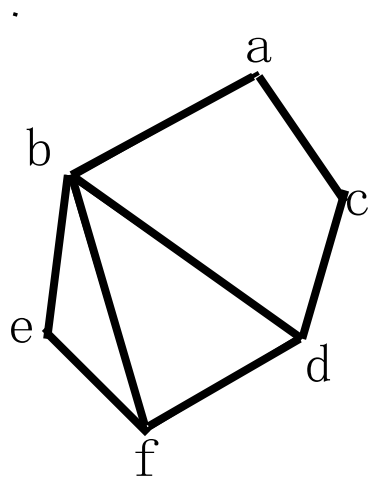


# Basic unit for distributed subgraph matching



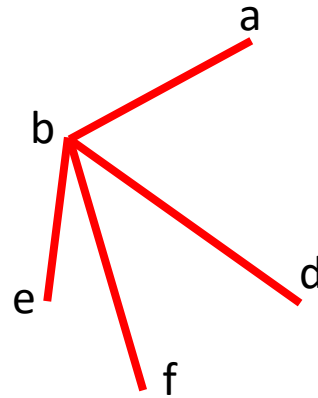
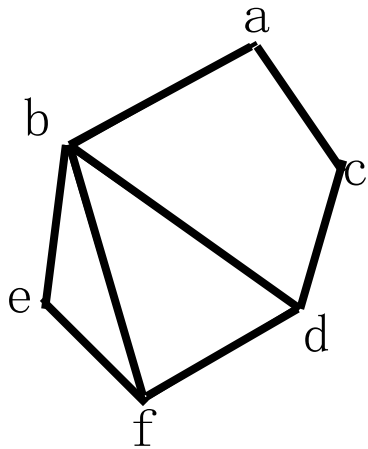
As a basic unit, which one is the best?

# Basic unit for distributed subgraph matching



As a basic unit, which one is the best?

# Basic unit for distributed subgraph matching

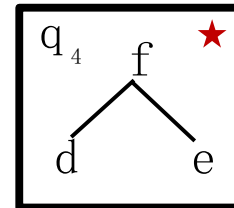
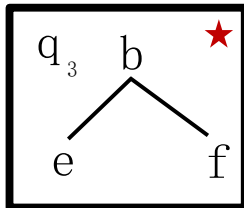
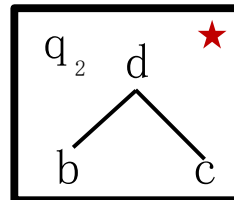
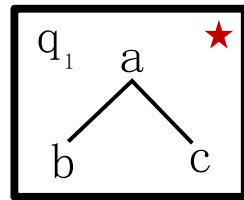
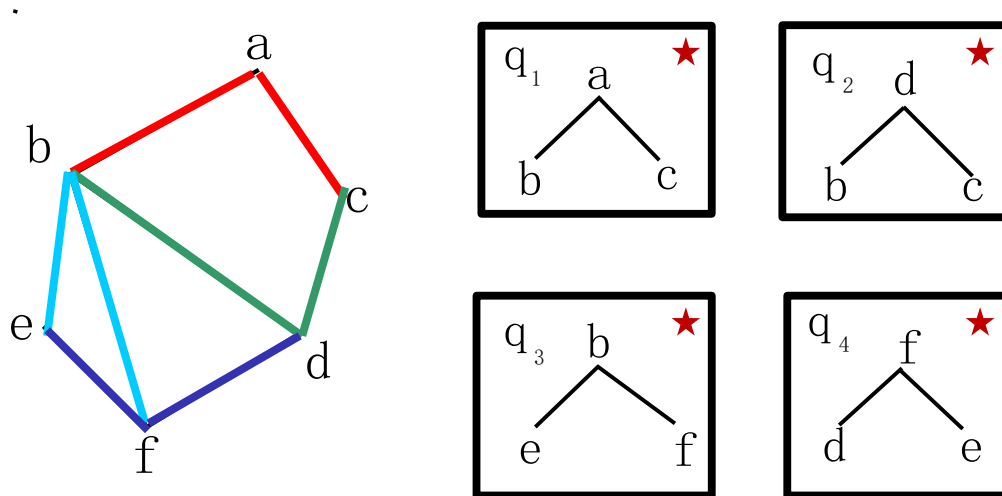


Twig

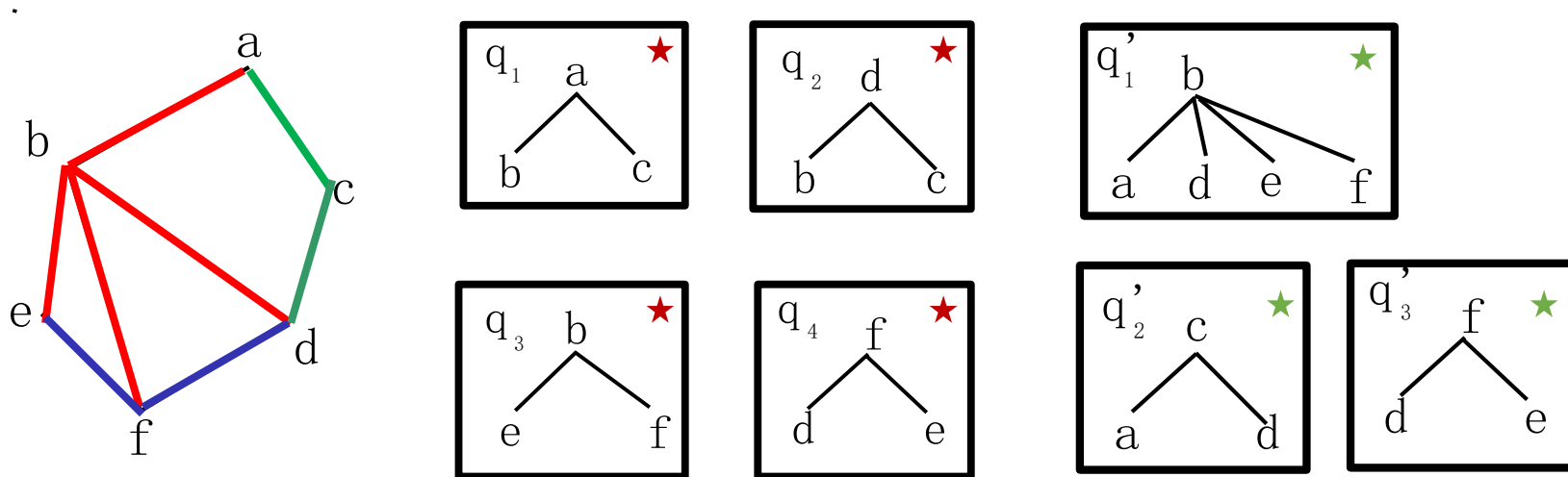
- Easy to decompose
- Height is always one
  - It at most needs to cross the network once

As a basic unit, which one is the best?

# Query decomposition



# Query decomposition



# Query optimization problems

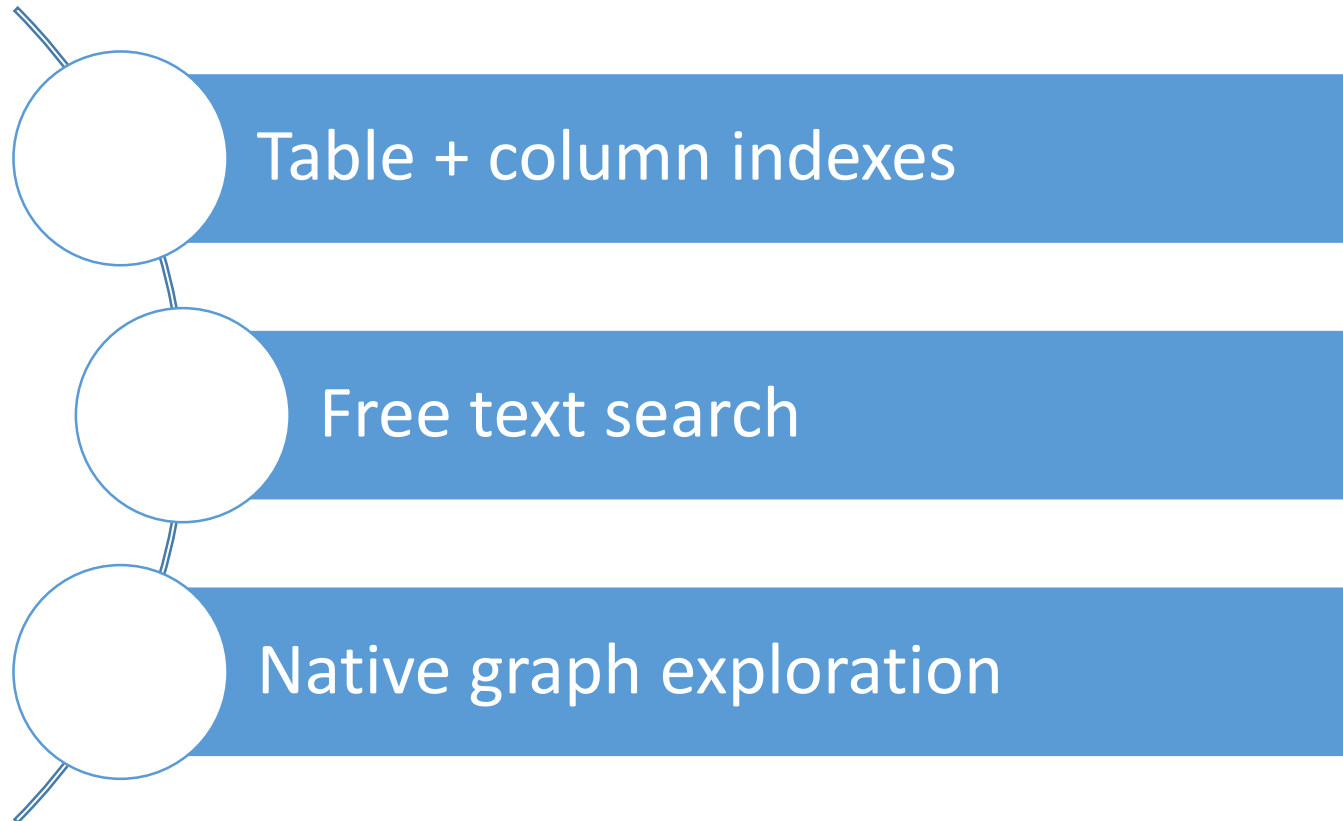
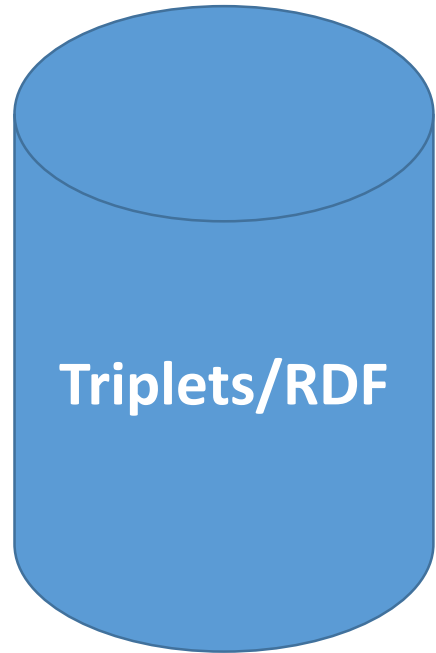
- How to choose a good query decomposition
- How to choose a good execution order
- How to choose a good join order

# Outline

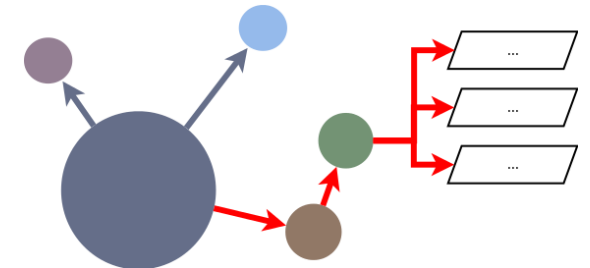
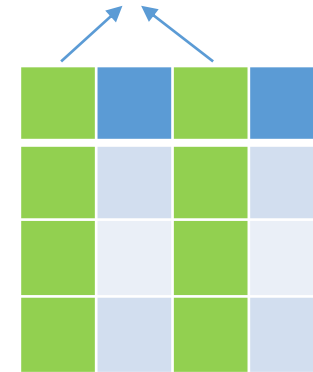
- Graph processing scenarios
- Challenges of large graph processing
- General design principles
- Offline analytics
- Online query processing
- **Case study**
- Graph generation
- Other graph representations and their applications



# How to Serve the Knowledge?



Column Index



# Representative Knowledge Serving Systems

System	Query Language	Known Scalability	Distributed
sw-Store	SPARQL	55M	V
RDFJoin	SPARQL	44M	
RDFKB	-	44M	
BitMat	SPARQL-like	47M	
RDF-3x	SPARQL	51M	V
Virtuoso	SPARQL	1,068M	V
Trinity	LIKQ, TQL, SPARQL	24.6B	V

Reference: A survey of RDF storage approaches (David C. FAYE, et al.)

# Problem and Our Goal

## Problem

- KG is a massive entity network
  - The most valuable part is its rich relationships, but
  - Currently mainly used via entity indexes
  - Cannot answer queries requiring accesses of **2+ hop relations**

## Goal

This project is to **provide advanced real-time knowledge graph serving operators**

- Serve the full-scale KG
- Make KG accessible in real time
- Provide advanced graph operators



# Challenges of Serving KG

Data size	
Raw RDF data	5T+
Triple Facts	25B+

- Complex data schema
  - Rich relations
  - Multi-typed entities

*123 mso/type.object.name "Pal"*

*123 mso/type.object.type  
mso/organism.dog*

*123 mso/organism.dog.breeds "Collie Rough"*

*123 mso/type.object.type mso/film.actor*

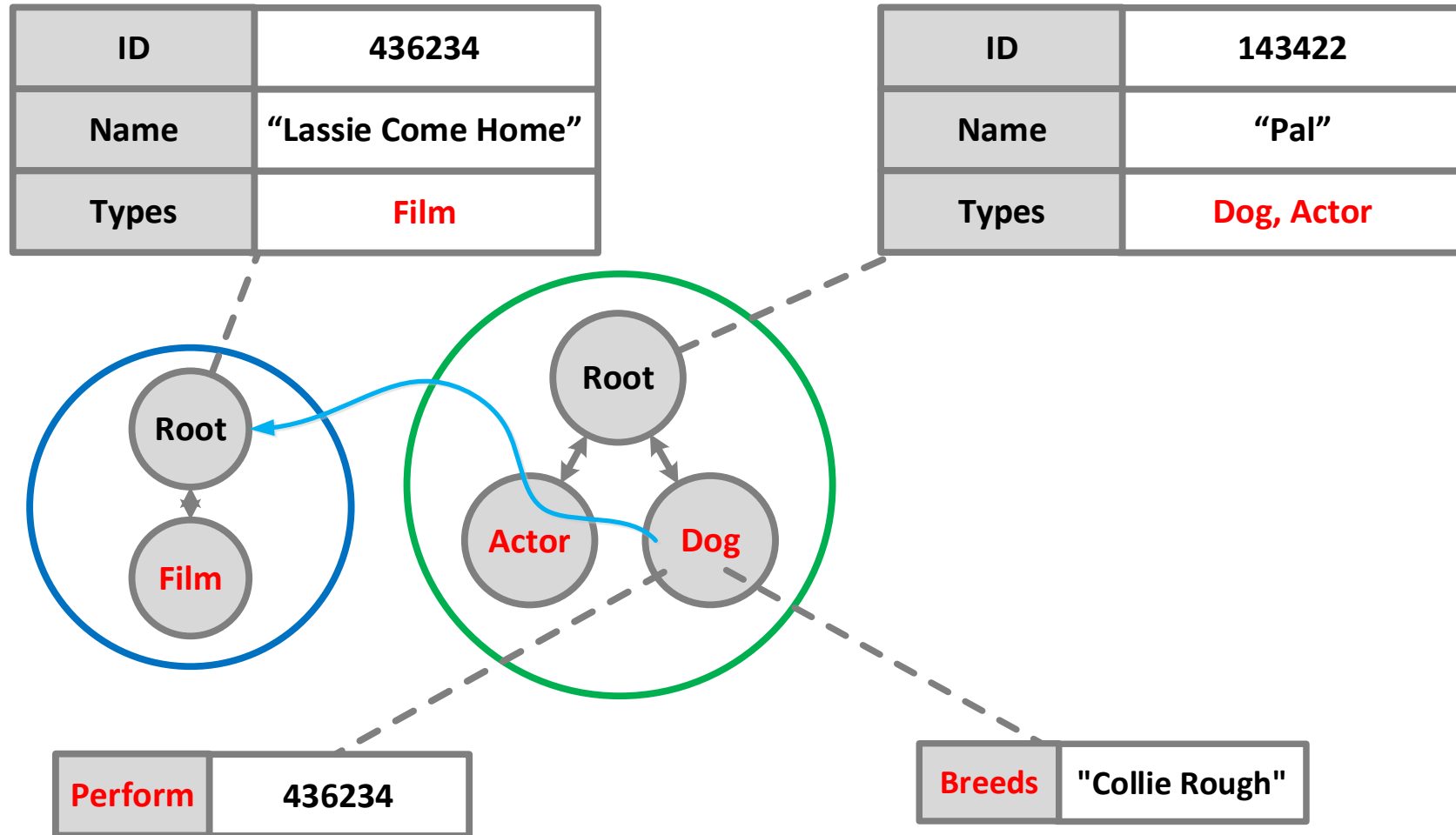
*123 mso/film.actor.film 789*

*789 mso/type.object.type mso/film.film*

*789 mso/type.object.name "Lassie Come Home"*

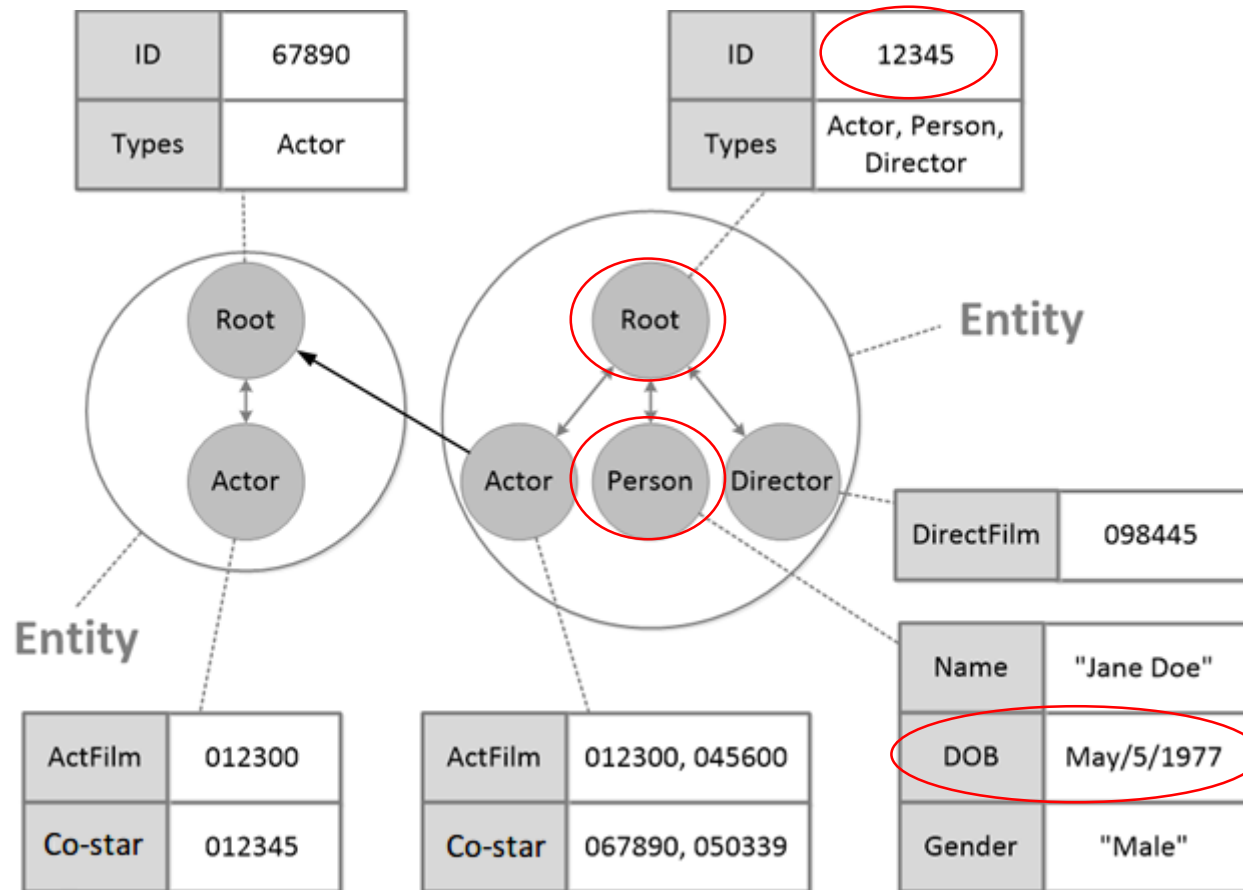
**"Pal"**

# A Strongly Typed System for RDF



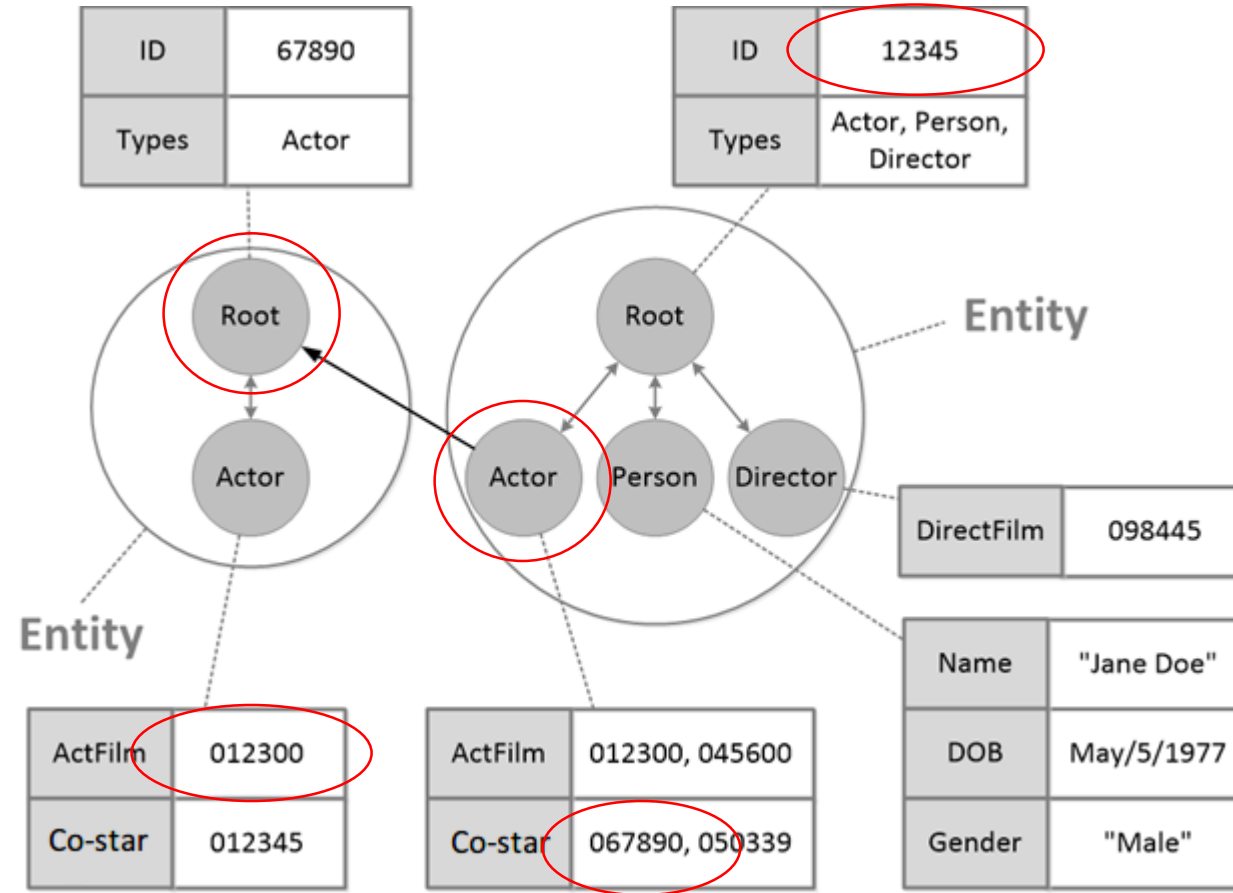
Models Multi-Typed Entities in a Strongly Typed Manner

# Strongly-typed data accesses



Get the DOB of entity 12345

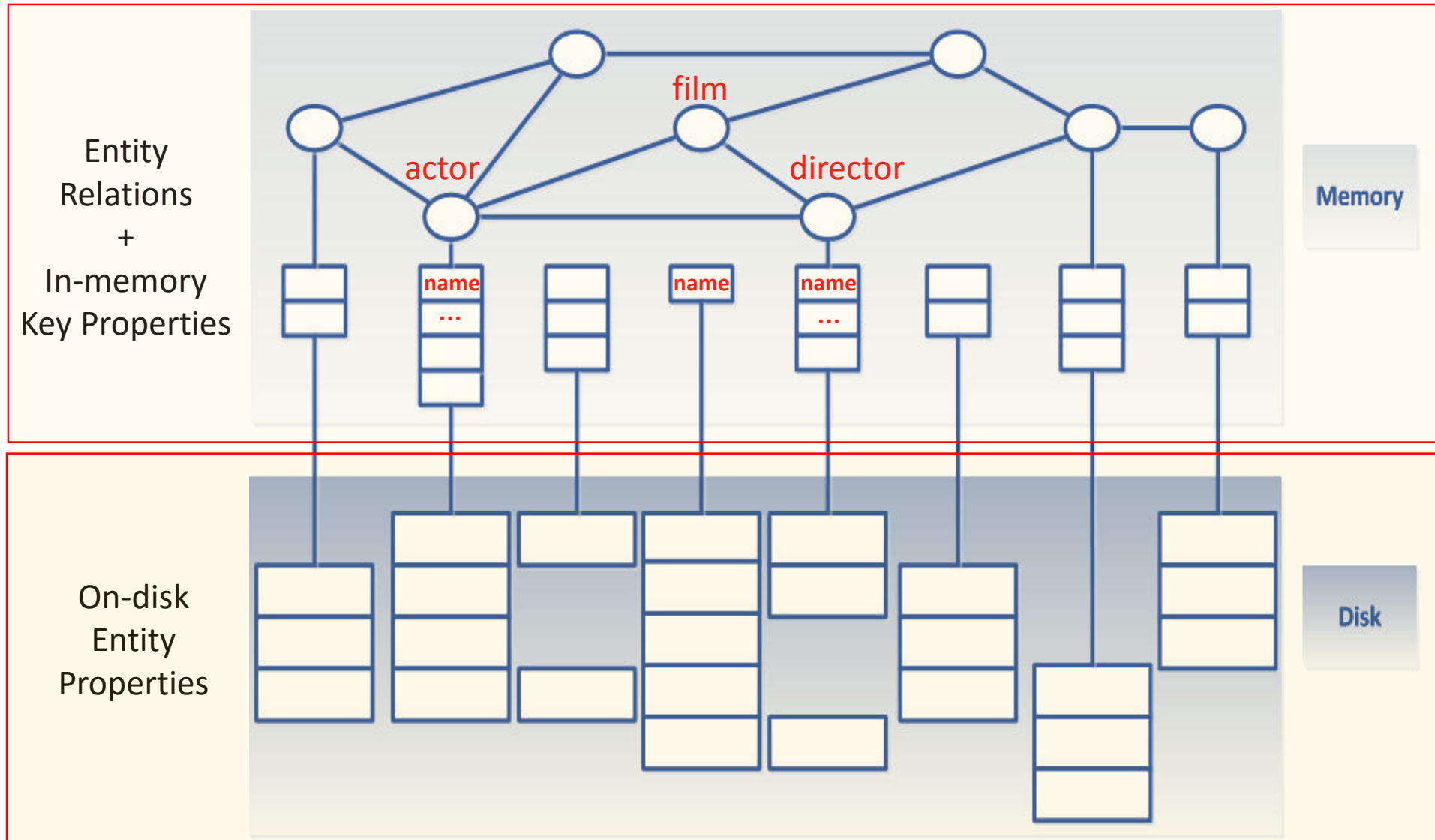
# Strongly-typed data accesses



Get the films of actors co-starring with entity 12345

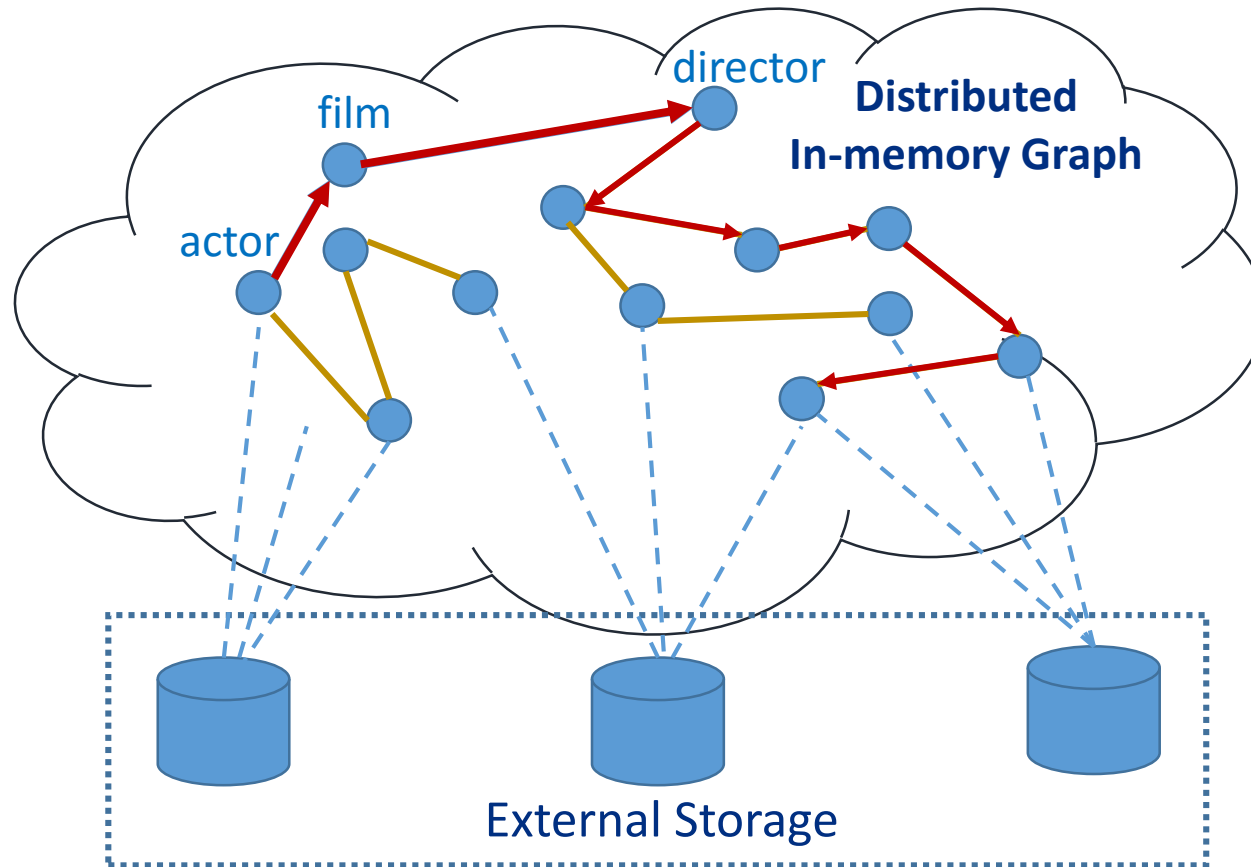



# Storage Architecture



# Query KG via Graph Exploration

Knowledge Serving Services/APIs





**Harvard University**  
 award.presenting\_organization, award.ranked\_item, award.winner, book.author, education.academic\_institution, education.educational\_institution ...

**Harvard University**

organization.organization, type.object

**harvard university**

internet.social\_network\_user, people.person, type.object

**harvard university**

internet.social\_network\_user, people.person, type.object

**Harvard University**

local.entity, type.object

**Harvard University**

local.entity, type.object

**Harvard University**



Harvard University is an American private Ivy League research university located in Cambridge, Massachusetts, United States, established in 1636 by the Massachusetts legislature. Harvard is the oldest institution of higher learning in the United States and the first corporation (officially The President and Fellows of Harvard College) chartered in the country. Harvard's history, influence,...

**Types**

award.presenting\_organization, award.ranked\_item, award.winner, book.author, education.academic\_institution, education.educational\_institution ...

**Predicates**

- education.educational\_institution.total\_enrollment
- education.educational\_institution.color
- education.educational\_institution.subsidiary\_or\_constituent\_schools**
- education.educational\_institution.number\_of\_staff
- education.educational\_institution.honorary\_degrees\_awarded
- education.educational\_institution.school\_sports\_team

[Prev Page](#) [Next Page](#)

**Values**

- "Harvard Extension School"
- "Harvard Medical School"
- "Harvard Business School"
- "Harvard College"
- "Harvard Division of Continuing Education"
- "John F. Kennedy School of Government"

[Prev Page](#) [Next Page](#)

Entity Explorer

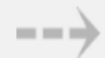
# Schema Graph

Meta Graph of Satori

Schema Type:

Go

Schema Path:



Go

### Fields:

.bust\_measurement mso/type.decimal  
.date\_of\_birth mso/type.datetime  
.eye\_color mso/type.text  
.first\_name mso/type.string  
.hair\_color mso/type.text  
.height mso/type.decimal  
.hips\_measurement mso/type.decimal  
.last\_name mso/type.string  
.waist\_measurement mso/type.decimal  
.weight mso/type.decimal

### Links:

.business\_employment\_tenure mso/business.employment\_tenure  
.children mso/people.person  
.city\_of\_birth mso/location.location

mso/people.person	.quotation	mso/media_common.quotation
mso/media_common.quotation	.character	mso/fictional_universe.character
mso/fictional_universe.character	.appears_in_the se_fictional_uni verses	mso/fictional_universe.universe
mso/fictional_universe.universe	.literary_series	mso/book.literary_series
mso/book.literary_series	.author	mso/book.author

# Schema Graph Services

## Satori Knowledge Graph Access API

API Names	Availability	Description
<a href="#">GetEntityIdByName</a>	Available	Gets a list of Trinity entity Ids by the specified entity name.
<a href="#">GetPredicatesByEntityId</a>	Available	Gets a list of predicates for the entity with the specified Trinity entity Id.
<a href="#">GetValuesByEntityPredicate</a>	Available	Gets the values of the specified predicates for the specified entity.
<a href="#">GetSubjectsByPredicateObject</a>	Available	Gets the subjects for the given object and a predicate.
<a href="#">GetEntityIdBySatoriId</a>	Available	Gets the corresponding Trinity entity Id for the specified Satori Guid.
<a href="#">GetSatoriIdByEntityId</a>	Available	Gets the corresponding Satori Guid for the specified Trinity entity Id.
<a href="#">GetRankedEntityIdByName</a>	Available	Gets a list of Trinity entity Ids by the specified entity name sorted by their static rank.
<a href="#">GetScoredValuesByEntityPredicate</a>	Available	Gets the values of the specified predicates for the specified entity, sorted by confidence score.
<a href="#">GetSortScoredValuesByEntityPredicate</a>	Available	Gets the values of the specified predicates for the specified entity, sorted by the column index (1 for...
<a href="#">GetEntityDescription</a>	Available	Gets the description of the specified entityid.

Testing: [GetScoredValuesByEntityPredicate](#)

Please input test parameters below:

EntityId

Predicate

PredicateValue	ConfidenceScore	OverallScore
2987469205879	0.71	1.311128
116281907553515	0.71	1.409593
265920831012309	0.71	1.416611
58184534540412	0.71	1.710736
237856925167352	0.71	1.228339
57628320423344	0.71	1.272193

Page 1 of 1

# Knowledge Serving APIs

# Knowledge Serving for Text Processing

## APIs for Knowledge Access

List<string[]> GetEntityIdByName (string entityName)

List<string> GetPredicatesByEntityId (string entityId)

List<string[]> GetValuesByEntityPredicate (string entityId, string predicate)

.....

• List<string[]> GetEntityIdByName (string entityName)

- Input
  - An entity name
- Output
  - A list of <entity id, entity ranking score> pairs

SATORI | james cameron

Entity Index

	<b>James Cameron</b> Person, Film director, Film actor, Film producer, Film writer James Francis Cameron is a Canadian film director, film producer, deep-sea explorer, screenwriter, and editor. He first found success with the science-fiction hit The Terminator. He then became a popu	In Trigger List	12.9025
	<b>James Cameron</b> Organism, Actor, Social network user, Person I have been involved within the Audio Visual Industry for over 10 years and have first hand experience in Custom Installation, Design, Supply and Commissioning. At Cameron & Noyes we offer audio visual		2.10592
	<b>James Cameron</b> Organism, Actor, Film actor, Person, Film writer		2.07427

• List<string> GetPredicatesByEntityId (string entityId)

- Input
  - An entity id
- Output
  - A set of predicates

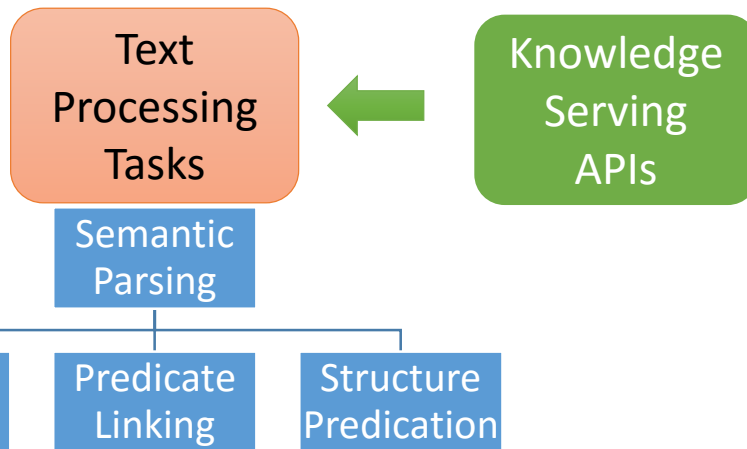
film.actor.film	Titanic; The Cutting Edge; The Magic of Movie Editing; Ghosts of the Abyss; Duets; Side By Side; The Muse; Solartax; Aro; Your Studio and You; Ray Harryhausen; Special Effects Titan; The Exodus Decoded; Hollywood between Paranoia and Sci-Fi; Auto Motives; Brian May's Brief History of 3D; Secret Life of Old Rose; The Art of Gloria Stuart
film.director.film	Titanic; Avatar; The Terminator; Terminator 2: Judgment Day; Aliens; The Abyss; True Lies; Pisanha II: The Spawning; An Alien Quadrilogy; Avatar 3; Avatar 4; T2 3-D Battle Across Time; Untitled James Cameron/3D Diving Documentary; Battle An
film.producer.film	Titanic; Avatar; Terminator 2: Judgment Day; True Lies; Solaris; Strange Days; Avatar 2; Aliens of the Deep; Ghosts of the Xenogenesis; Avatar 3; The Exodus Decoded
film.story_contributor.film_story_credit	Aliens; Terminator Salvation; Terminator 3: Rise of the Machines; Strange Days; Avatar 3
film.writer.film	Titanic; Avatar; Terminator; The Terminator; Terminator 2: Judgment Day; Aliens; The Abyss; True Lies; Pisanha II: The Spawning; Terminator 3: Rise of the Machines; Terminator 5; Avatar 3; Avatar 4; Avatar 3; Battle Angel; Titanic
influence.influence_node.influenced	Nick Saglimbeni; Joe Vaskovsky
organization.founder.organizations_founded	Lightstorm Entertainment; Digital Domain; Cameron Pace Group

• List<string[]> GetValuesByEntityPredicate (string entityId, string predicate)

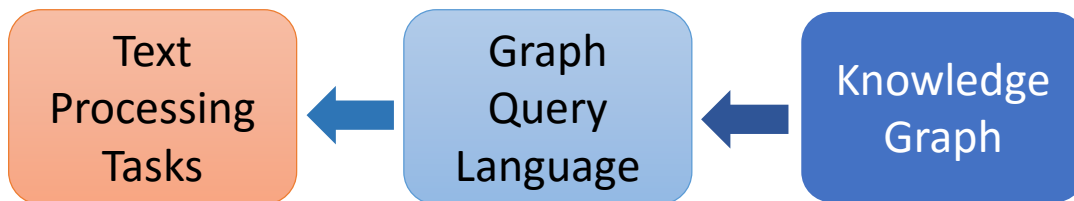
- Input
  - An entity id and a predicate
- Output
  - A set of <entity id, confidence score> pairs

film.actor.film	Titanic; The Cutting Edge; The Magic of Movie Editing; Ghosts of the Abyss; Duets; Side By Side; Your Studio and You; Ray Harryhausen; Special Effects Titan; The Exodus Decoded; Hollywood between Paranoia and Sci-Fi; Auto Motives; Brian May's Brief History of 3D; Secret Life of Old Rose; The Art of Gloria Stuart	Overall Score: 3.482116
	Confidence: 0.6800, Occ: 8.30, Rank: 8964	
	Contexts: freebase, wikipedia_verification	

1



2



# Entity Disambiguation/Type Resolving

Who are the advisees of Michael Jordan?

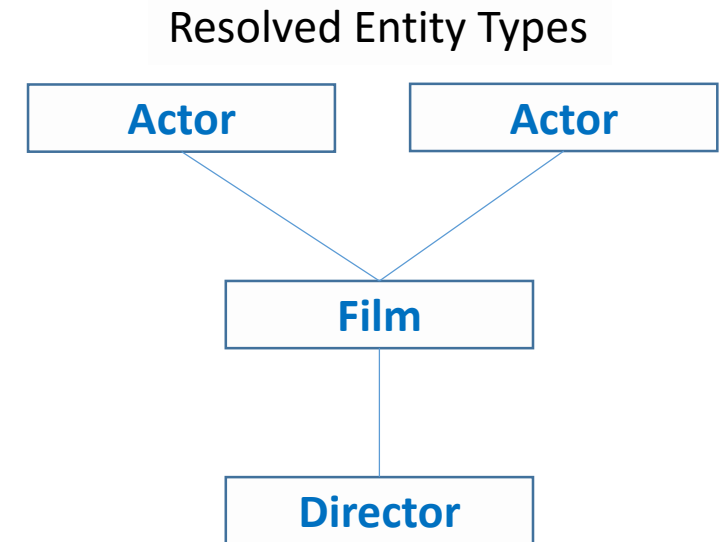
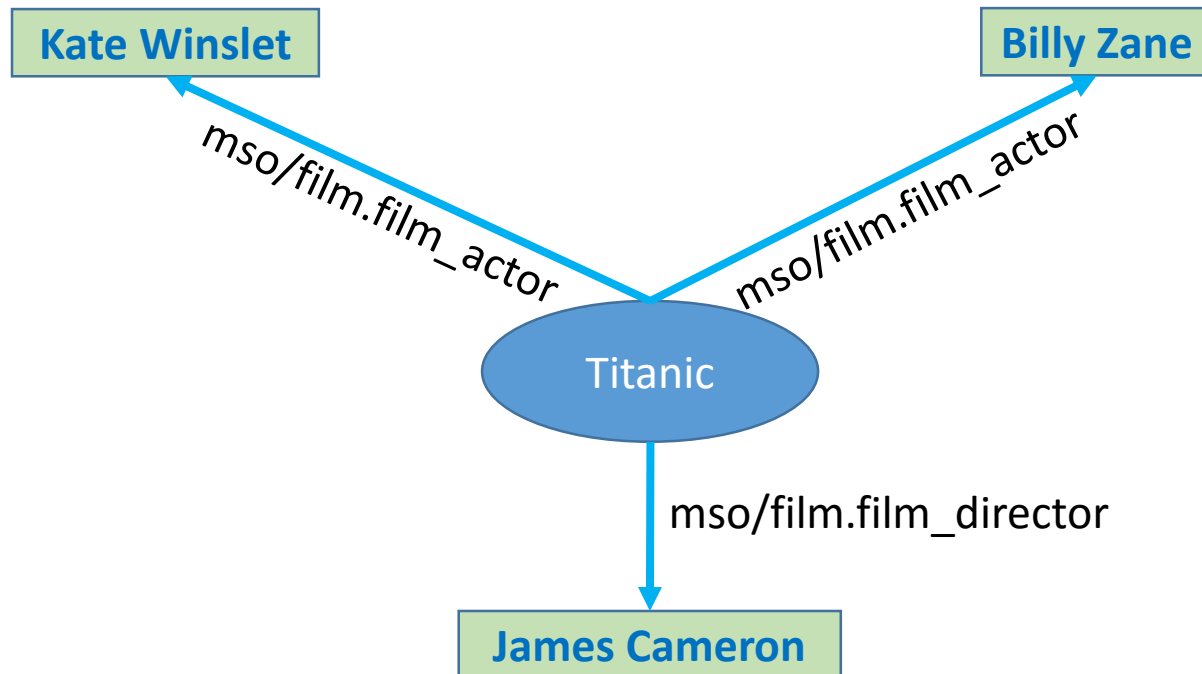
**Which Michael?**

- [Michael Jordan \(footballer\)](#) (born 1986)
- [Michael-Hakim Jordan](#) (basketball player) (born 1977)
- [Michael Jordan \(Irish politician\)](#)
- [Michael I. Jordan](#) (Professor) (born 1957)
- ....

8234993200123	mso/education.academic.advisees	"Andrew Ng"
8234993200123	mso/type.object.name	"Michael Jordan"
8234993200123	mso/people.person.profession	"Professor"

# Discover Linking Entities

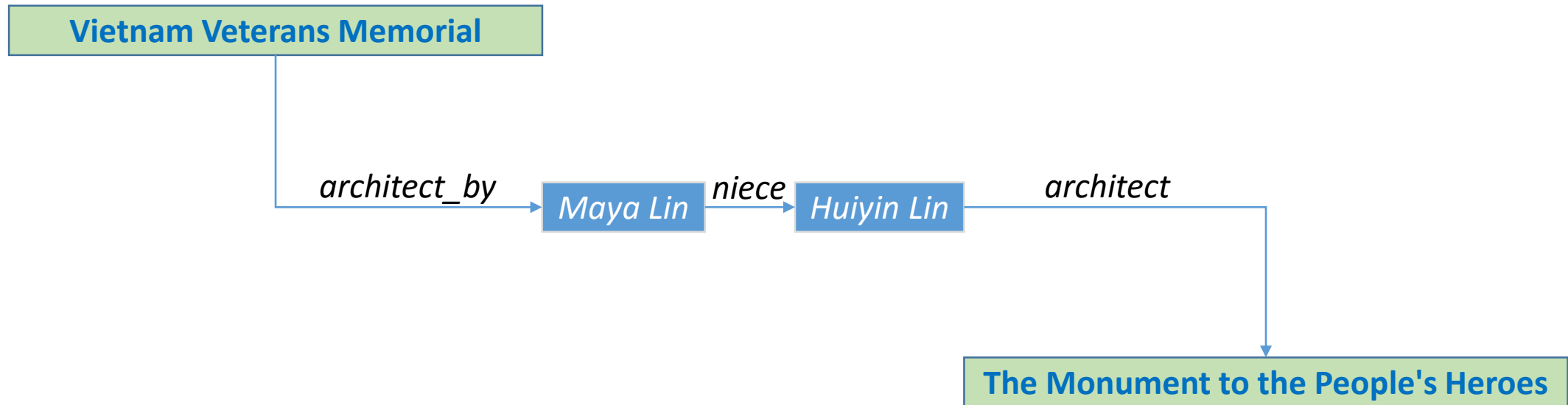
Given three entities “*Kate Winslet*”, “*Billy Zane*”, and “*James Cameron*”





# Discover Linking Relations

Given two entities “*Vietnam Veterans Memorial*” and “*The Monument to the People's Heroes*”



Satori

film

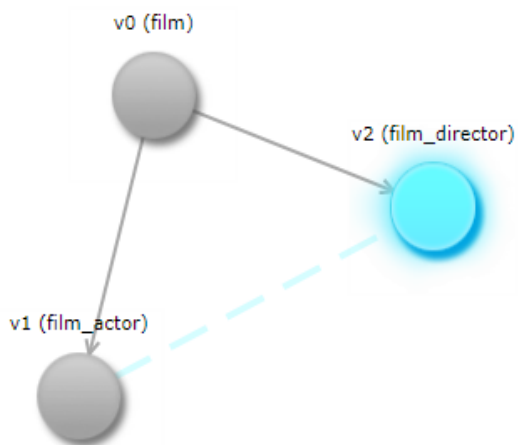
Add

View

TQL

Results

# Graphical Query Interface



Node Information

Alias: v2

Type: film\_director

URI: mso\_film\_director

Conditions:

Outputs:

- Steve Saari
- Steve Sacks
- Steve Sale
- Steve Salinaro
- Steve Salisian
- Steve Sanders
- Steve Sanguedolce
- Steve Saporito
- Steve Savage
- Steve Savitz
- Steve Scheffler

You could add some conditions a

name =



Submit



# Multi-hop Relation Search

Home Schema API Relation Search People Relation Search

Satori

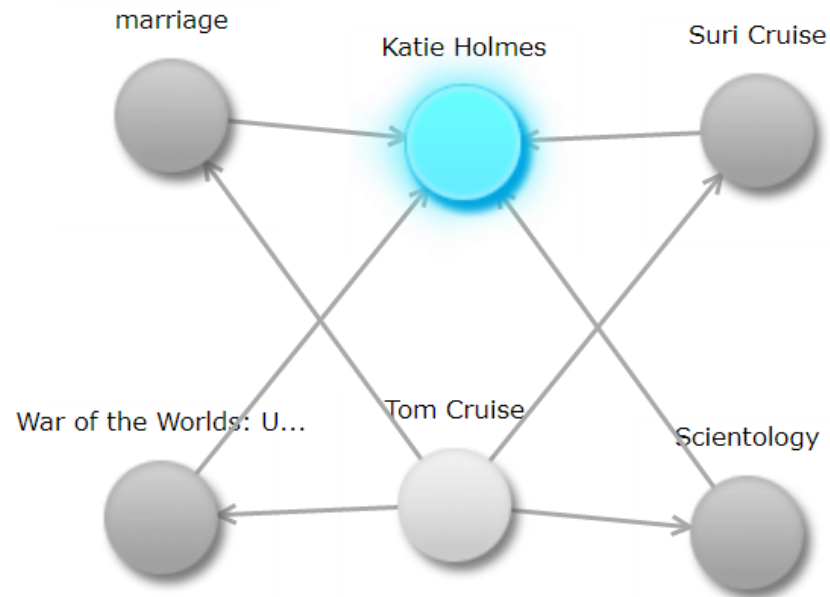
Add

Search

Tom Cruise, Katie Holmes

Results

[View](#)



## Katie Holmes

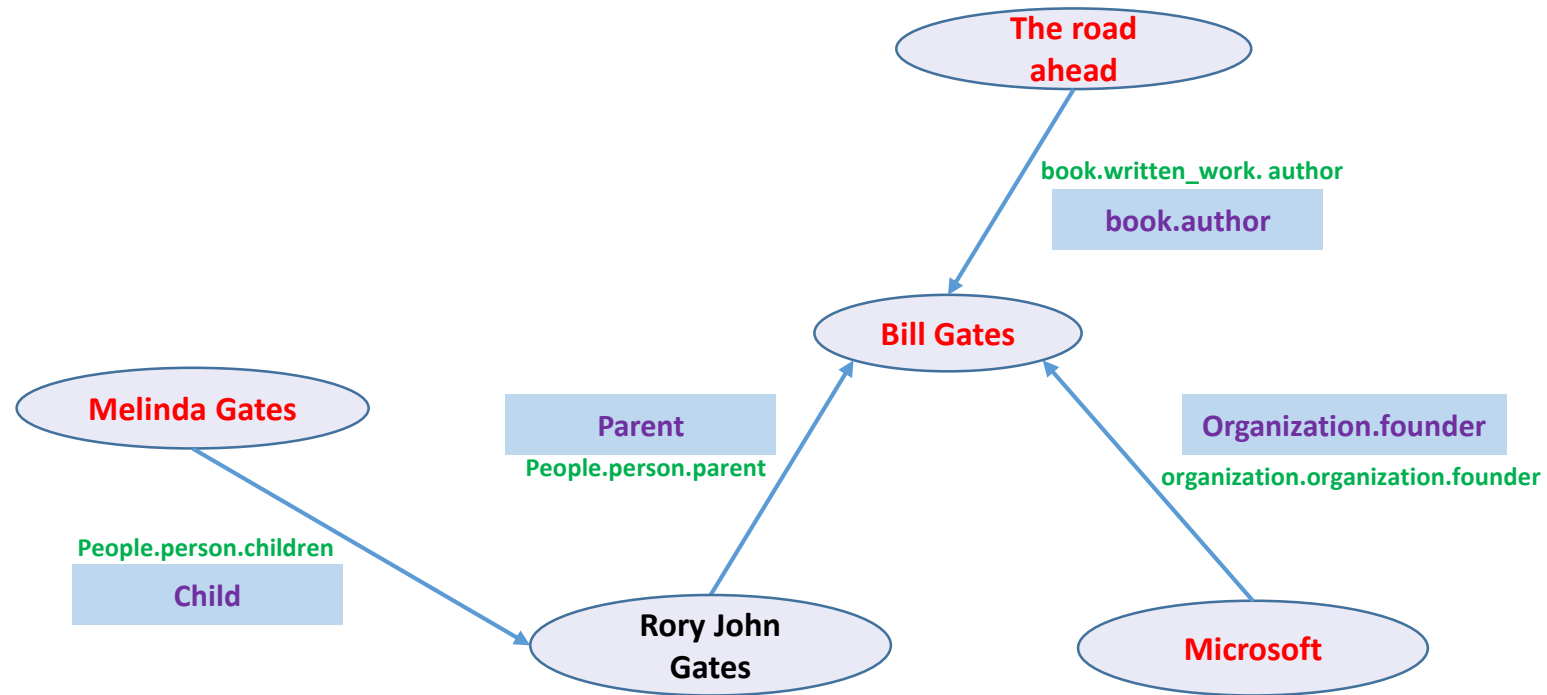


Kate Noelle "Katie" Holmes (born December 18, 1978) is an American actress and model who first achieved fame for her role as Joey Potter on The WB television teen drama Dawson's Creek from 1998 to 2003....

### Types

award.nominee, award.ranked\_item, award.winner, film.actor, film.writer, medicine.notable\_person\_with\_medical\_condition ...

# Keyword Search



(Bill Gates, Melinda Gates, Microsoft, The road ahead)

# Relation Search Demo

Satori

**Tom Cruise, Mimi Rogers, Nicole Kidman, Katie Holmes**

[Results](#) [View](#)

94 Results (103 ms)

Results
o--film.actor.film-->(Eyes Wide Shut)--film.film.actor-->(Nicole Kidman)
o--film.actor.film-->(National Movie Awards)--film.film.actor-->(Katie Holmes)
o--film.actor.film-->(InStyle: Celebrity Weddings)--film.film.actor-->(Katie Holmes)
o--people.person.marriage-->(marriage)--time.event.person-->(Katie Holmes)
o--people.person.marriage-->(marriage)--time.event.person-->(Nicole Kidman)
o--film.actor.film-->(War of the Worlds: UK Premiere Special)--film.film.actor-->(Katie Holmes)
o--film.producer.film-->(The Others)--award.nominated_work.nomination-->(nomination)--award.nomination.nominee--(Nicole Kidman)
o--people.person.children-->(Connor Cruise)--people.person.siblings-->(Isabella Jane Cruise)--people.person.parent--(Nicole Kidman)
o--film.producer.film-->(The Others)--award.nominated_work.nomination-->(nomination)--award.nomination.nominee--(Nicole Kidman)
o--film.actor.performance-->(performance)--film.performance.film-->(Eyes Wide Shut)--film.film.actor--(Nicole Kidman)

[Prev Page](#) [Next Page](#)

# Relation Search Demo

Satori

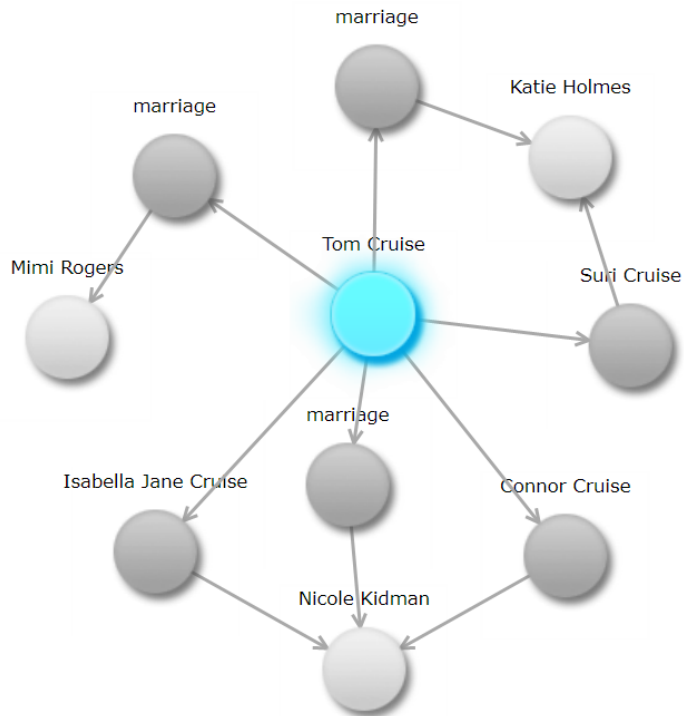
Add

Search

**Tom Cruise, Mimi Rogers, Nicole Kidman, Katie Holmes**

Results

[View](#)



## Tom Cruise



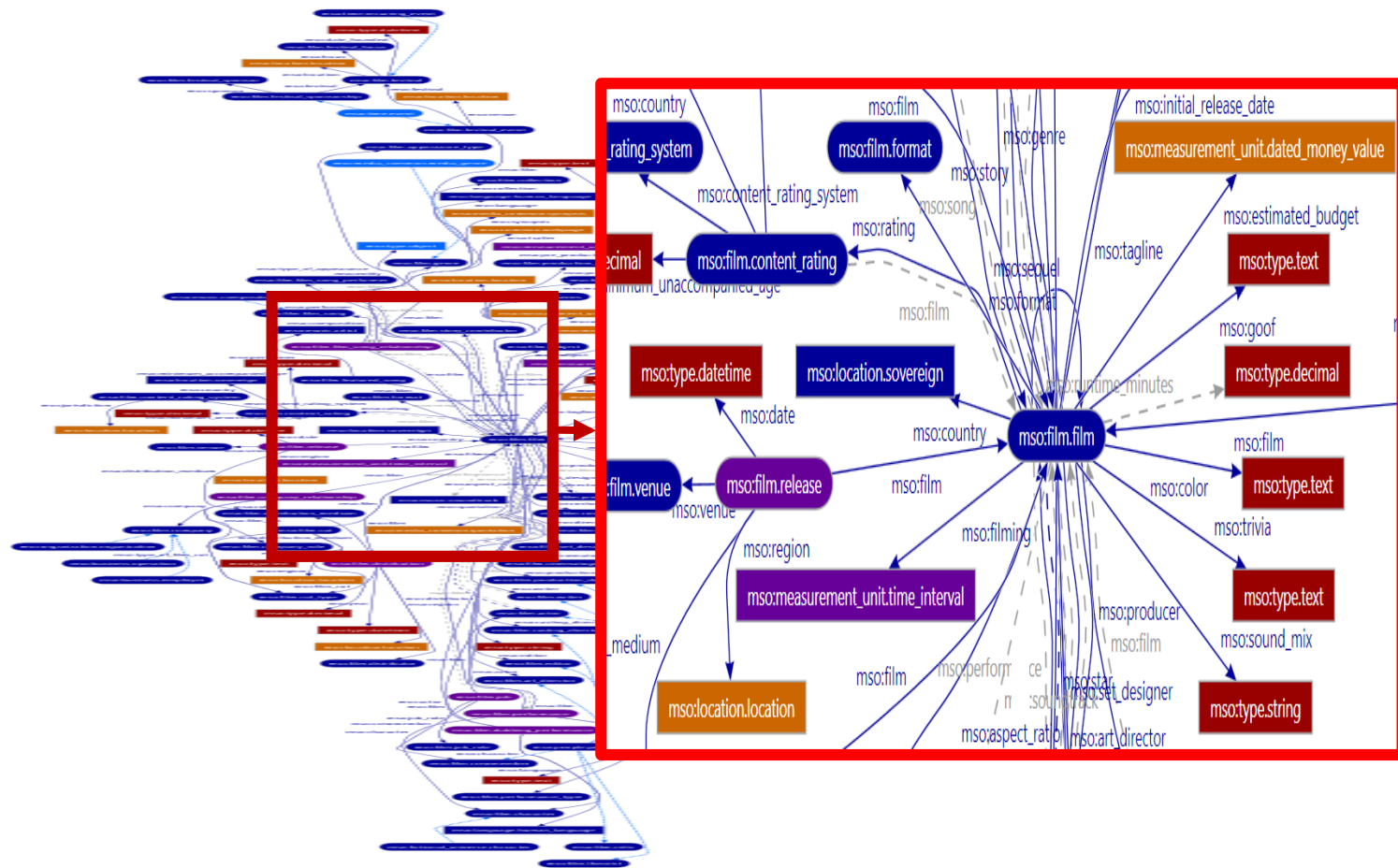
Tom Cruise (born Thomas Cruise Mapother IV; July 3, 1962), is an American film actor and producer. He has been nominated for three Academy Awards and has won three Golden Globe Awards. He started his career at age 19 in the 1981 film *Endless Love*. After portraying supporting roles in *Taps* (1981) and *The Outsiders* (1983), his first leading role was in *Risky Business*, released in August 1983. Cruise became a full-fledged movie...

### Types

award.nominee, award.winner, film.actor, film.director, film.producer, film.story\_contributor ...

# How can we make it fast enough

- Big data
  - emm, we have a large variety of tools available
- But, how do we handle “big schema” ...



# Big Schema



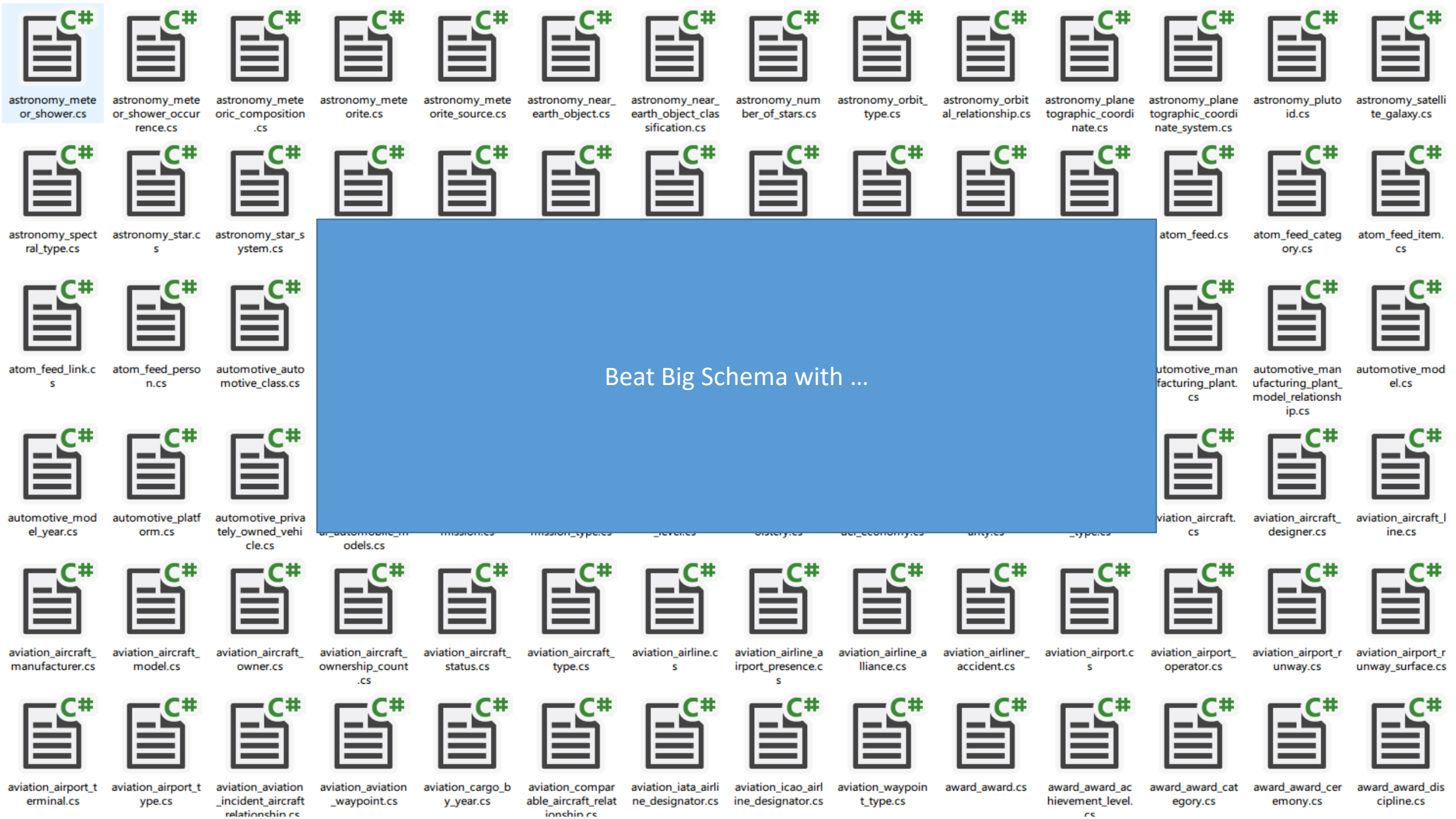
# How can we make it fast enough

- Big data
  - emm, we have a large variety of tools available
- But, how do we handle “big schema” ...  
If we treat everything as texts and build indexes for these piles of words



- Inefficient data processing (weakly-typed system)
- Limited search functionality we can provide

Beat Big Schema with ...



Beat Big Schema with ...



astronomy\_meteor\_shower.cs



astronomy\_meteor\_shower\_occurrence.cs



astronomy\_meteor\_composition.cs



astronomy\_meteorite.cs



astronomy\_meteorite\_source.cs



astronomy\_near\_earth\_object.cs



astronomy\_near\_earth\_object\_classification.cs



astronomy\_number\_of\_stars.cs



astronomy\_orbit\_type.cs



astronomy\_orbital\_relationship.cs



astronomy\_planetographic\_coordinate.cs



astronomy\_planetographic\_coordinate\_system.cs



astronomy\_pluto\_id.cs



astronomy\_satellite\_galaxy.cs



astronomy\_spectral\_type.cs



astronomy\_stars.cs



astronomy\_star\_system.cs



astronomy\_star\_system.cs



astronomy\_star\_system.cs



astronomy\_star\_system.cs



astronomy\_star\_system.cs



astronomy\_star\_system.cs



astronomy\_star\_system.cs



astronomy\_star\_system.cs



astronomy\_star\_system.cs



atom\_feed.cs



atom\_feed\_category.cs



atom\_feed\_item.cs



atom\_feed\_links.cs



atom\_feed\_persons.cs



automotive\_automotive\_class.cs



automotive\_automotive\_class.cs



automotive\_automotive\_class.cs



automotive\_automotive\_class.cs



automotive\_automotive\_class.cs



automotive\_automotive\_class.cs



automotive\_automotive\_class.cs



automotive\_automotive\_class.cs



automotive\_manufacturing\_plant.cs



automotive\_manufacturing\_plant\_model\_relationship.cs



automotive\_model.cs



automotive\_model\_year.cs



automotive\_platform.cs



automotive\_privately\_owned\_vehicle.cs



automotive\_privately\_owned\_vehicle.cs



automotive\_privately\_owned\_vehicle.cs



automotive\_privately\_owned\_vehicle.cs



automotive\_privately\_owned\_vehicle.cs



automotive\_privately\_owned\_vehicle.cs



automotive\_privately\_owned\_vehicle.cs



automotive\_privately\_owned\_vehicle.cs



aviation\_aircraft.cs



aviation\_aircraft\_designer.cs



aviation\_aircraft\_line.cs



aviation\_aircraft\_manufacturer.cs



aviation\_aircraft\_model.cs



aviation\_aircraft\_owner.cs



aviation\_aircraft\_ownership\_count.cs



aviation\_aircraft\_status.cs



aviation\_aircraft\_type.cs



aviation\_airline.cs



aviation\_airline\_airport\_presence.cs



aviation\_airline\_alliance.cs



aviation\_airline\_accident.cs



aviation\_airports.cs



aviation\_airport\_operator.cs



aviation\_airport\_runway.cs



aviation\_airport\_runway\_surface.cs



aviation\_airport\_terminal.cs



aviation\_airport\_type.cs



aviation\_incident\_aircraft\_relationship.cs



aviation\_aviation\_waypoint.cs



aviation\_cargo\_bay\_year.cs



aviation\_comparable\_aircraft\_relationship.cs



aviation\_iata\_airline\_designator.cs



aviation\_icao\_airline\_designator.cs



aviation\_waypoint\_type.cs



award\_award.cs



award\_award\_achievement\_level.cs



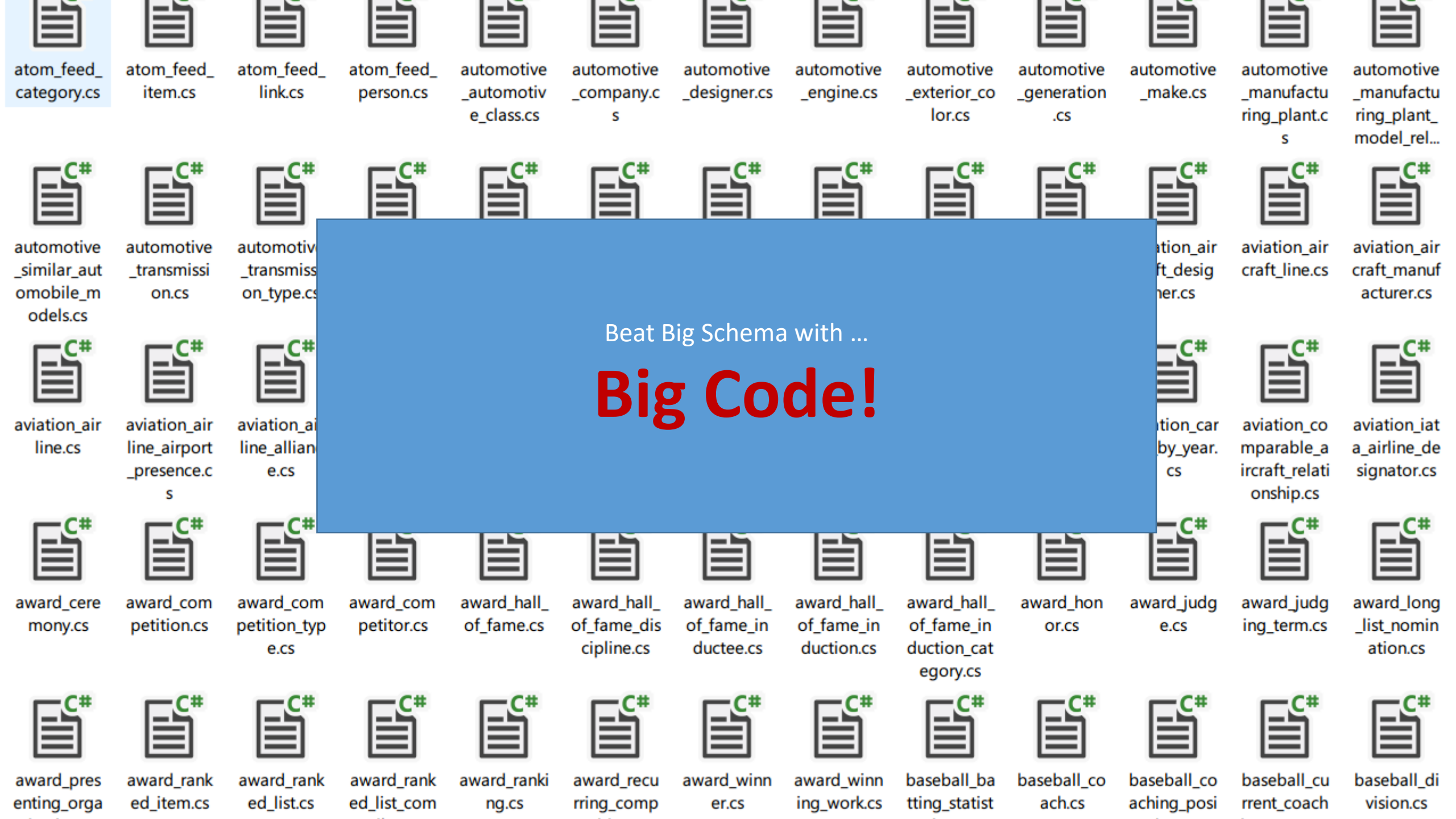
award\_award\_category.cs



award\_award\_ceremony.cs



award\_award\_discipline.cs



Beat Big Schema with ...

**Big Code!**

atom\_feed\_category.cs

atom\_feed\_item.cs

atom\_feed\_link.cs

atom\_feed\_person.cs

automotive\_automotive\_class.cs

automotive\_company.cs

automotive\_designer.cs

automotive\_engine.cs

automotive\_exterior\_color.cs

automotive\_generation.cs

automotive\_make.cs

automotive\_manufacturing\_plants

automotive\_manufacturing\_plant\_model\_rela...

automotive\_similar\_automobile\_models.cs

automotive\_transmission.cs

automotive\_transmission\_type.cs

aviation\_aircraft\_line.cs

aviation\_aircraft\_manufacturer.cs

aviation\_car\_by\_year.cs

aviation\_comparable\_aircraft\_relationship.cs

aviation\_jet\_airline\_designator.cs

award\_ceremony.cs

award\_competition.cs

award\_competition\_type.cs

award\_competitor.cs

award\_hall\_of\_fame.cs

award\_hall\_of\_fame\_discipline.cs

award\_hall\_of\_fame\_inductee.cs

award\_hall\_of\_fame\_induction.cs

award\_hall\_of\_fame\_induction\_category.cs

award\_honor.cs

award\_judging.cs

award\_judging\_term.cs

award\_long\_list\_nomination.cs

award\_presenting\_organization.cs

award\_ranked\_item.cs

award\_ranked\_list.cs

award\_ranked\_list\_coming.cs

award\_ranking.cs

award\_recurring\_competition.cs

award\_winner.cs

award\_winning\_work.cs

baseball\_batting\_statistics.cs

baseball\_coach.cs

baseball\_coaching\_position.cs

baseball\_current\_coach.cs

baseball\_diagnostics.cs

baseball\_diagnostics.cs

baseball\_diagnostics.cs

baseball\_diagnostics.cs

baseball\_diagnostics.cs

baseball\_diagnostics.cs

# Freebase Graph:

- Generated lines of code for Freebase:  
**8,868,163**
- Bytes of code: **446,747,058**

# What is the huge amount of code for?

- Provides extremely fine-grained data access methods best matching the data



**= Efficiency**

# Outline

- Graph processing scenarios
- Challenges of large graph processing
- General design principles
- Offline analytics
- Online query processing
- Case study
- **Graph generation**
- Other graph representations and their applications

# What is a graph generator & why do we need one

- A graph generator generates can graphs with user-specified size and properties
- We need to generate large graphs for experiments
- Large graph generation takes a long time



# PGBL graph generator

[http://www.boost.org/doc/libs/1\\_59\\_0/libs/graph\\_parallel/doc/html/rmat\\_generator.html](http://www.boost.org/doc/libs/1_59_0/libs/graph_parallel/doc/html/rmat_generator.html)

**When the existing ones cannot meet our needs, we may want to write one.**

# What is a good graph generator

- It can generate a graph with certain properties
- It can generate a large graph fast
- It is as resource economical as possible
- It can generate graphs in native graph formats

# Graph representation: adjacency list vs. matrix

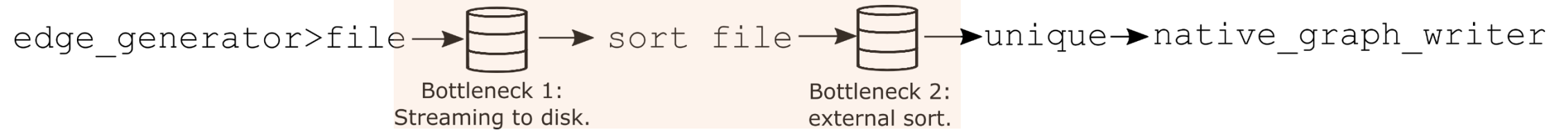
- In most cases, adjacency list is **preferable** to the matrix representation
  - Matrix does not support dynamic node insertion and deletion
  - The space overhead is high when we are generating a sparse graph

# A common graph generation pipeline

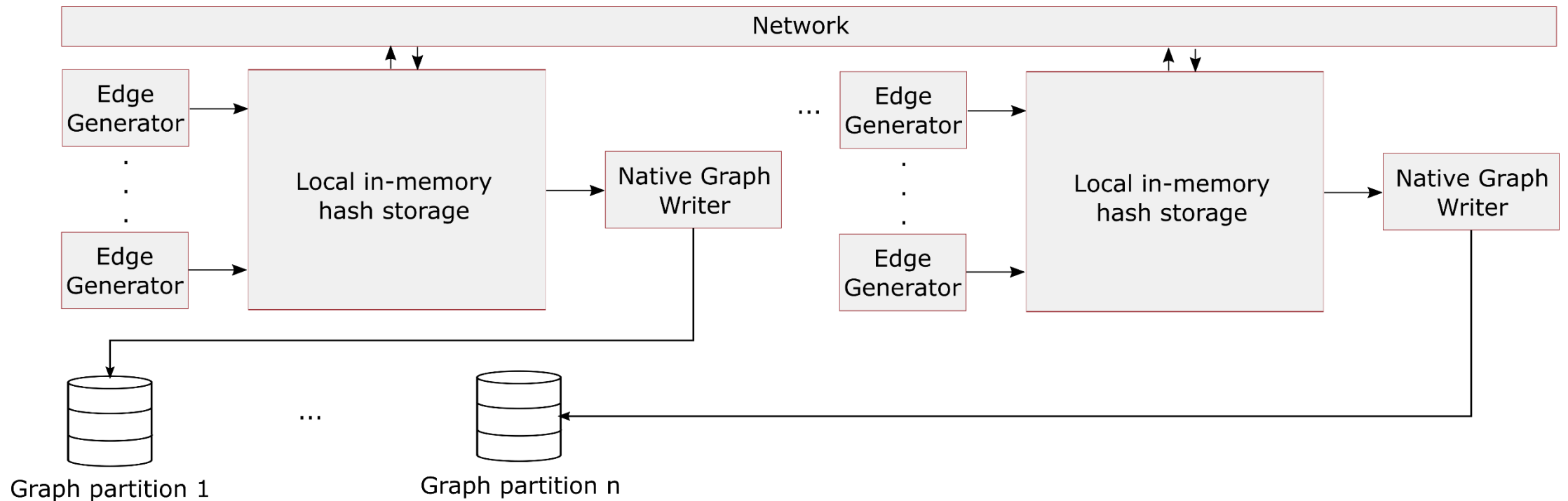


# Bottlenecks of the pipeline

## Sorting Edges

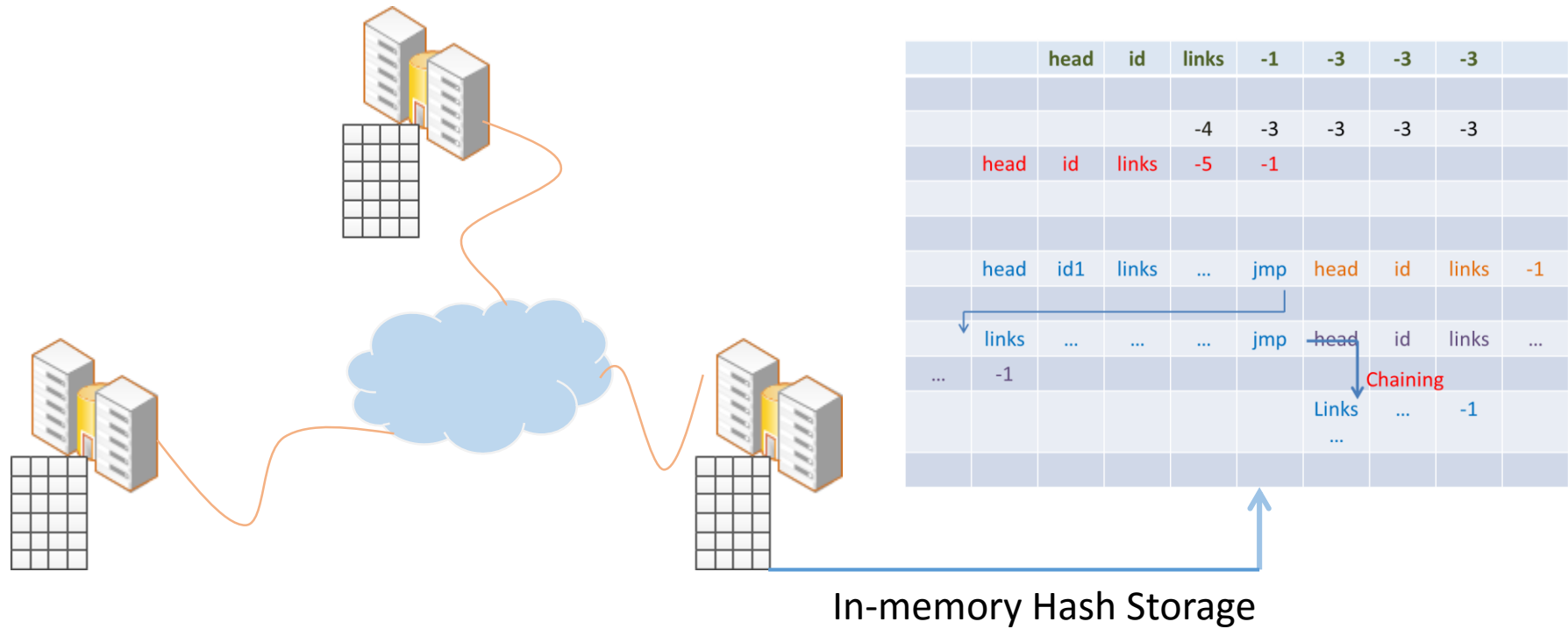


# Avoid sorting by using an in-memory hash storage



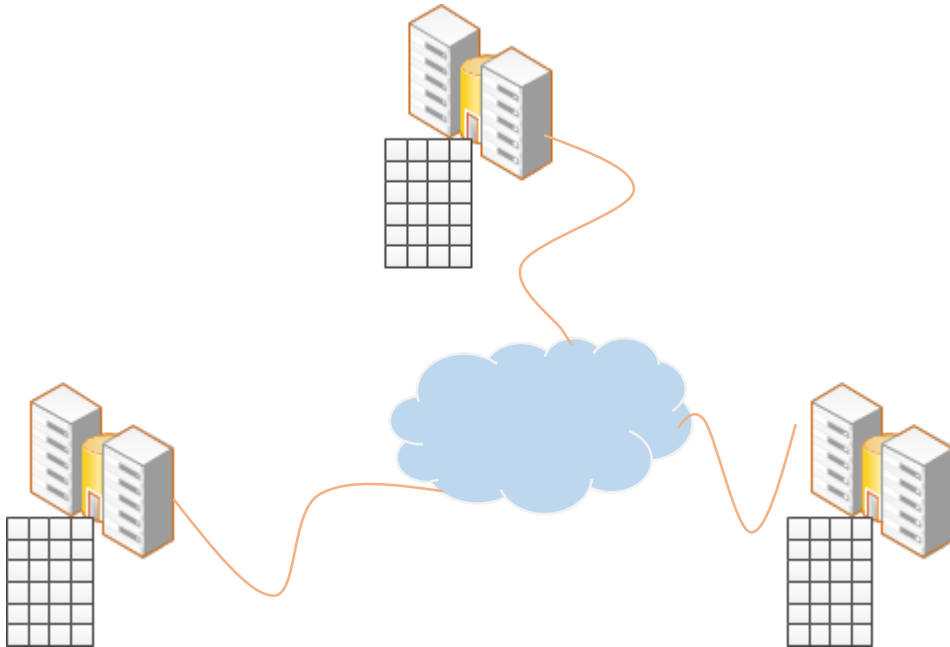
# Distributed graph generation

- Step 1: Preparing a distributed hash storage



# Distributed graph generation

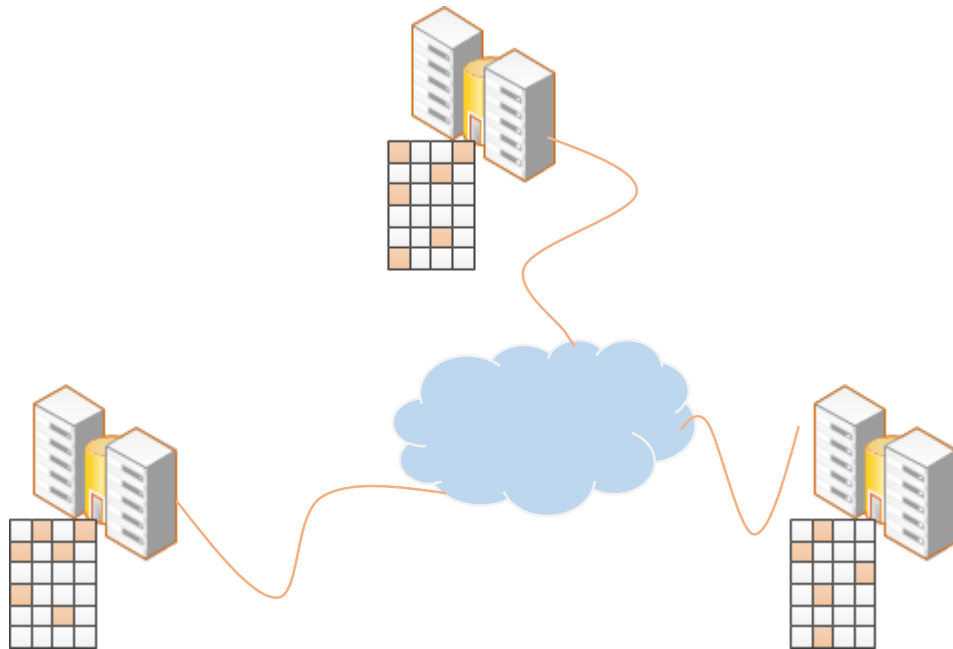
- Step 2: Generating the graph in parallel





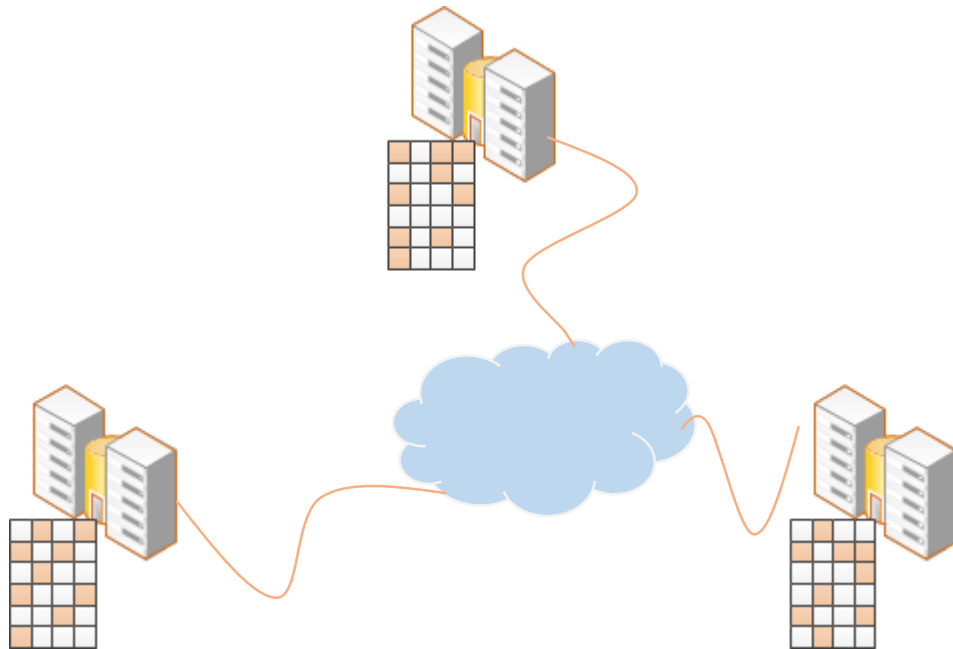
# Distributed graph generation

- Step 2: Generating the graph in parallel



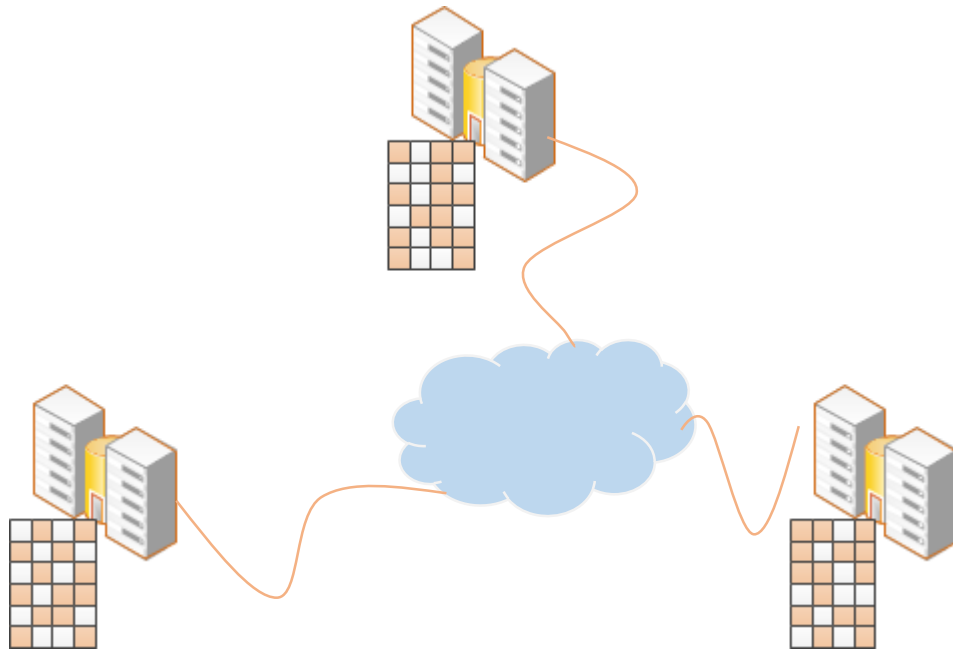
# Distributed graph generation

- Step 2: Generating the graph in parallel



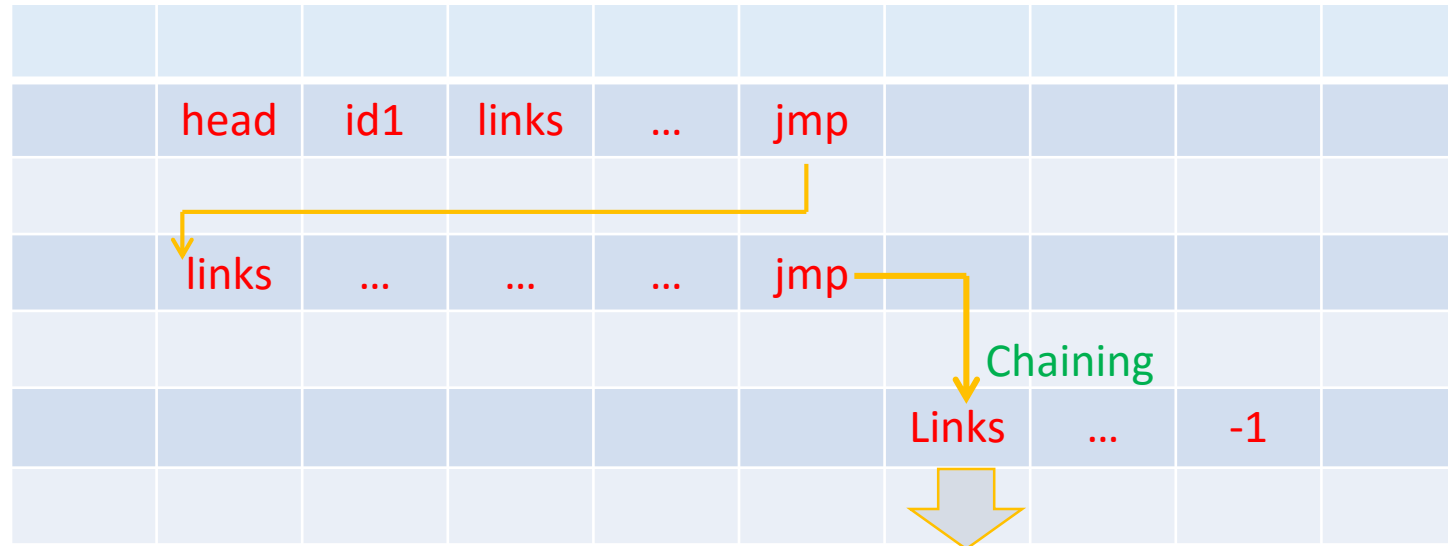
# Distributed graph generation

- Step 2: Generating the graph in parallel



# Distributed graph generation

- Step 3: Write the generated graph to disk



Packing memory segments into Graph nodes

# Hash Storage

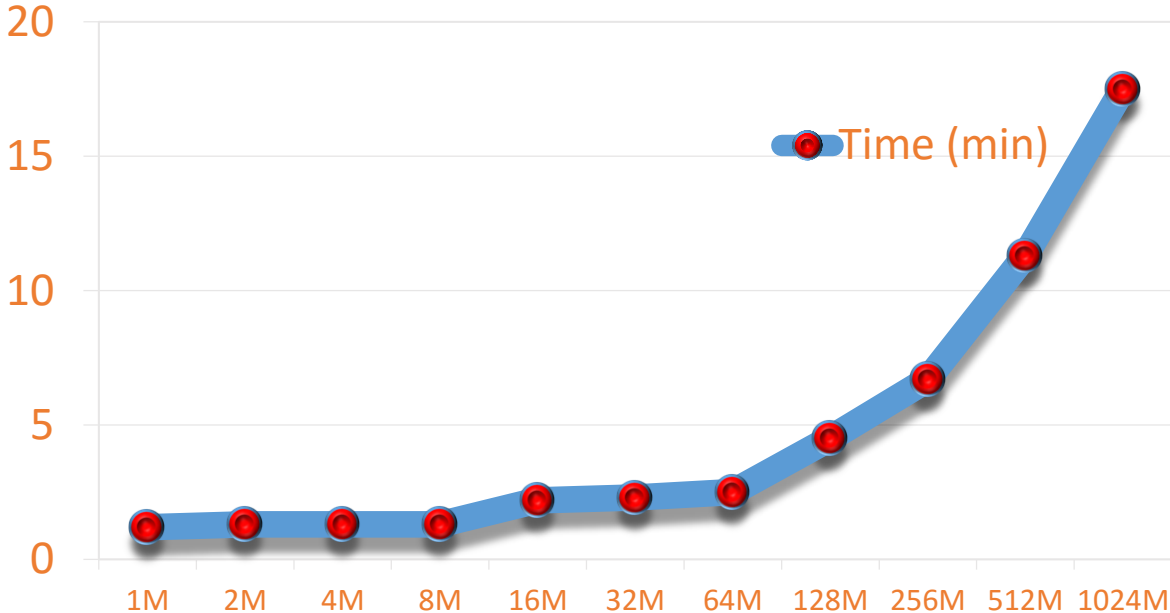
		head	id	links	-1				
	head	id	links	...	-1				
	head	id1	links	...	jmp	head	id	links	-1
	links	...	...	...	jmp	head	id	links	...
...	-1								
						Links...	...	-1	

or

In-memory key-value store

# An example

<http://www.graphengine.io/docs/manual/DemoApps/GraphGenerator.html>



# Outline

- Graph processing scenarios
- Challenges of large graph processing
- General design principles
- Offline analytics
- Online query processing
- Case study
- Graph generation
- **Other graph representations and their applications**

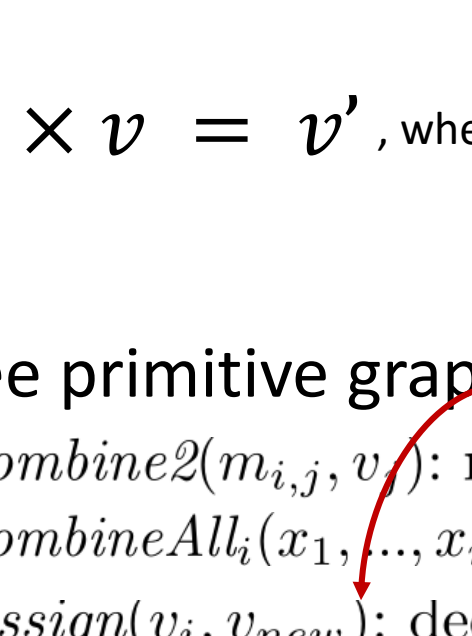
# Matrix arithmetic



# Representative System: Pegasus

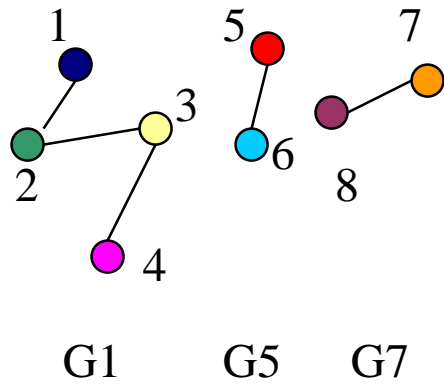
- Open source large graph mining system
  - Implemented on Hadoop
- Convert graph mining operations into iterative matrix-vector multiplication
- Pegasus uses a  $n$  by  $n$  matrix  $M$  and a vector  $v$  of size  $n$  to represent graph data

# Generalized Iterated Matrix-Vector Multiplication

$$M \times v = v', \text{ where } v'_i = \sum_{j=1}^n m_{i,j} \times v_j$$


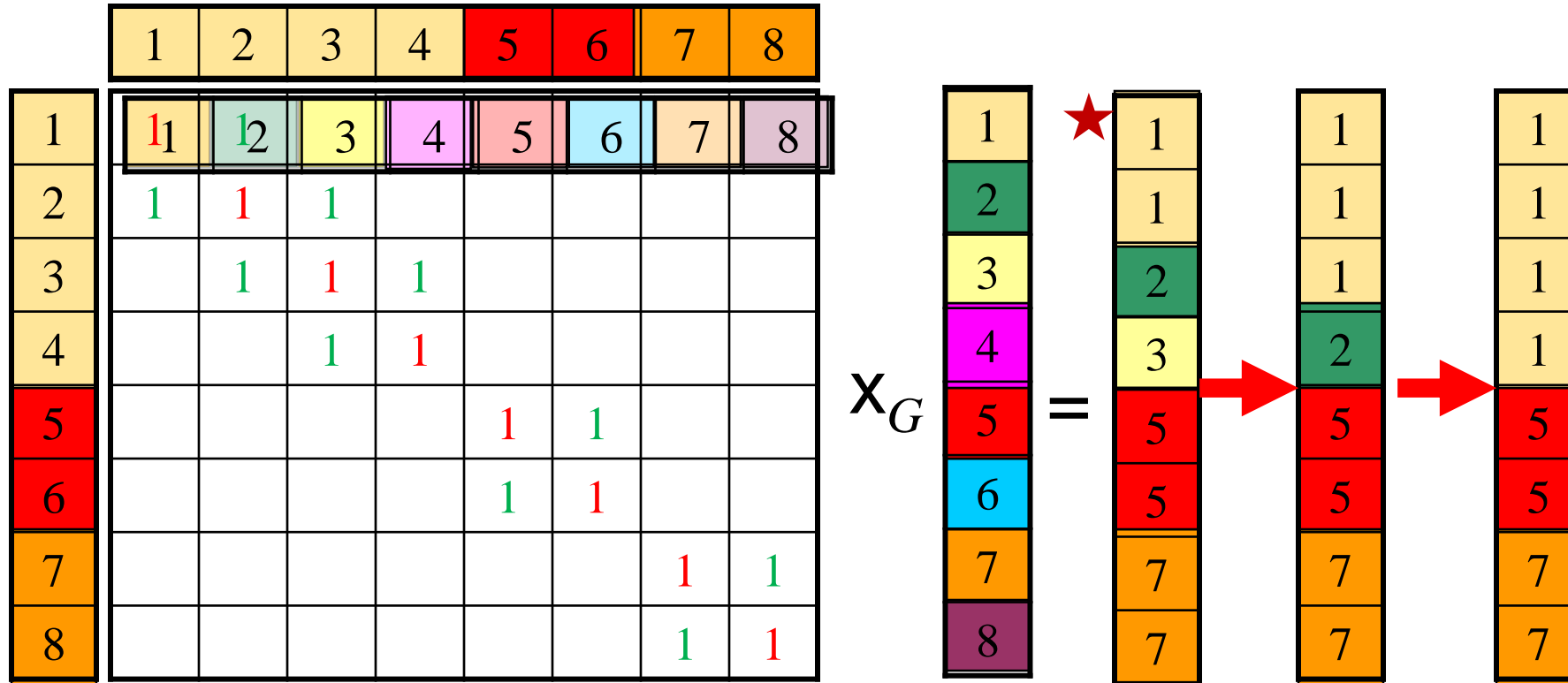
- Three primitive graph mining operations
  - $combine2(m_{i,j}, v_j)$ : multiply  $m_{i,j}$  and  $v_j$
  - $combineAll_i(x_1, \dots, x_n)$ : sum  $n$  all the multiplication results from  $combine2$
  - $assign(v_i, v_{new})$ : decide how to update  $v_i$  with  $v_{new}$
- Graph mining problems are solved by customizing the three operations

# Example: Connected Components



	1	2	3	4	5	6	7	8
1		1						
2	1		1					
3		1		1				
4			1					
5						1		
6					1			
7								1
8							1	

# Example: Connected Components

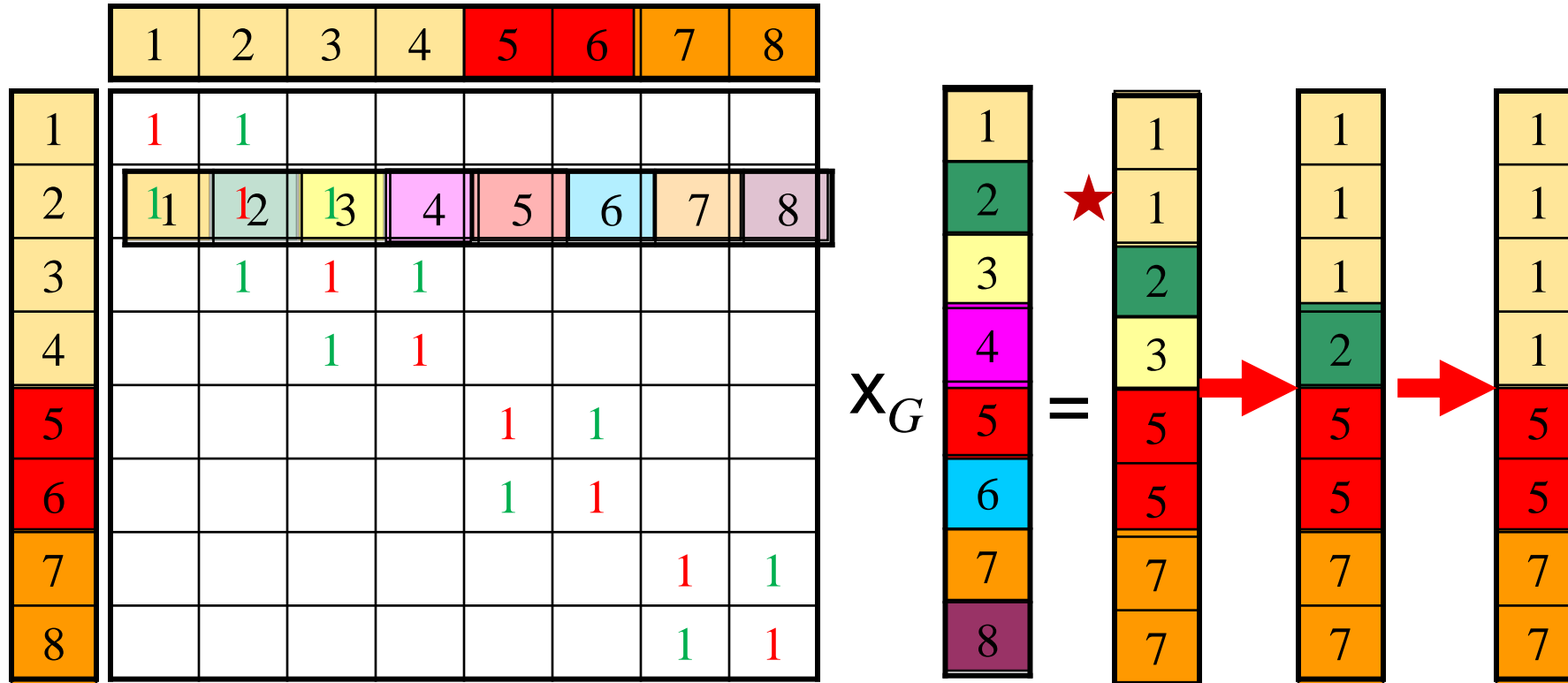


$\text{combine2}(m_{i,j}, v_j) = m_{i,j} \times v_j.$

$\text{combineAll}_i(x_1, \dots, x_n) = \text{MIN}\{x_j \mid j = 1..n\}$

$\text{assign}(v_i, v_{\text{new}}) = \text{MIN}(v_i, v_{\text{new}}).$

# Example: Connected Components

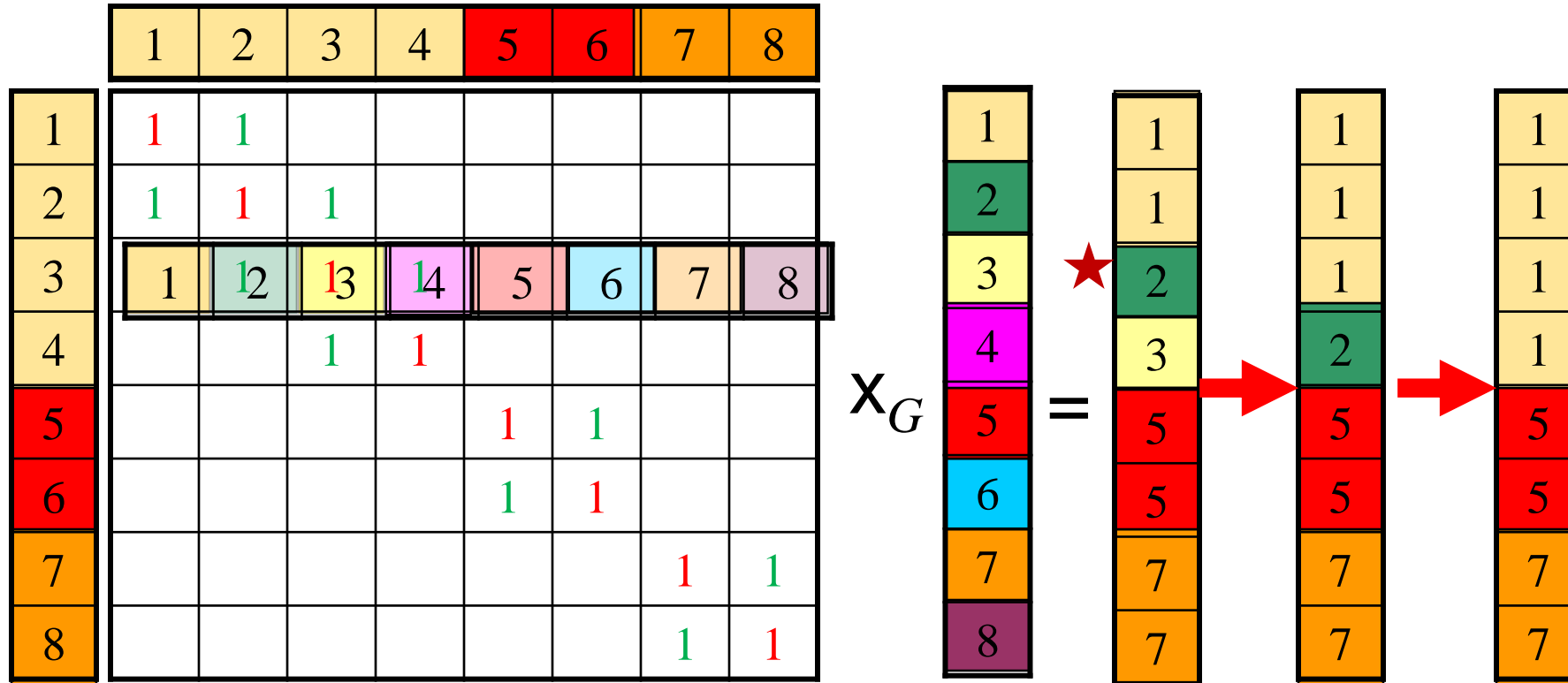


$\text{combine2}(m_{i,j}, v_j) = m_{i,j} \times v_j.$

$\text{combineAll}_i(x_1, \dots, x_n) = \text{MIN}\{x_j \mid j = 1..n\}$

$\text{assign}(v_i, v_{\text{new}}) = \text{MIN}(v_i, v_{\text{new}}).$

# Example: Connected Components

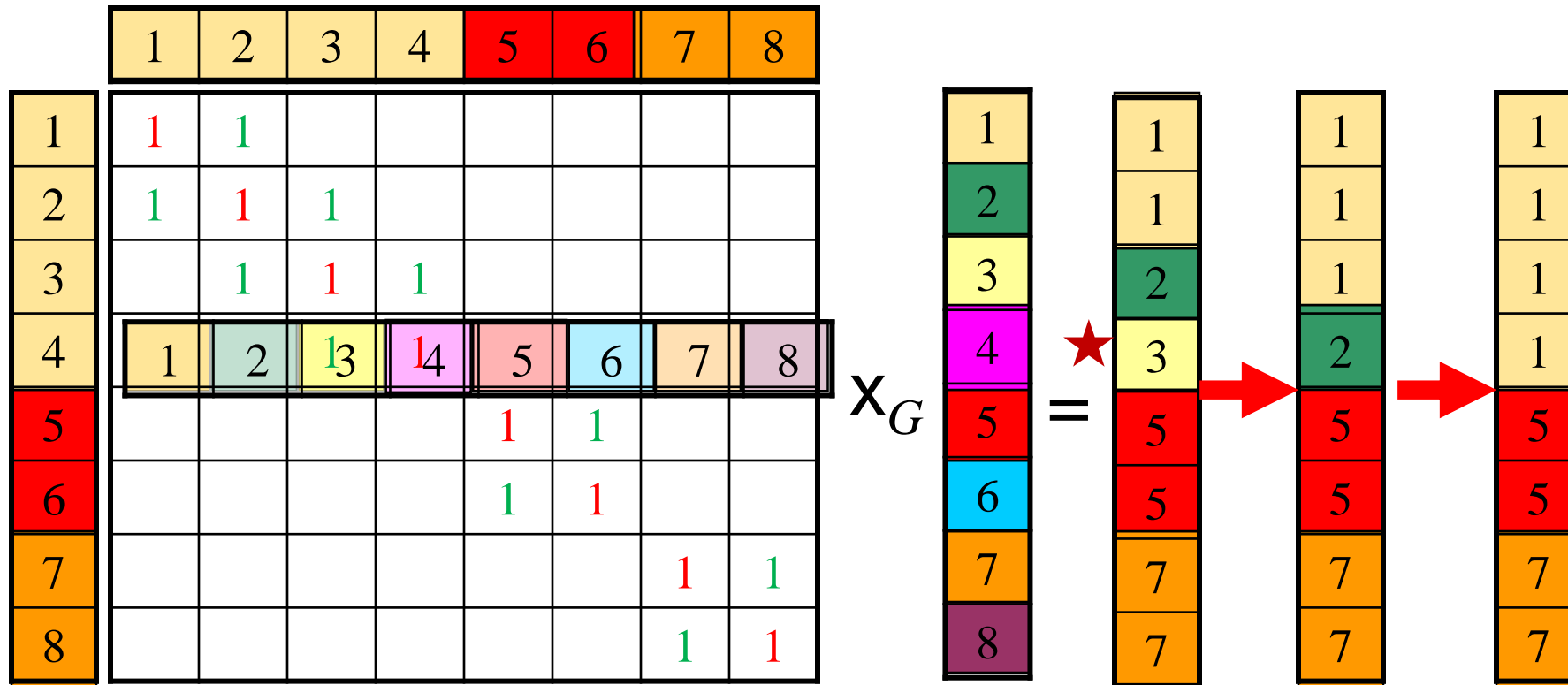


$\text{combine2}(m_{i,j}, v_j) = m_{i,j} \times v_j.$

$\text{combineAll}_i(x_1, \dots, x_n) = \text{MIN}\{x_j \mid j = 1..n\}$

$\text{assign}(v_i, v_{new}) = \text{MIN}(v_i, v_{new}).$

# Example: Connected Components

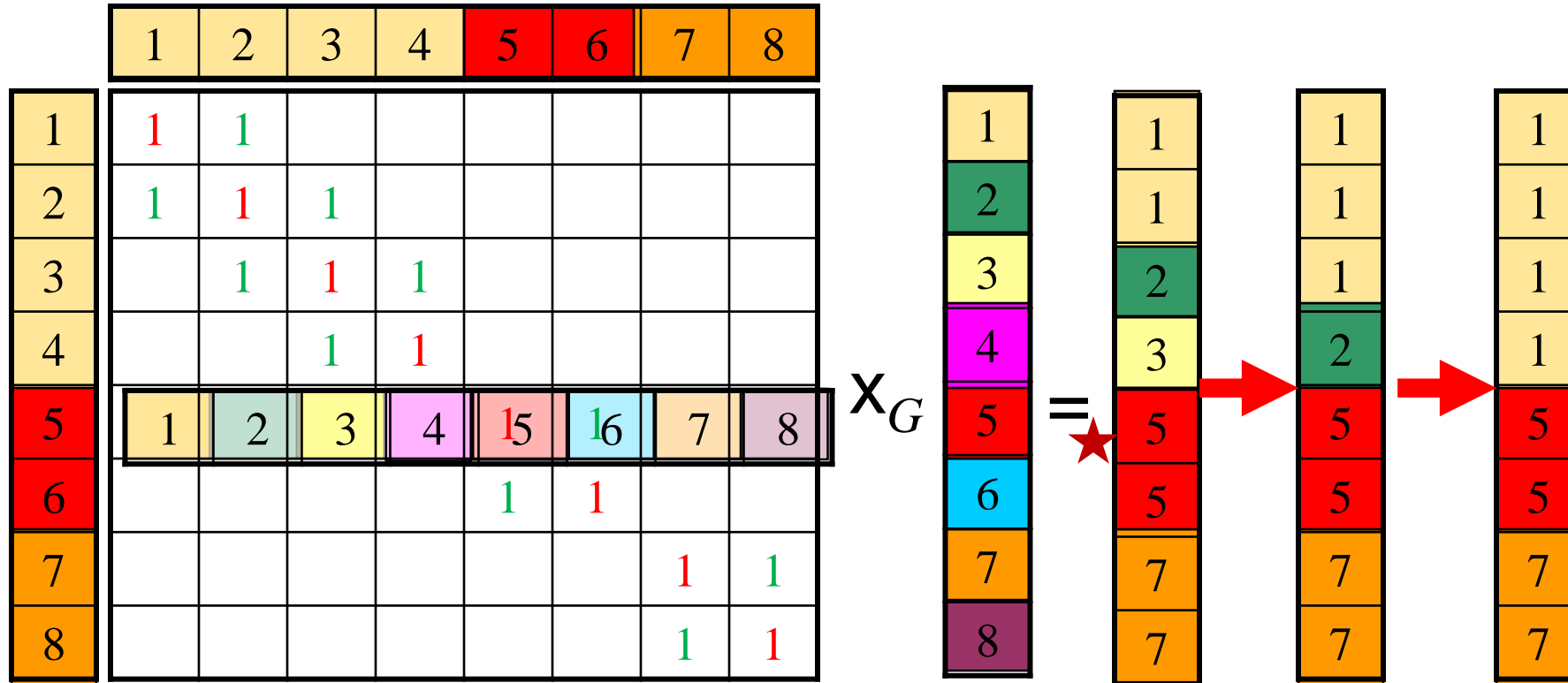


$\text{combine2}(m_{i,j}, v_j) = m_{i,j} \times v_j.$

$\text{combineAll}_i(x_1, \dots, x_n) = \text{MIN}\{x_j \mid j = 1..n\}$

$\text{assign}(v_i, v_{new}) = \text{MIN}(v_i, v_{new}).$

# Example: Connected Components



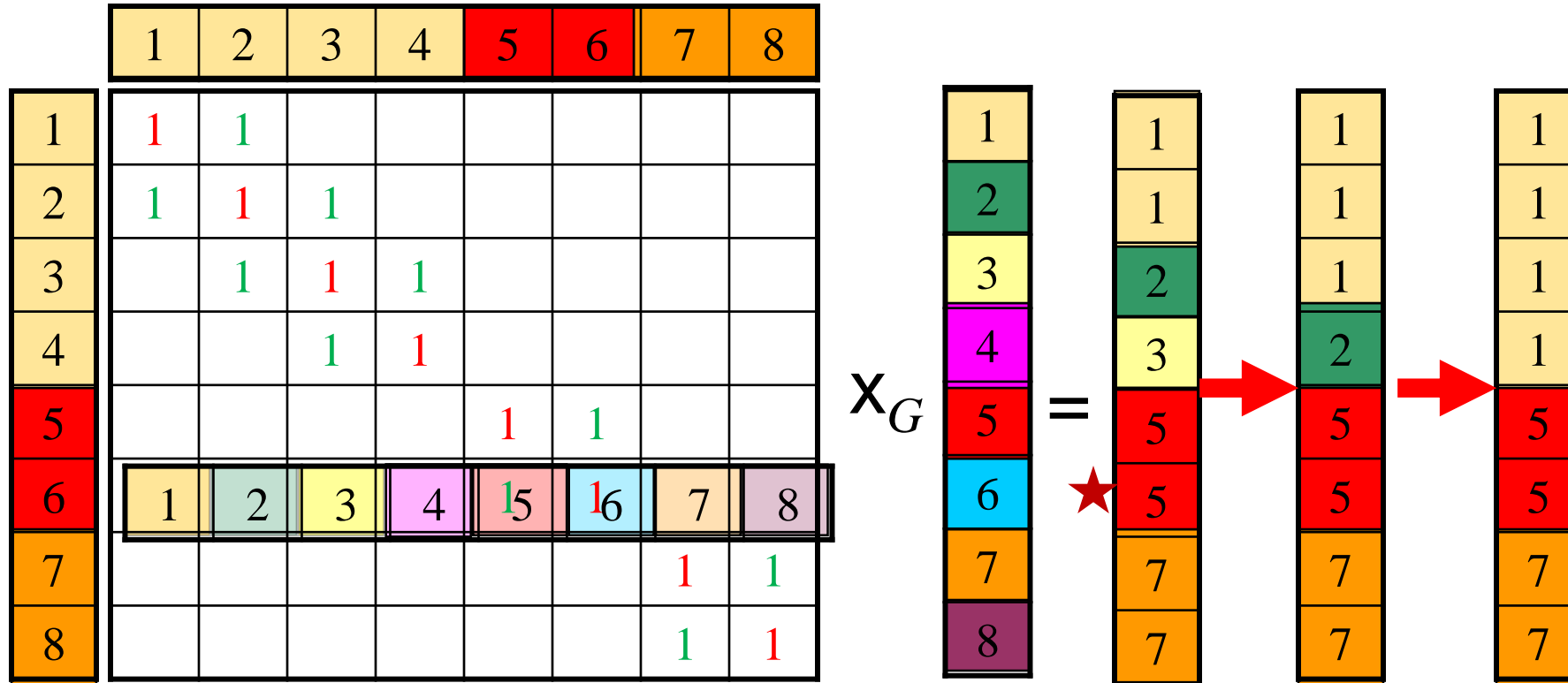
$\text{combine2}(m_{i,j}, v_j) = m_{i,j} \times v_j.$

$\text{combineAll}_i(x_1, \dots, x_n) = \text{MIN}\{x_j \mid j = 1..n\}$

$\text{assign}(v_i, v_{\text{new}}) = \text{MIN}(v_i, v_{\text{new}}).$



# Example: Connected Components

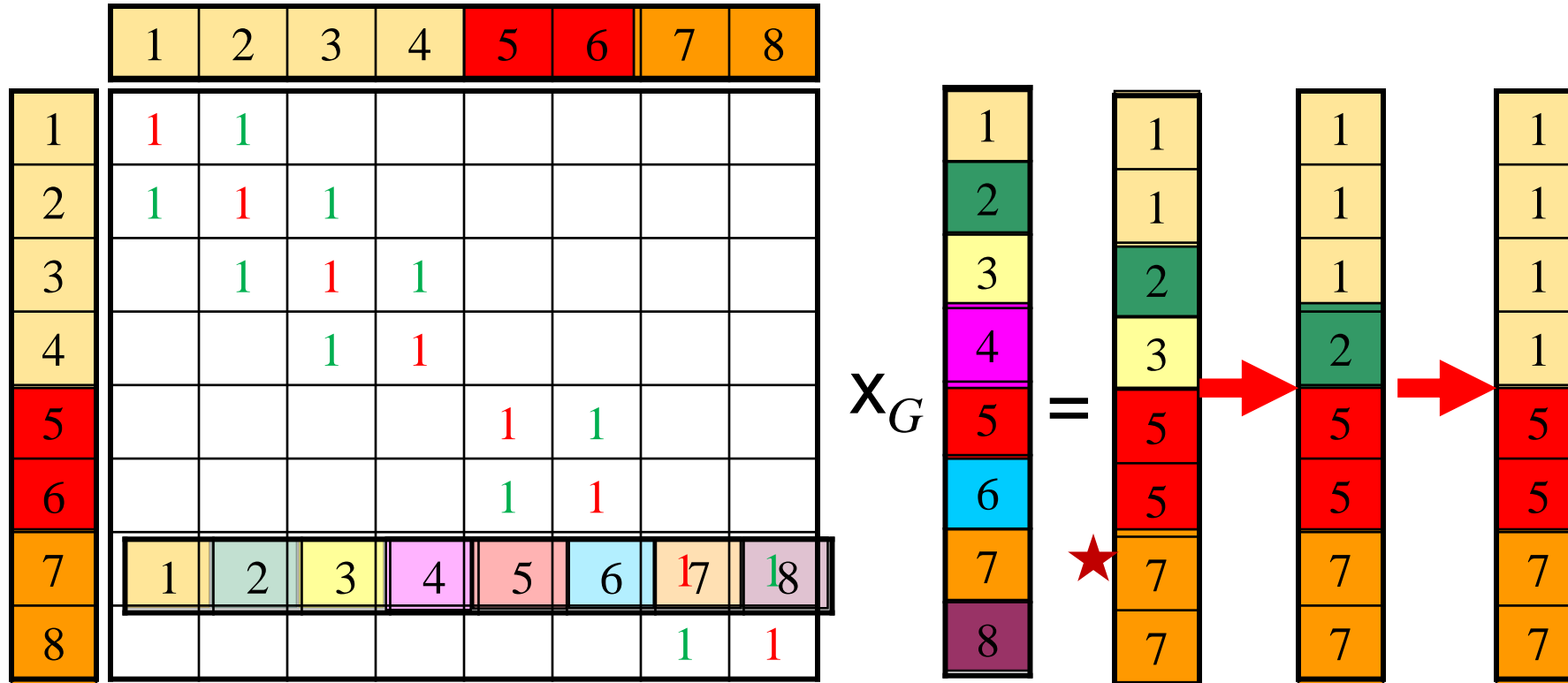


$\text{combine2}(m_{i,j}, v_j) = m_{i,j} \times v_j.$

$\text{combineAll}_i(x_1, \dots, x_n) = \text{MIN}\{x_j \mid j = 1..n\}$

$\text{assign}(v_i, v_{\text{new}}) = \text{MIN}(v_i, v_{\text{new}}).$

# Example: Connected Components

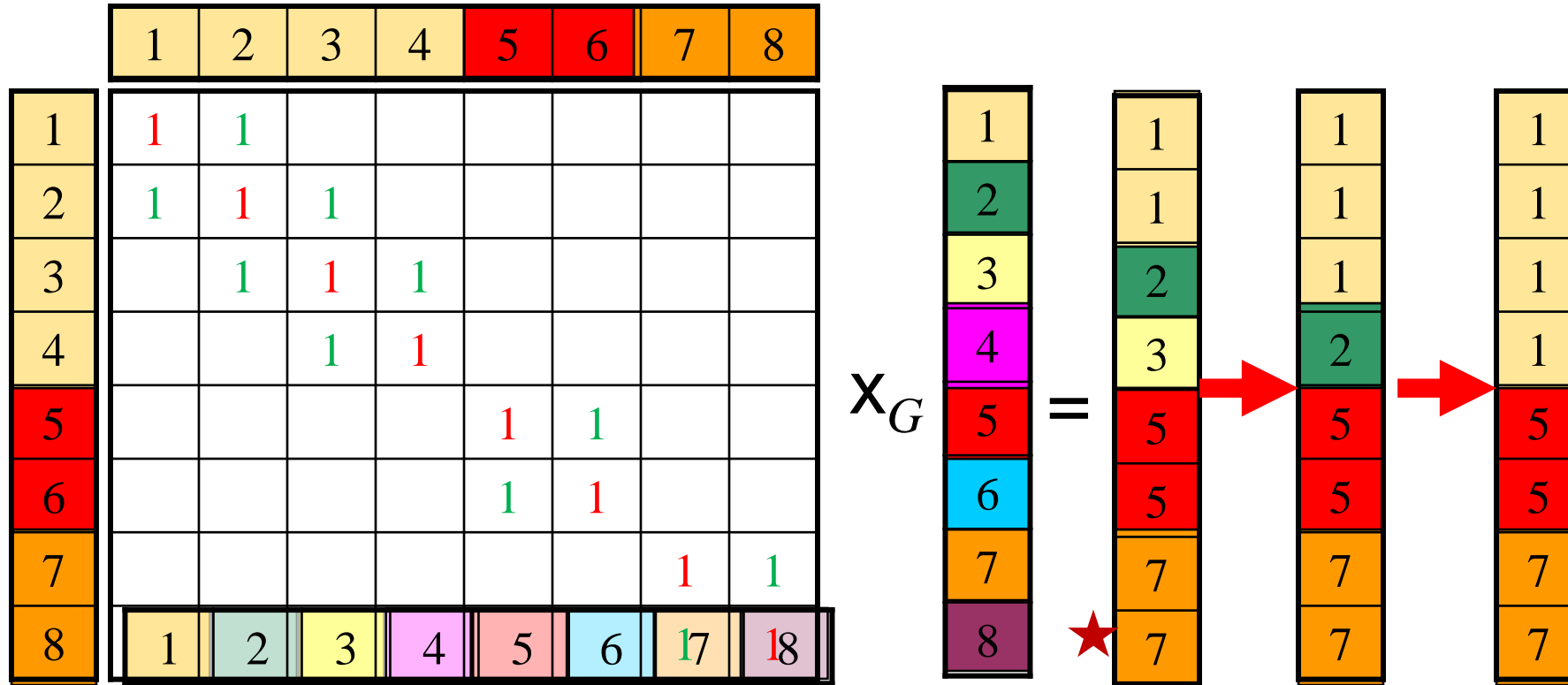


$\text{combine2}(m_{i,j}, v_j) = m_{i,j} \times v_j.$

$\text{combineAll}_i(x_1, \dots, x_n) = \text{MIN}\{x_j \mid j = 1..n\}$

$\text{assign}(v_i, v_{\text{new}}) = \text{MIN}(v_i, v_{\text{new}}).$

# Example: Connected Components



$\text{combine2}(m_{i,j}, v_j) = m_{i,j} \times v_j.$

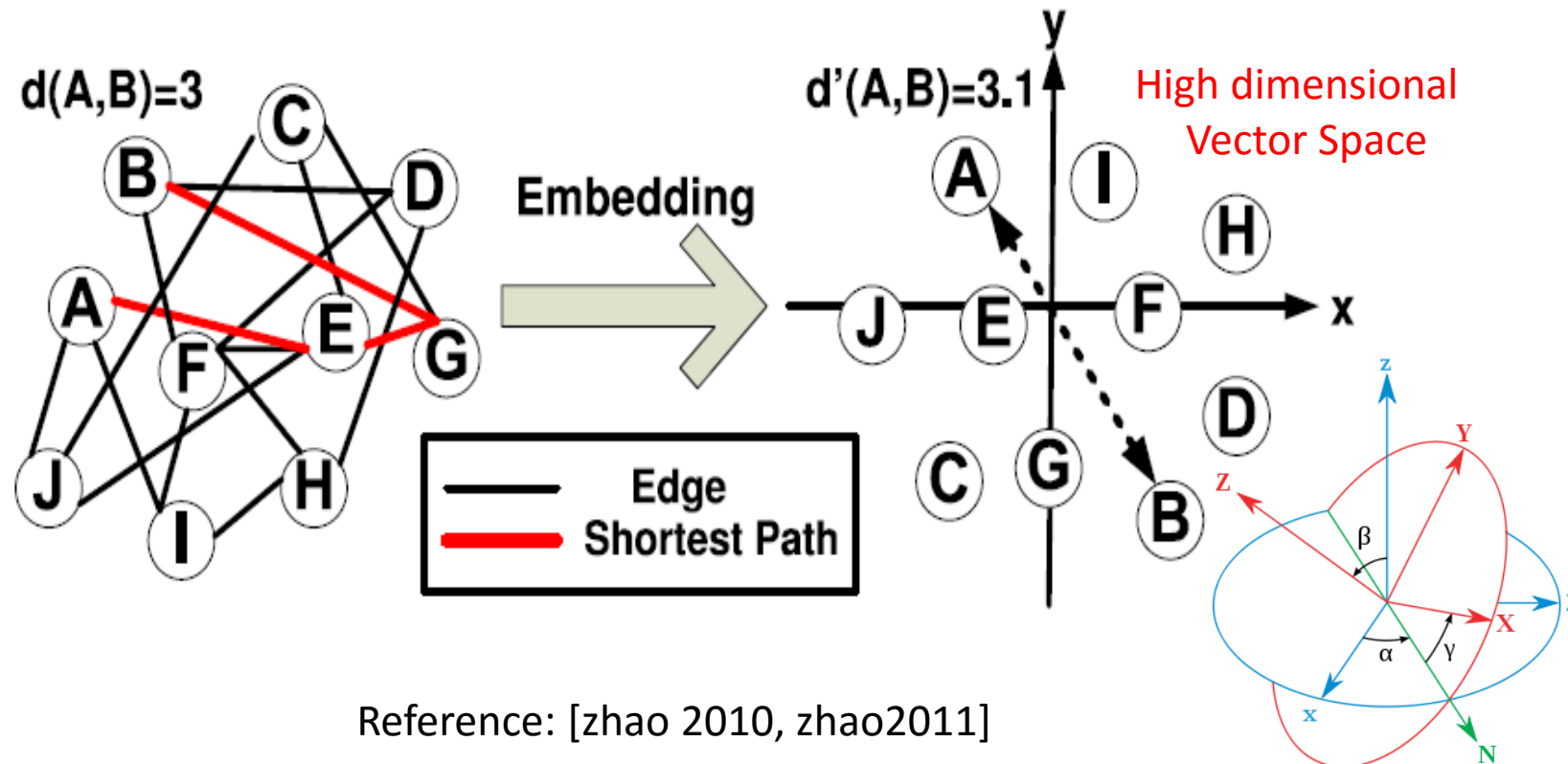
$\text{combineAll}_i(x_1, \dots, x_n) = \text{MIN}\{x_j \mid j = 1..n\}$

$\text{assign}(v_i, v_{\text{new}}) = \text{MIN}(v_i, v_{\text{new}}).$

# Graph embedding

# Graph Embedding

- Embed a graph into a geometric space so that distances in the space preserve the shortest distances in the graph



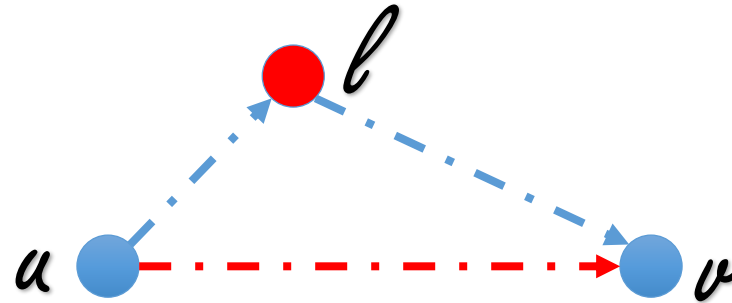
Reference: [zhao 2010, zhao2011]

# Application: Distance Oracle

- Choose a small number of landmarks (~100)
  - Heuristics: Degree , betweenness, ...
- Calculate the distance from each landmark to all other vertices using *BFS starting from each landmark*
- Calculate the embedding of landmarks using the *downhill simplex method* according to the distances between landmarks
- Calculate the embedding of other vertices using the *downhill simplex method* according to the distances from these vertices to landmarks

# Distance oracle in a nutshell

- Step 1: Using sketch to give the lower and upper bound of the shortest distance between two vertices



$$|d(u, l) - d(l, v)| \leq d(u, v) \leq d(u, l) + d(l, v)$$

Triangle Inequality

$$l(u, v) \leq d(u, v) \leq r(u, v)$$

# Distance oracle in a nutshell

- Step 2: Refining results using graph embedding

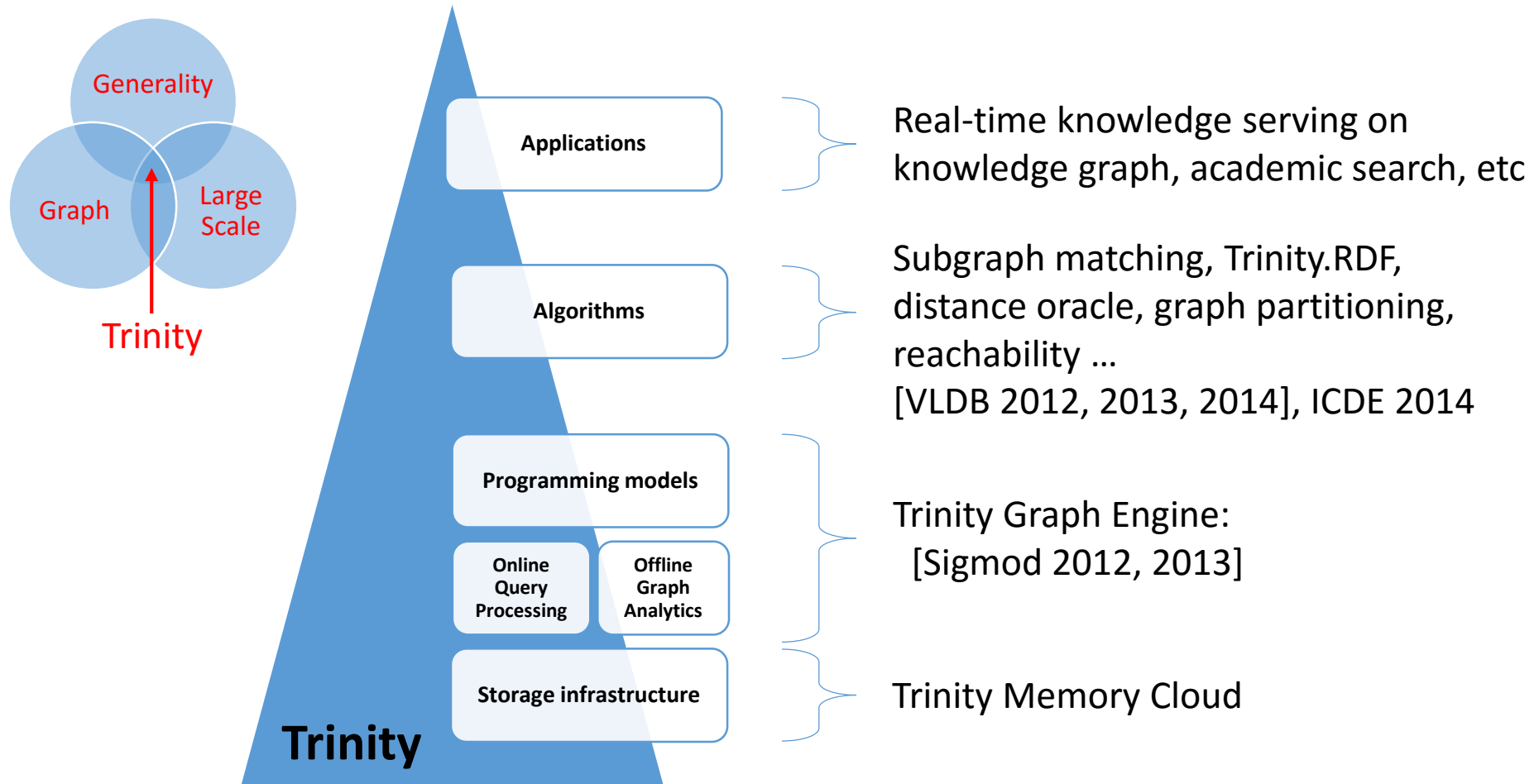
$$d(u, v) = \begin{cases} \bar{d}(u, v) & \text{if } l(u, v) \leq \bar{d}_{u,v} \leq r(u, v); \\ l(u, v) & \text{if } \bar{d}_{u,v} < l(u, v); \\ r(u, v) & \text{if } \bar{d}_{u,v} > r(u, v); \end{cases}$$

$\bar{d}(u, v)$  is the coordinate distance in the embedding space



# A Brief Introduction to Trinity Graph Engine

# Trinity Research Roadmap



# Design Philosophy

**Not a one-size-fits-all graph system, but a graph engine**

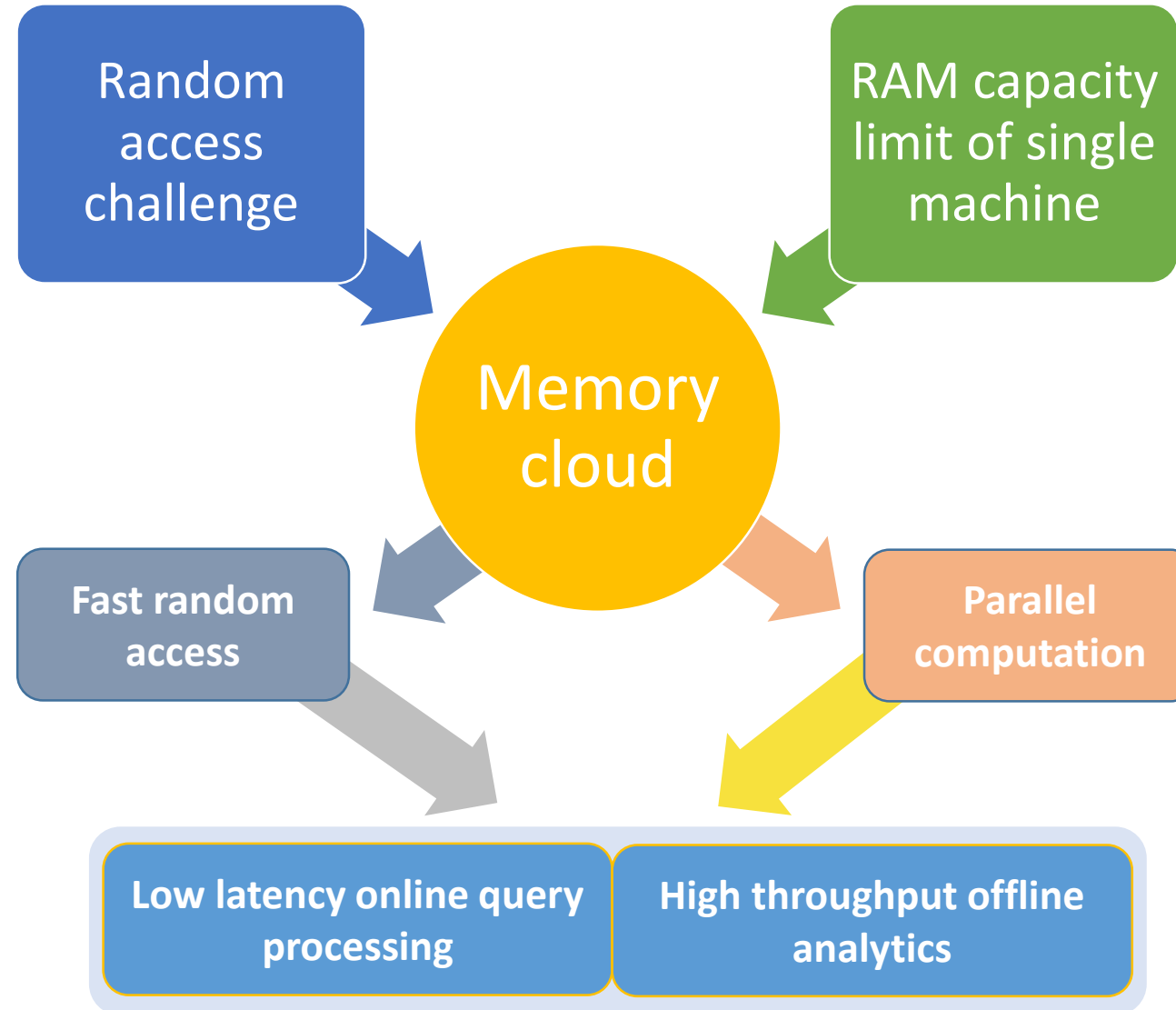
Flexible data and computation modeling capability



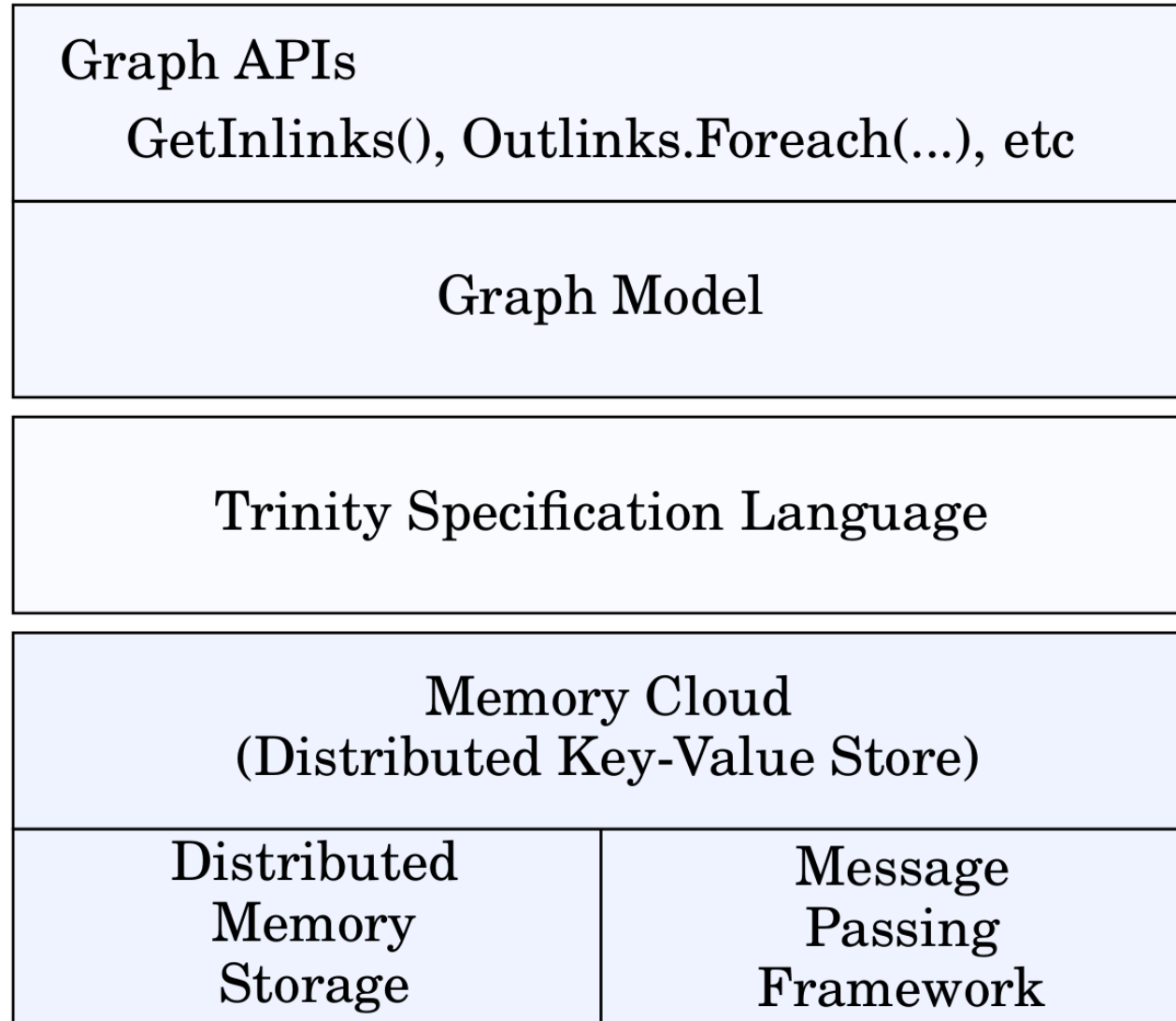
Trinity can morph into  
a large variety of graph processing systems

***Trinity* = Graph Modeling Tools +  
Distributed In-memory Data Store +  
Declarative Programming Model**

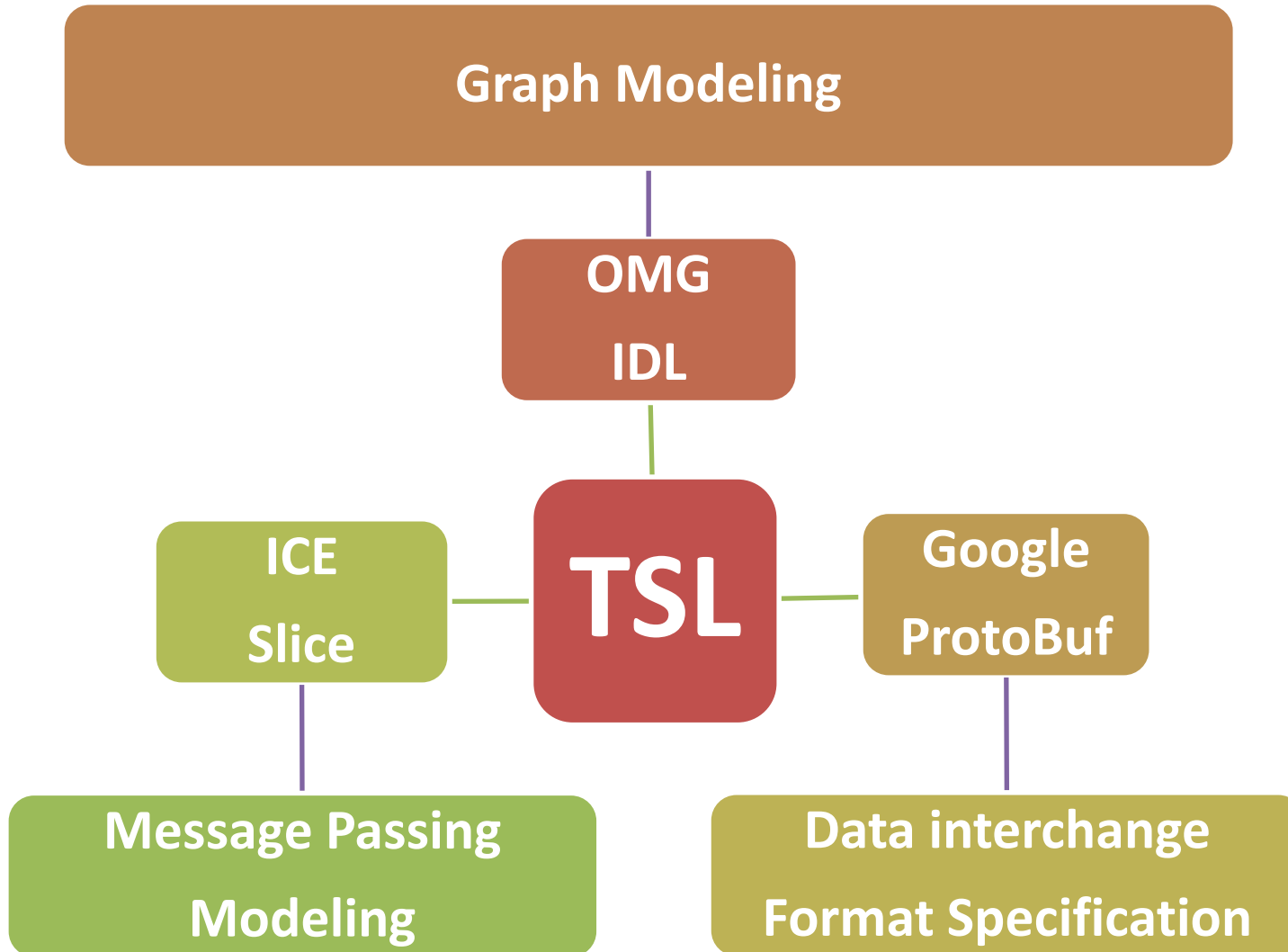
# Design Rationale of Memory Cloud



# System Stack



# Trinity Specification Language



# Why TSL?

- TSL allows users to define graph schemata, and communication protocols through declarative interfaces.
- TSL makes Trinity memory cloud beyond a key-value store
  - Users are allowed to freely define the data schema
  - TSL makes message passing programming ever so easy

# Modeling a Movie and Actor Graph

```
[CellType: NodeCell]
cell struct Movie
{
    string Name;
    [EdgeType: SimpleEdge, ReferencedCell: Actor]
    List<long> Actors;
}
[CellType: NodeCell]
cell struct Actor
{
    string Name;
    [EdgeType: SimpleEdge, ReferencedCell: Movie]
    List<long> Movies;
}
```





# Modeling Message Passing

```
struct MyMessage
{
    string Text;
}
protocol Echo
{
    Type: Syn;
    Request: MyMessage;
    Response: MyMessage;
}
```

# Trinity-enabled Graph Computation Paradigms

- **Vertex-centric graph analytics**
  - Prosperous since Pregel, e.g. Giraph, GraphChi
- **Approximate graph computation based on local sampling**
  - Enabled by randomly partitioned in-memory graph
  - Fast approximate computation with minimum communication costs
  - Application: distance oracle [VLDB 2014]
- **Index-free real-time online query processing**
  - Enabled by fast in-memory distributed graph exploration
  - Examples, subgraph match (vldb 2012) and Trinity.RDF (vldb 2013)



# Graph Engine

SERVING BIG GRAPH IN REAL-TIME

<http://www.graphengine.io/>

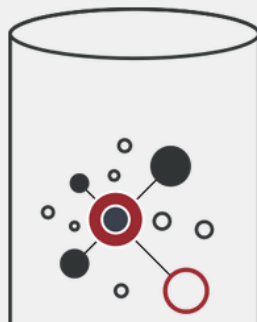
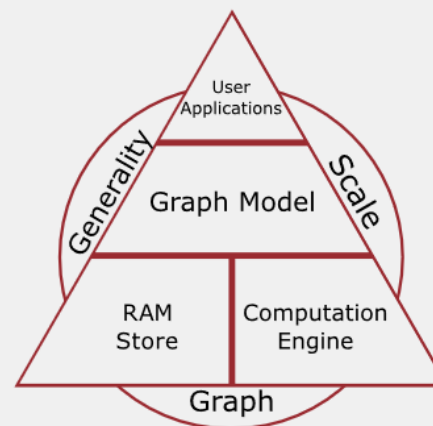
## Graph Engine

= **RAM Store + Computation Engine + Graph Model**

Graph Engine (GE) is a highly modularized graph processing system, underpinned by a strongly-typed RAM store and a general computation engine.

The distributed RAM store provides a globally addressable high-performance key-value store over a cluster of machines. Through the RAM store, GE enables the fast random data access power over a large distributed data set.

The capability of fast data exploration and distributed parallel computing makes GE a natural large graph processing platform. GE supports both low-latency online query processing and high-throughput offline analytics on billion-node large graphs.



## Strongly-typed RAM Store

### Schema Matters

Schema does matter when we need to process data efficiently. Strongly-typed data modeling is crucial for compact data storage, fast data access, and clear data semantics.

### One Byte Counts

GE is good at managing billions of run-time objects of varied sizes. One byte counts as the number of objects goes large. GE provides fast memory allocation and efficient memory reallocation with

# Thanks!

<http://www.graphengine.io/>